

1 Four-dimensional NOE-NOE spectroscopy of SARS-CoV-2 Main  
2 Protease to facilitate resonance assignment and structural analysis

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19 This study is dedicated to Robert Kaptein on the occasion of his 80<sup>th</sup> birthday

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21 **ABSTRACT.** Resonance assignment and structural studies of larger proteins by NMR can be  
22 challenging when exchange broadening, multiple stable conformations, and **<sup>1</sup>H back-exchange of**  
23 the fully deuterated chain pose problems. These difficulties arise for the SARS-CoV-2 Main  
24 Protease, a homodimer of 2×306 residues. We demonstrate that the combination of four-  
25 dimensional (4D) TROSY-NOESY-TROSY spectroscopy and 4D NOESY-NOESY-TROSY  
26 spectroscopy provides an effective tool for delineating the <sup>1</sup>H-<sup>1</sup>H dipolar relaxation network. In  
27 combination with detailed structural information obtained from prior X-ray crystallography work,  
28 such data are particularly useful for extending and validating resonance assignments, as well as  
29 for probing structural features.

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## 30 **1. Introduction**

31 The extension of conventional two-dimensional <sup>1</sup>H-<sup>1</sup>H NMR spectroscopy of natural proteins  
32 (Wüthrich, 1986) to three-dimensional (3D) homonuclear NMR experiments offered the ability to  
33 simplify spectral analysis by removing resonance overlap (Vuister et al., 1988; Oschkinat et al.,  
34 1988) and by providing access to a direct, more detailed analysis of <sup>1</sup>H-<sup>1</sup>H dipolar cross relaxation  
35 networks. In particular, the homonuclear 3D NOE-NOE experiment (Boelens et al., 1989; Breg et  
36 al., 1990) not only decreased resonance overlap, it also directly elucidated spin-diffusion pathways.  
37 This information complemented and validated the elegant relaxation matrix analysis of spin  
38 diffusion (Boelens et al., 1988).

39 Such homonuclear <sup>1</sup>H 3D experiments and analysis strategies were soon followed by a myriad of  
40 heteronuclear 3D experiments that required isotopic enrichment, and therefore cloning and  
41 bacterial overexpression (Marion et al., 1989b; Zuiderweg and Fesik, 1989; Ikura et al.,  
42 1990; Marion et al., 1989a; Wagner, 1993). Most of these heteronuclear experiments simply served  
43 to disperse the regular <sup>1</sup>H-<sup>1</sup>H 2D spectrum into a third dimension, thereby removing spectral  
44 overlap but providing little or no new information on the all-important <sup>1</sup>H-<sup>1</sup>H spin diffusion  
45 pathways. The 3D NOESY-HMQC experiment (Marion et al., 1989b; Zuiderweg and Fesik, 1989)  
46 subsequently was extended to four dimensions (4D), thereby dispersing the conventional 2D <sup>1</sup>H-  
47 <sup>1</sup>H NOESY experiment into two additional dimensions that correspond to the chemical shifts of  
48 the nuclei to which each of the protons is covalently bound (Kay et al., 1990; Clore et al.,  
49 1991; Zuiderweg et al., 1991).

50 These multi-dimensional experiments provided a tremendous degree of spectral simplification, in  
51 particular after appropriate analysis software became available. However, it also quickly became  
52 clear that extension to large, slowly tumbling proteins was hampered by low signal-to-noise,  
53 caused by the relative inefficiency of the magnetization transfer steps when the dimensionality of  
54 a spectrum is increased. This decrease in sensitivity was remedied by generating the protein in a  
55 highly perdeuterated state, while keeping the solvent-exchangeable backbone amide protons  
56 protonated (Torchia et al., 1988; Lemaster and Richards, 1988). Combining the perdeuteration  
57 approach with both the triple resonance assignment strategy (Grzesiek et al., 1993) and the  
58 subsequently introduced powerful TROSY line-narrowing method (Pervushin et al., 1997) made  
59 it possible to assign and analyze the structure of quite large proteins, as exemplified by the 723-  
60 residue protein malate synthase G (Tugarinov et al., 2002; Tugarinov et al., 2005a). The sensitivity  
61 gained by perdeuteration, enabling the recording of 4D  $^{15}\text{N}$ -separated NOE spectra, also was key  
62 in solving the structure of a HIV-1 accessory protein that had been too challenging for analysis by  
63 more conventional methods (Grzesiek et al., 1995). **Zhu and co-workers introduced a TROSY-  
64 NOESY-TROSY version of Grzesiek's 4D NOESY experiment which, illustrated for a partially  
65 deuterated 27 kDa protein, yielded further improved sensitivity and intrinsic  $^1\text{H}$  and  $^{15}\text{N}$  line widths  
66 (Xia et al., 2000). Their implementation relied on eight-step phase cycling, thereby limiting  
67 digitization of the time domain data and unable to exploit the improved TROSY relaxation in the  
68 indirect dimensions. Diercks *et al.* introduced an elegant method to suppress diagonal signals from  
69 a 4D TROSY-NOESY-TROSY spectrum (Diercks et al., 2010), a particularly useful feature when  
70 spectral resolution is limited. However, we opted not to use this implementation as, at the long  
71 mixing times used, the diagonal resonances serve as convenient reference anchors during analysis  
72 and are sufficiently attenuated such as not to obscure nearby peaks in our 4D spectra that are of  
73 very high digital resolution.**

74 In the present report, we merge the above-mentioned prior advances, 3D NOE-NOE and 3D  $^{15}\text{N}$ -  
75 separated NOESY, into a 4D experiment. **In combination with extensive perdeuteration and  
76 gradient-enhanced encoding to enable a four-step phase cycle as well as non-uniform sampling  
77 (NUS) (Rovnyak et al., 2004), the experiments take better advantage of the improved resolution  
78 afforded by 4D NMR.** We demonstrate the utility of the experiments by applying them to the study  
79 of the main protease of SARS-CoV-2 ( $\text{M}^{\text{pro}}$ ) which is the virus responsible for coronavirus-2019  
80 disease (COVID-19).  $\text{M}^{\text{pro}}$ , also known as 3CL $^{\text{pro}}$  or Nsp5, is a homodimeric cysteine protease of

81 2×306 residues that does not have closely related mammalian homologues and is therefore an  
82 intense target for drug development, with a promising inhibitor now entered in a phase I clinical  
83 trial (Boras et al., 2021). Its NMR analysis is challenging, not only for its large size (67.6 kD), but  
84 also because of the presence of a minor conformer associated with the cis-isomer of one of its 13  
85 Pro residues (P184), the difficulty in back-exchanging all backbone amide protons when the  
86 protein is expressed in <sup>2</sup>H<sub>2</sub>O, and the presence of intermediate time scale motions that lead to  
87 exchange broadening in the vicinity of the protein's active site. Here we focus on an enzyme  
88 variant where the catalytic Cys145 residue has been mutated to Ala (M<sup>Pro</sup><sub>C145A</sub>), a construct that is  
89 stable for multiple weeks at the high concentrations required for NMR spectroscopy. The  
90 assignment process and a full structural analysis of the protein will be presented elsewhere. The  
91 focus of the present work is on technical innovations, including recording two types of 4D NOE-  
92 based NMR spectra that proved invaluable both for the validation of resonance assignments, as  
93 well as the subsequent structural analysis.

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## 95 **2. Methods and Experiments**

### 96 **2.1 Protein production**

97 The gene encoding a C145A variant of M<sup>Pro</sup> (M<sup>Pro</sup><sub>C145A</sub>) with an N-terminal affinity (and  
98 solubility), tag was synthesized by GenScript (USA) and then cloned into a Pet24a+ plasmid  
99 between BamH1 and Xho1 restriction sites. The fusion protein encoded for 6His tag – GB1–SG  
100 rich linker–TEV cleavage site – M<sup>Pro</sup><sub>C145A</sub>, and was purified according to methods collectively  
101 developed by the COVID-19 NMR consortium (Altincekic, 2021). In brief, following cell culture  
102 and harvesting (see Supporting Information), the cell lysate was passed down a 6His-affinity  
103 column (IMAC) and eluted in a small volume; the solubility tag was cleaved off to generate a  
104 native N-terminus; the reaction mix was then passed through an IMAC column to remove  
105 uncleaved protein, before size separation on a Sephadex G75 column. **The resulting, extensively  
106 perdeuterated, <sup>2</sup>H,<sup>15</sup>N-M<sup>Pro</sup><sub>C145A</sub> homo dimer was used for experiments and throughout the  
107 recombinant protein expression, extensive care was taken to achieve a high (>~98%) level of  
108 deuteration of the non-exchangeable hydrogens. For more detail, see Supporting Information.**

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### 110 **2.2 Recording of NMR data**

111 Spectra were acquired on a sample containing 1.8 mM (0.9 mM dimer) <sup>2</sup>H,<sup>15</sup>N-M<sup>Pro</sup><sub>C145A</sub> in 10 mM

112 sodium phosphate, pH 7.0, 0.5 mM TCEP, 3% v/v  $^2\text{H}_2\text{O}$  and 0.3 mM sodium  
113 trimethylsilylpropanesulfonate (DSS; as an internal chemical shift reference), in a 300  $\mu\text{L}$  Shigemi  
114 microcell. All experiments were recorded at 25  $^\circ\text{C}$  on an 800 MHz Bruker Avance III spectrometer,  
115 equipped with a 5-mm TCI probe containing a triple-axis gradient accessory, and running TopSpin  
116 software version 3.1.

117 Considering that the measurements are carried out for perdeuterated protein, the spectral windows  
118 in the indirect  $^1\text{H}$  dimensions were limited to the region downfield from the water resonance, and  
119 EBURP2 pulses (Geen and Freeman, 1991) were used where needed to prevent excitation of  
120 protons outside of this region. For the 4D TROSY-NOESY-TROSY experiment (Fig. 1a), only a  
121 small fraction (0.54%) of the full data matrix, consisting of  $1536 * (^1\text{H}, t_4, 119.8 \text{ ms}) \times 90 * (^{15}\text{N},$   
122  $t_3, 35.1 \text{ ms}) \times 91 * (^1\text{H}, t_2, 20.0 \text{ ms}) \times 90 * (^{15}\text{N}, t_1, 35.1 \text{ ms})$  complex points, was recorded (SI Table  
123 S1) using nonuniform sampling for the indirect dimensions. Selection of the sampled data points  
124 was unweighted, randomly distributed, and without time-ordering. The sampling schedule  
125 (included in the uploaded data sets, see Data availability) was automatically generated by Topspin  
126 3.1 when the experiment started, with the random seed left to its default value (54321) and the  $T_2$   
127 for each indirect dimension set to 1 second to avoid significant weighting of the sampling schedule.  
128 Specifically, a total of 31896 FIDs along the directly detected  $t_4$  dimension were recorded. Using  
129 4 scans per FID for phase cycling, and an interscan delay of 2.07 seconds, the total measurement  
130 time was approximately 88 hours, but three-fold shorter would have sufficed (see Concluding  
131 remarks).

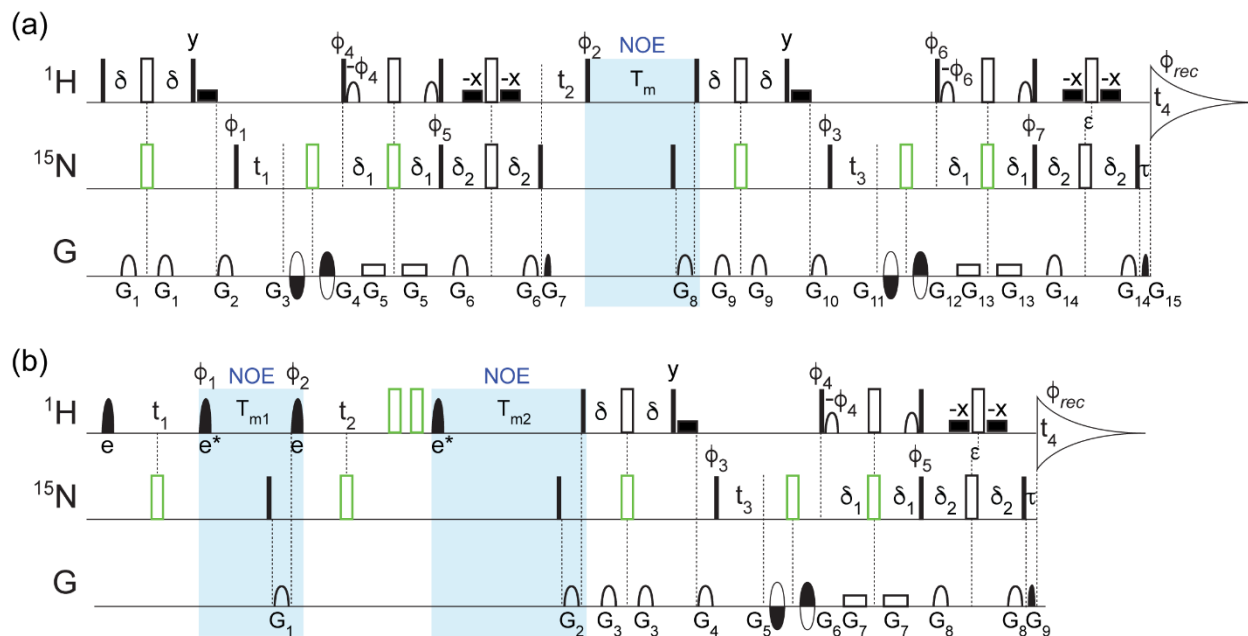
132 Nonstandard processing was needed for the TROSY-NOESY-TROSY experiment because the  
133 spectrum was recorded with sensitivity-enhanced gradient selection in the  $^{15}\text{N}$   $t_1$  evolution period  
134 that preceded the NOE mixing (Xia et al., 2000). Specifically, the 4D NUS data set was first sorted  
135 and expanded according to the sampling schedule using the *nusExpand.tcl* script within the  
136 NMRPipe software package (Delaglio et al., 1995). The expanded data was then converted to the  
137 NMRPipe format, with the quadrature mode for  $t_3$  set to *Echo-AntiEcho*, while the quadrature  
138 mode for  $t_1$  was temporarily set to *Complex*. After the conversion, the 4D matrix needs to be  
139 transposed to enable use of the NMRPipe macro *bruk\_ranceA.M* to correctly reshuffle the data,  
140 turning the phase-modulated  $t_1$  dimension into conventional amplitude modulated data prior to  
141 processing as regular, complex data. This transposition is accomplished by reading in the  
142 NMRPipe-formatted matrix with the z-axis along the  $t_2$  dimension, application of the macro, and

143 restoring the data to its original axis order prior to regular processing, with the full script included  
144 with the raw time domain data sets (see Data availability). For the processing, the direct dimension  
145 was apodized with a squared, shifted sine bell window, spanning from  $72^\circ$  to  $176.4^\circ$ , whereas an  
146 additional 15 Hz exponential line broadening was used to better match the apodization window to  
147 the natural decay of the signal, thereby improving the signal to noise ratio (S/N). This was  
148 followed by zero filling and Fourier transformation. Subsequently, the indirect data points that  
149 were not experimentally sampled were reconstructed using the SMILE (Ying et al., 2017) program,  
150 and the reconstructed data was further processed in NMRPipe. To enhance the spectral resolution,  
151 by default the acquisition times in all indirect dimensions were extended by 50% during the SMILE  
152 reconstruction, leading to an effective sampling sparsity of 0.16%. The data matrix for the final  
153 reconstructed 4D spectrum consists of  $614 (^1\text{H}, F_4, 6.3 \text{ Hz/point}) \times 512 (^{15}\text{N}, F_3, 5.0 \text{ Hz/point}) \times$   
154  $512 (^1\text{H}, F_2, 8.9 \text{ Hz/point}) \times 512 (^{15}\text{N}, F_1, 5.0 \text{ Hz/point})$  real points (see SI Table S1).  
155 The full time-domain data matrix of the 4D NOESY-NOESY-TROSY experiment (Fig. 1b)  
156 consists of  $1536 (^1\text{H}, t_4, 95.8 \text{ ms}) \times 90 (^{15}\text{N}, t_3, 35.1 \text{ ms}) \times 60 (^1\text{H}, t_2, 12.0 \text{ ms}) \times 60 (^1\text{H}, t_1,$   
157  $12.0 \text{ ms})$  complex points (SI Table S1). An unweighted, random NUS sampling scheme with a  
158 sparsity of 1.69% (corresponding to 43856  $t_4$  FIDs) was used to record a small subset of the data  
159 points. Using an interscan delay of 1.77 s and 4 scans per FID, the total experimental time was  
160 approximately 110 hours, but three-fold shorter would have sufficed (see Concluding remarks).  
161 The data was processed and reconstructed in the same manner as described above with 50%  
162 extension of all indirect dimensions during the SMILE reconstruction, resulting in an effective  
163 sparsity of 0.5% and a final spectral matrix size of  $492 (^1\text{H}, F_4, 7.8 \text{ Hz/point}) \times 512 (^{15}\text{N}, F_3, 4.7$   
164  $\text{Hz/point}) \times 512 (^1\text{H}, F_2, 13.9 \text{ Hz/point}) \times 512 (^1\text{H}, F_1, 13.9 \text{ Hz/point})$  real points (SI Table S1).  
165 Note that since in the NOESY-NOESY-TROSY experiment the data was recorded using the Echo-  
166 AntiEcho mode (Kay et al., 1992) only in the  $t_3$  dimension, immediately preceding acquisition, the  
167 *bruk\_ranceA.M* macro was not needed after the conversion of the expanded NUS data. The  
168 residual in-phase axial peaks along the  $F_2$  dimension were treated as real peaks and optimally  
169 reconstructed by SMILE to suppress the sampling artifacts of the axial signals from spreading to  
170 the regions with NOE peaks. The processing macros used for both 4D spectra are included with  
171 the raw time domain data (see Data availability).

172

173 2.3 Spectrum analysis

174 Spectra were processed using NMRPipe software (Delaglio et al., 1995); peak picking and  
 175 spectrum analysis was performed using SPARKY software (Goddard and Kneller, 2008; Lee et al.,  
 176 2015) as well as NMRDraw (Delaglio et al., 1995). Programs for visualization and analysis were  
 177 written using freely available python libraries (Hunter, 2007; Harris et al., 2020), as well as NMR-  
 178 specific python libraries (Helmus and Jaroniec, 2013).  
 179



180 **Figure 1.** Pulse schemes for four-dimensional (a) TROSY-NOESY-TROSY and (b) NOESY-  
 181 NOESY-TROSY experiments. The filled and open rectangular bars on the  $^1\text{H}$  and  $^{15}\text{N}$  channels  
 182 represent  $90^\circ$  and  $180^\circ$  pulses, respectively. The open bars in green represent composite  $180^\circ$   
 183 pulses consisting of  $90^\circ_x 207^\circ_y 90^\circ_x$  for  $^1\text{H}$  and  $90^\circ_x 216^\circ_y 90^\circ_x$  for  $^{15}\text{N}$ . The filled shaped  $^1\text{H}$  pulses  
 184 correspond to selective EBURP2 (labeled e) and time-reversed EBURP2 (labeled e\*) pulses (Geen  
 185 and Freeman, 1991), while the open  $^1\text{H}$  shaped pulses represent  $90^\circ$  water-flipback pulses (center  
 186 lobe of a sinc profile, 1.1 ms duration at 800 MHz) (Grzesiek and Bax, 1993). The wide filled  
 187 rectangular boxes denote  $90^\circ$  water-flipback pulses (also 1.1 ms duration at 800 MHz). Unless  
 188 indicated otherwise, all pulses were applied along x. The following delays were used for the initial  
 189 INEPT and TROSY transfers:  $\delta = 2.1$  ms,  $\delta_1 = 2.1$  ms,  $\delta_2 = 2.5$  ms. The  $^1\text{H}$  chemical shift  
 190 evolution during the delay  $\tau = 0.181$  ms was compensated by offsetting the last pair of  $^1\text{H}$  and  $^{15}\text{N}$   
 191  $180^\circ$  pulses by  $\epsilon = \tau/2$  to avoid the linear phase error in the  $t_4$  dimension. (a) For the TROSY-  
 192 NOESY-TROSY: NOE mixing time  $T_m = 200$  ms; phase cycling:  $\phi_1 = y$ ,  $\phi_2 = x$ ,  $x$ ,  $-x$ ,  $-x$ ,  $\phi_3 = y$ ,  
 193  $-y$ ,  $\phi_4 = y$ ,  $\phi_5 = y$ ,  $\phi_6 = y$ ,  $\phi_7 = y$ ,  $\phi_{rec} = y$ ,  $-y$ ,  $-y$ ,  $y$ ; gradients were sine-bell or rectangular shaped  
 194 (as depicted in the figure) with durations  $G_{1,2,3,4,5,6,7,8,9,10,11,12,13,14,15} = 0.977, 1.2, 0.4, 0.4, 0.986,$   
 195  $0.977, 0.081, 1.7, 0.977, 1.2, 0.4, 0.4, 0.986, 0.977,$  and  $0.081$  ms, z-strengths of 21.7, 28.7, -25.9,  
 196 32.9, 2.1, 25.9, 29.4, 30.8, 21.7, 28.7, -31.5, 38.5, 2.1, 25.9, and 35.0 G/cm, and additional x- and  
 197 y-strength of -22.5, 27.5, and 25.0 G/cm for  $G_{11}$ ,  $G_{12}$ , and  $G_{15}$ , respectively. The duration of  
 198 decoding pulses  $G_7$  ( $G_{15}$ ) was empirically optimized for maximum signal and can differ from the

199 theoretical value derived from the gyromagnetic ratios of  $^{15}\text{N}$  and  $^1\text{H}$  and the encoding pulses  
200  $G_3+G_4$  ( $G_{11}+G_{12}$ ) by several microseconds due to rise and fall times of short gradient pulses.  
201 Quadrature detection in  $t_3$  ( $t_1$ ) was achieved using the Echo-AntiEcho scheme (Kay et al., 1992)  
202 by inverting the encoding gradient  $G_{11}$  and  $G_{12}$  ( $G_3$  and  $G_4$ ) together with  $\phi_6$  and  $\phi_7$  ( $\phi_4$  and  $\phi_5$ ) to  
203 obtain the second FID for every  $t_3$  ( $t_1$ ) increment. The  $t_2$  dimension was acquired using States-TPPI  
204 by incrementing  $\phi_2$  by  $90^\circ$ . **(b)** For the NOESY-NOESY-TROSY, the selective EBURP2 and time-  
205 reversed EBURP2 pulses have a duration of 1.0 ms at 800 MHz, centered at 8.3 ppm, thereby  
206 exciting the amide protons downfield from the water resonance without perturbing any upfield  
207 exchangeable protons, or residual aliphatic protons resulting from imperfect perdeuteration. NOE  
208 mixing times,  $T_{m1} = 50$  ms;  $T_{m2} = 300$  ms. Phase cycling:  $\phi_1 = x, x, -x, -x$ ,  $\phi_2 = x-\pi/4$ ,  $\phi_3 = y, -$   
209  $y$ ,  $\phi_4 = y$ ,  $\phi_5 = y$ ,  $\phi_{\text{rec}} = y, -y, -y, y$ . Gradients were sine bell or rectangular shaped with durations  
210  $G_{1,2,3,4,5,6,7,8,9} = 1.7, 1.2, 0.977, 1.2, 0.4, 0.4, 0.986, 0.977, \text{ and } 0.081$  ms, z-strengths of 20.3, 30.8,  
211 21.7, 28.7, -31.5, 38.5, 2.1, 25.9, and 35.0 G/cm, and additional x- and y-strengths of -22.5, 27.5  
212 and 25.0 G/cm for  $G_5, G_6$ , and  $G_9$ , respectively. The duration of  $G_9$  was empirically optimized for  
213 maximum signal. Quadrature detection in  $t_3$  was achieved using the Echo-AntiEcho scheme by  
214 inverting the encoding gradient  $G_5$  and  $G_6$  together with the  $\phi_4$  and  $\phi_5$  to obtain the second FID for  
215 every  $t_3$  increment, while States-TPPI was used to obtain quadrature in the  $t_1$  dimension, by  
216 incrementing the  $\phi_1$  pulse phase by  $90^\circ$ , and for  $t_2$  by incrementing  $\phi_2$  by  $90^\circ$ . Pulse sequence code  
217 and parameter files can be downloaded from <https://zenodo.org/record/4625615>.  
218



219

### 220 3. Results and Discussion

221 Two types of complementary 4D NOE experiments were recorded: (1) 4D TROSY-NOESY-  
222 TROSY and (2) 4D NOESY-NOESY-TROSY (Fig. 1). While the former is very similar to the  
223 HMQC-NOESY-TROSY experiment used recently for a single  $\alpha$ -helical domain with a long  
224 rotational correlation time (Barnes et al., 2019), the 4D NOESY-NOESY-TROSY experiment  
225 extends earlier work by Kaptein and co-workers (Boelens et al., 1989; Breg et al., 1990).

226

#### 227 3.1 Recording and analysis of the 4D TROSY-NOESY-TROSY spectrum

228 The rotational correlation time of **the C145A variant** of M<sup>Pro</sup> (M<sup>Pro</sup><sub>C145A</sub>) at 25 °C is *ca.* 27 ns, and  
229 consequently, transverse relaxation is rapid for both <sup>15</sup>N and <sup>1</sup>H<sup>N</sup> nuclei. For this reason, it proved  
230 beneficial to substitute a TROSY element for the HMQC or HSQC segment that was previously  
231 used for such measurements (Kay et al., 1990; Barnes et al., 2019). Even though the TROSY  
232 element only utilizes half of the amide <sup>1</sup>H<sup>N</sup> magnetization present at the start of the pulse sequence,  
233 combining its <sup>15</sup>N evolution with sensitivity-enhanced gradient selection during the subsequent *t*<sub>2</sub>  
234 evolution period (Fig. 1a) limits the loss to  $\sqrt{2}$ , or even somewhat less when taking the gain from  
235 the <sup>15</sup>N Boltzmann magnetization into account (Pervushin et al., 1998). **A 2D TROSY spectrum**  
236 **(Fig. S1) of this sample allowed identification of 261 backbone amide peaks out of 293 non-proline**  
237 **residues, suggesting the feasibility of implementing the TROSY version of the 4D NOESY**  
238 **experiment. Conformational exchange on a time scale that results in extensive line broadening and**  
239 **incomplete back exchange of amides when the protein was purified in <sup>1</sup>H<sub>2</sub>O are the primary causes**  
240 **for the absence of the *ca.* 30 amide signals.**

241 **The high quality and S/N of the TROSY-HSQC spectrum (Fig. 2b), suggested the feasibility of**  
242 **implementing the TROSY version of the 4D NOESY experiment. Combined with the enhanced**  
243 **relaxation properties during *t*<sub>1</sub> and *t*<sub>2</sub> evolution of the TROSY-selected coherence, we found**  
244 **experimentally that spectral quality attainable for M<sup>Pro</sup><sub>C145A</sub> with the 4D TROSY-NOESY-TROSY**  
245 **was better than with the HMQC-NOESY-TROSY version of the experiment, consistent with the**  
246 **previous report that the TROSY implementation improved both the sensitivity and resolution over**  
247 **the 4D HSQC-NOESY-HSQC (Xia et al., 2000). Figure 2 shows expanded regions of six (F<sub>1</sub>,F<sub>2</sub>)**  
248 **cross-sections through the 4D spectrum, each orthogonal to the (F<sub>3</sub>,F<sub>4</sub>) frequencies of the six amide**

249 correlations that are highlighted in a section of the regular 2D  $^1\text{H}$ - $^{15}\text{N}$  TROSY-HSQC spectrum of  
250 Figure 2b. A total of 231 peaks, out of the 261 peaks in the 2D TROSY spectrum, can be detected  
251 as (semi-)resolvable diagonal peaks in the projected  $^{15}\text{N}$ - $^1\text{H}$  ( $F_3, F_4$ ) plane (data not shown). These  
252 numbers do not include the doubling of resonances associated with isomerization of P184.

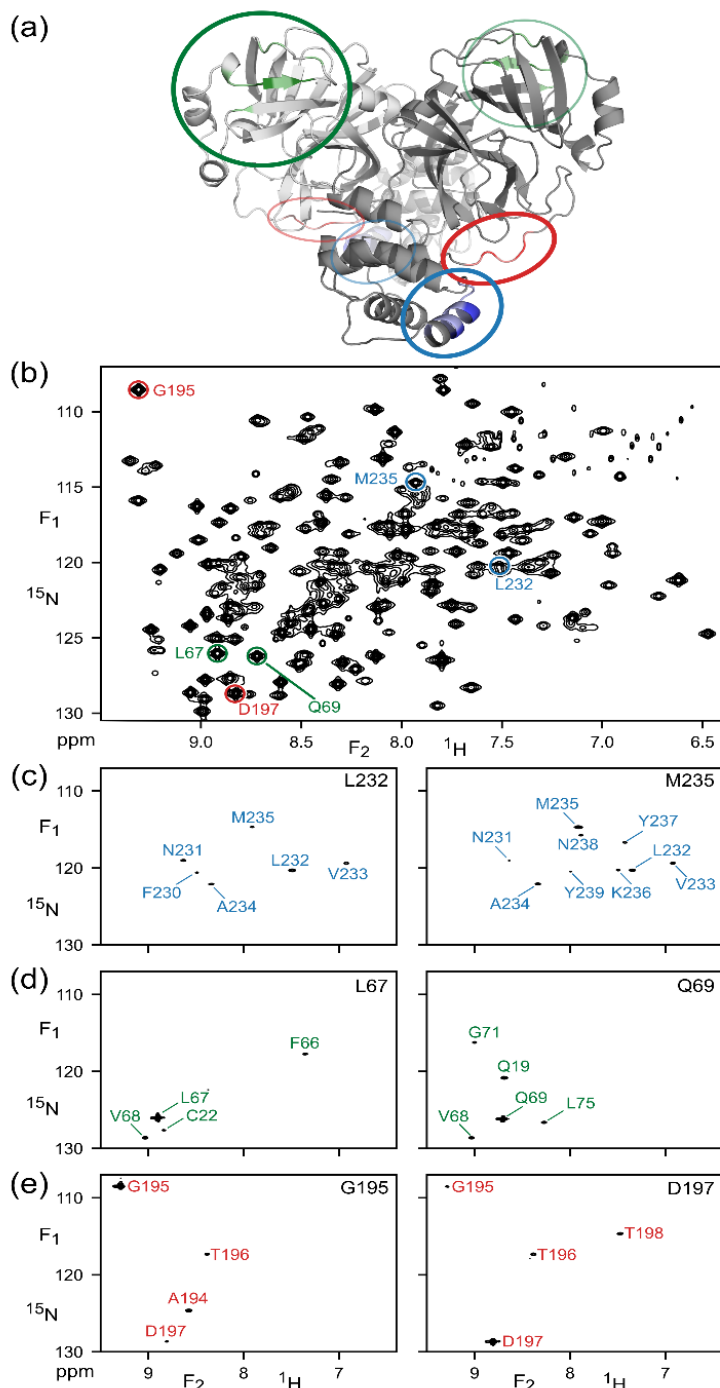
253 The cross sections exemplify the power of 4D analysis for three types of secondary structure:  $\alpha$ -  
254 helix (Fig. 2c),  $\beta$ -sheet (Fig. 2d), and a loop region (Fig. 2e). Due to the long NOE mixing time  
255 used in this experiment (200 ms), substantial spin diffusion occurs which results in numerous NOE  
256 correlations for each amide. For example,  $\alpha$ -helical residues L232 and M235 not only show NOE  
257 interactions with one another, but also share NOE cross peaks to V233 and A234, with M235 even  
258 showing a weak cross peak to N231. Such correlations are particularly useful for validating the  
259 assignments obtained from the limited number of triple resonance backbone assignment  
260 experiments that are applicable to larger proteins such as  $\text{M}^{\text{pro}}$ .

261 The amides of L67 and Q69 in strand  $\beta_4$  only share a single NOE, to sequential residue V68, but  
262 they show valuable long-range NOEs to amide protons in strands  $\beta_1$  (C22) and  $\beta_5$  (L75). G195  
263 and D197, located in the long loop that connects strand  $\beta_{13}$  to helix  $\alpha_6$ , have an NOE to one  
264 another as well as sequential NOEs, but show no long-range interactions, consistent with the X-  
265 ray structure (Douangamath et al., 2020). However, NOEs from L67 or Q69 to T21 or Q19 are not  
266 observed, despite close proximity, due to the minimal back exchange of amide protons in the  $\beta_1$   
267 strand.

268 It is interesting to compare the diagonal peak intensities in these various cross sections of the  
269 TROSY-NOESY-TROSY spectrum. Diagonal intensity is a function of the amount of amide  $^1\text{H}$  z  
270 magnetization present at the start of the pulse sequence, *i.e.*, it depends on the non-selective  
271 longitudinal relaxation time of the amide proton, but also on the attenuation of this magnetization  
272 during the NOE mixing time, in other words, on the selective longitudinal relaxation time which  
273 is dominated by  $J(0)$  spectral density terms. The latter dominate the differences in diagonal  
274 intensity seen in the various cross sections. For example, the helical amides of L232 and M235  
275 rapidly lose their magnetization to their proximate sequential amide neighbors, separated by *ca.*  
276 2.7 Å, that each are in close contact with other neighboring protons. By contrast, none of the L67,  
277 Q69, G195 and D197 amides are closer than 3.7 Å from any neighboring protonated amide in the  
278 1.25 Å X-ray structure of  $\text{M}^{\text{pro}}$  (Douangamath et al., 2020), causing their diagonal intensities to

279 remain high.

280



**Figure 2.** Illustration of amide-amide NOEs in perdeuterated, amide-protonated SARS-CoV-2 Main Protease, observed by 4D TROSY-NOESY-TROSY. (a) Ribbon diagram depicting the backbone homodimeric X-ray structure (PDB: 6LU7), with colors marking the regions that are highlighted in ( $F_1, F_2$ ) cross sections taken at the ( $F_3, F_4$ ) coordinates of (c) L232 and M235 (blue); (d) L67 and Q69 (green) and (e) G195 and D197 (red). These resonances are marked in (b), which represents the most crowded region of the 800-MHz  $^1\text{H}$ - $^{15}\text{N}$  TROSY-HSQC (the full spectrum, is shown in SI Fig. S1).

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307

308

### 309 3.1 Recording and analysis of the 4D NOESY-NOESY-TROSY spectrum

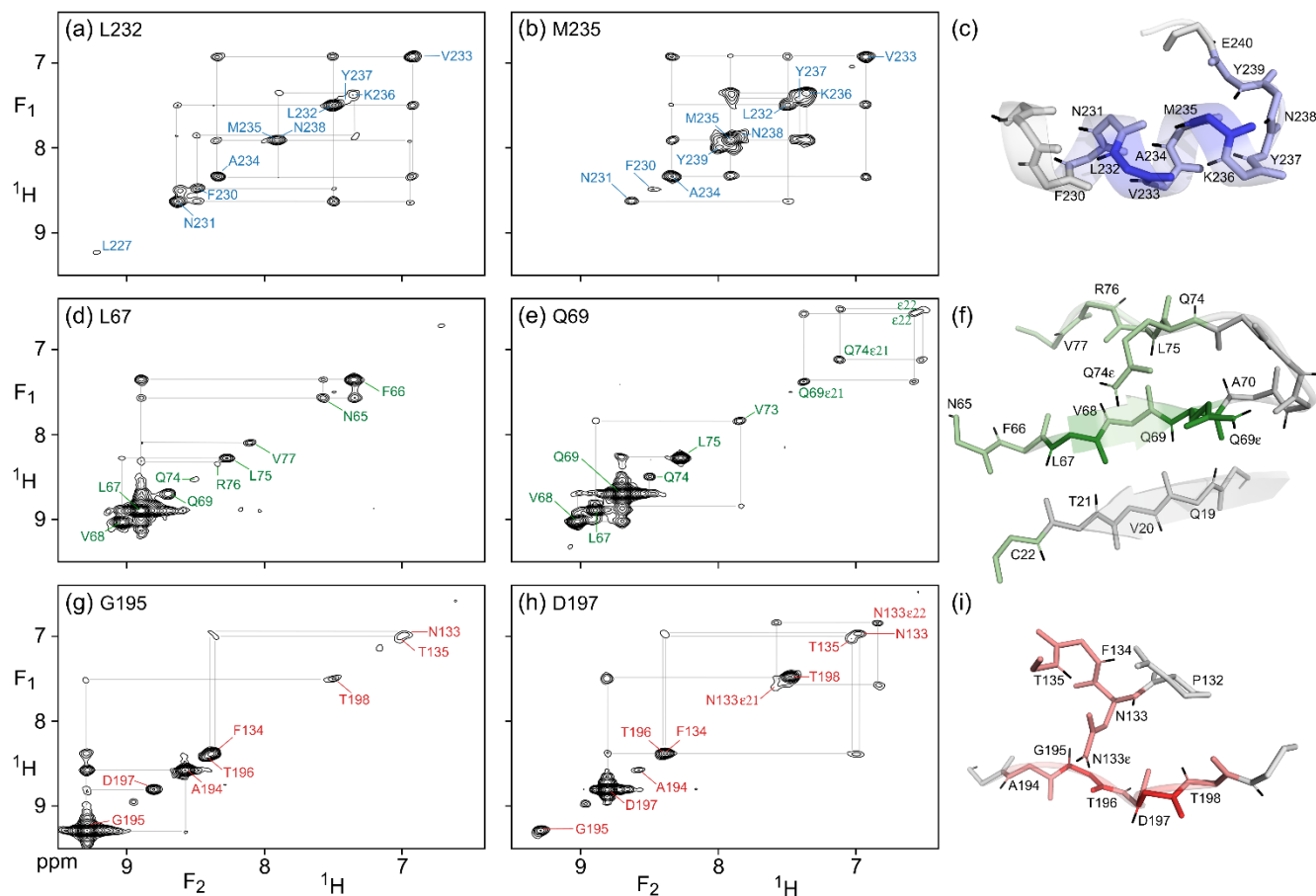
310 As highlighted by the work of Kaptein and co-workers, 3D NOE-NOE experiments provided an  
311 effective method for studying the  $^1\text{H}$ - $^1\text{H}$  cross relaxation network in proteins in more detail. Here,  
312 we extend this powerful experiment to four dimensions, making it more straightforward to analyze  
313 such a spectrum, while limiting the relaxation pathways by perdeuteration of the protein.

314 The pulse scheme of this 4D NOESY-NOESY-TROSY is shown in Figure 1b. It represents a  
315 straightforward extension of the original NOE-NOE 3D experiment (Boelens et al., 1989), but with  
316 the detection period substituted by the gradient-enhanced 2D  $^1\text{H}$ - $^{15}\text{N}$  TROSY scheme (Pervushin  
317 et al., 1998). The latter enhances the attainable spectral resolution in the  $t_3$  and  $t_4$  dimensions, while  
318 dispersing the detected  $^1\text{H}^{\text{N}}$  resonances in the  $^{15}\text{N}$  dimension. A number of minor technical  
319 considerations are also relevant in this respect. (1) First, in order to maximize the number of ( $t_1$ ,  
320  $t_2$ ,  $t_3$ ) data points sampled, the phase cycling of the 4D experiment was reduced to 4 steps, and the  
321 observed spectral window was restricted to the region downfield of the  $\text{H}_2\text{O}$  resonance. To prevent  
322 bleeding in of several weaker imperfectly deuterated aliphatic or exchangeable resonances present  
323 in the upfield spectral region, selective EBURP2 and reverse-EBURP2 pulses (Geen and Freeman,  
324 1991) were used to also restrict the regions where  $^1\text{H}$  resonances were excited to those resonating  
325 downfield from the water resonance. As a result, no NOE peaks from a few amide protons  
326 resonating near water or upfield from water were observed. (2) Recording of a 4D NMR spectrum  
327 at adequate resolution requires the use of non-uniform sampling. High quality NUS reconstruction  
328 of a 4D NMR spectrum can be accomplished by the SMILE program (Ying et al., 2017) but this  
329 as well as most other NUS reconstruction software performs better if the various time domains are  
330 acquired in a manner that results in either a  $0^\circ$  or a  $180^\circ$  linear phase correction across the spectrum.  
331 For this purpose, and to ensure that the non-suppressed axial peaks can be optimally reconstructed,  
332 which requires  $0^\circ$  linear phase correction, it was preferable to insert a non-selective  $90^\circ_x 207^\circ_y 90^\circ_x$   
333 composite  $^1\text{H}$  inversion pulse (highlighted as the green open bar in Fig. 1b), followed by a second  
334 such pulse that reverses any phase imperfections introduced by the first composite pulse (Hwang  
335 et al., 1997). Specifically, the  $\phi_1$  phase cycling serves to eliminate axial peaks in the  $t_1$  dimension  
336 caused by pulse imperfection as well as  $T_1$  relaxation and amide exchange with solvent during  $T_{m1}$ ,  
337 while also suppressing axial peaks in the  $t_2$  dimension resulting from  $T_1$  relaxation and water  
338 exchange during  $T_{m2}$ . To minimize the number of phase cycling steps,  $\phi_2$  was not phase cycled.

339 However, this resulted in small residual axial peaks along the  $F_2$  dimension caused by pulse  
340 imperfections. To ensure that these residual axial peaks were absorptive in the final spectrum,  
341 thereby simplifying SMILE NUS reconstruction, an echo is generated by the application of two  
342 composite  $^1\text{H}$   $180^\circ$  pulses in order to suppress initial chemical shift evolution at  $t_2=0$ , thereby  
343 eliminating the need for a linear phase correction. Considering that the real and imaginary  
344 components of the residual axial signals have the same amplitude, they result in a  $45^\circ$  phase error  
345 for the axial peaks in the  $F_2$  dimension. Shifting the  $\phi_2$  phase by  $-45^\circ$  ensures that the NOE and  
346 axial peaks both can be phased absorptive using the same phase correction, thus facilitating NUS  
347 processing.

348 Compared to the 4D TROSY-NOESY-TROSY pulse scheme, the 4D NOESY-NOESY-TROSY  
349 experiment avoids the lossy magnetization transfer step from  $^1\text{H}$  to  $^{15}\text{N}$  and back (leading to a  
350 slightly larger number of 241 diagonal peaks on the  $^{15}\text{N}$ - $^1\text{H}$  ( $F_3, F_4$ ) projected plane, compared to  
351 231 for TROSY-NOESY-TROSY). Instead, its magnetization is simply transferred, in part, to its  
352 nearest neighbors by cross relaxation during the first NOE mixing period of duration  $T_{m1} = 50$  ms.  
353 There is virtually no loss in total spin polarization summed over the initial “starting spin”, whose  
354  $t_1$  evolution is monitored, and those of its immediate neighbors that are within cross-relaxation  
355 contact. As a result, the intrinsic sensitivity of such NOESY-NOESY-TROSY measurements is  
356 quite high, allowing the choice of a long duration of 300 ms for the second NOE mixing time,  $T_{m2}$ .  
357 During this second, much longer mixing time, the  $z$ -magnetization distributes over considerable  
358 distances due to indirect transfers (Fig. 3). Even in this extensively perdeuterated protein, NOEs  
359 to nearly a dozen neighboring protons are observed on the diagonals of the ( $F_1, F_2$ ) cross sections,  
360 taken at the same ( $^{15}\text{N}$ ,  $^1\text{H}$ ) frequencies used for illustrating the utility of the 4D TROSY-NOESY-  
361 TROSY spectrum of Figure 2. However, as pointed out by Boelens *et al.* and Breg *et al.* (Boelens  
362 *et al.*, 1989; Breg *et al.*, 1990), the NOE-NOE combination offers a wealth of new information on  
363 the cross-relaxation pathways that led to the long-distance NOEs, substantially aiding both the  
364 assignment and analysis of distance information. Below, we briefly highlight a few examples.

365 As expected,  $\alpha$ -helical residue L232 shows intense cross peaks to both of its sequential neighbors,  
366 N231 and V233, as well as a weaker cross peak to F230. Despite the relatively short mixing time  
367 of only 50 ms that separates  $t_1$  and  $t_2$  evolution, the latter must result mostly from indirect



368

369 **Figure 3.** ( $F_1, F_2$ ) cross sections through the 4D NOESY-NOESY-TROSY spectrum of  $M^{\text{pro}}_{C145A}$ ,  
 370 taken orthogonal to the ( $F_3, F_4$ ) TROSY-HSQC plane at the  $^{15}\text{N}, ^1\text{H}$  frequencies of (a) L232, (b)  
 371 M235, (d) L67, (e) Q69), (g) G195, and (h) D197. These cross sections show diagonal resonances  
 372 for amide protons that are within long-range contact of the selected amide, either through direct or  
 373 indirect NOE transfer during the two mixing periods that have a total duration of 50+300 ms. Off-  
 374 diagonal resonances in these cross sections correspond to NOE magnetization transfer during the  
 375 50-ms mixing period that separates the  $t_1$  and  $t_2$  evolution periods. Colors match those of the  
 376 corresponding residues in Figure 2. Expanded views of the structural elements (PDB: 6LU7) that  
 377 gave rise to the observed NOEs are shown in panels (c), (f), and (i).  
 378

379 transfer through N231, because N231 and F230 share an intense cross peak. So in effect, each  
 380 cross section through the 4D spectrum shown in Figure 3 corresponds to a 2D NOESY spectrum  
 381 of a small, localized, region within the protein structure - making its analysis far simpler. For  
 382 residues with few neighbors, direct NOE contacts between neighbors separated by as much as 4.5  
 383 Å give rise to quite intense cross peaks after 50 ms NOE mixing, as exemplified by the contacts  
 384 between G195 and its A194 and T196 neighbors (Fig. 3g). A weaker cross peak between G195 and  
 385 D197, at an interproton distance of 6.4 Å, appears not to be mediated by spin diffusion because

386 the G195 and D197 panels (Fig. 3g) show no common strong NOE to any visible resonance.  
387 However, the possibility that the hydroxyl proton of T196 serves as a relay partner cannot be  
388 excluded.

389 The NOESY-NOESY-TROSY spectrum also shows multiple NOEs to sidechain amide protons  
390 that are not visible in the TROSY-NOESY-TROSY spectrum because the TROSY element does  
391 not select magnetization transfer for NH<sub>2</sub> groups. For example, D197 shows long-range NOEs to  
392 the N133 carboxamide protons, whereas Q69 shows NOEs to both its own carboxamide protons  
393 and to those of Q74. The non-equivalent NH<sub>2</sub> pairs are readily recognized by cross-peak to  
394 diagonal peak intensity ratios that are close to one, owing to their short interproton distance.

395

#### 396 **4. Concluding remarks**

397 The spectra shown in this study were recorded during the summer of 2020, when access to campus  
398 facilities was strongly restricted due to COVID-19 pandemic mitigation efforts. These restrictions  
399 allowed for much lengthier acquisition of spectra than commonly used, for a total of eight days for  
400 the two 4D spectra. As a benefit of NUS reconstruction, it is possible to generate spectra of the  
401 same resolution recorded in any fraction of that time. Alternatively, we can discard the data  
402 recorded at the longest values of  $t_1$ ,  $t_2$ , and  $t_3$ . Indeed, processing the same time domain data sets  
403 but shortening the time domains using a previously described protocol that considers the total  
404 normalized length of the 3D ( $t_1, t_2, t_3$ ) time domain vector (Ying et al., 2019), using only one third  
405 of the acquired time domain data yields spectra that are very similar to the ones shown in Figures  
406 2 and 3, albeit at slightly lower resolution and signal-to-noise, due to the use of three-fold less time  
407 domain data. Nevertheless, the quality of the resulting spectra remains excellent, with near-  
408 identical information content (Supporting Information Figures S2 and S3).

409 Use of the lengthy data acquisition times needed to collect the 4D spectra requires a high stability  
410 sample, which in our case benefited from the C145A active site mutation, protecting the sample  
411 from auto-proteolysis. As with all NMR experiments, S/N is approximately proportional to sample  
412 concentration. Therefore, working at high concentrations benefits S/N of these experiments that  
413 involve multiple magnetization transfer steps, an issue that is particularly important for NOE  
414 experiments where magnetization from a single nucleus is distributed over many neighbors.

415 We note that the TROSY-NOESY-TROSY experiment used a long NOE mixing time of 200 ms,



416 such as to increase the number of observed connectivities by adding indirect NOE effects,  
417 including spin diffusion through hydroxyl protons (Koharudin et al., 2003), thereby aiding the  
418 assignment process. The use of a 50-ms NOE mixing period in the subsequent 4D NOESY-  
419 NOESY-TROSY experiment then provided a semi-quantitative measure of distance between these  
420 protons and their neighbors. Indeed, as pointed out by Kaptein and co-workers, recording of NOE-  
421 NOE spectra provides important experimental data on the pathway of magnetization transfer  
422 during NOE mixing. Such information could be used to convert this data into more quantitative  
423 distance information than the typical qualitative analysis of NOE intensities, potentially leading to  
424 the generation of higher resolution structures (Vogeli et al., 2009; Vogeli et al., 2012). Quantitative  
425 NOE interpretation traditionally relied on the recording of a series of NOE buildup data, which  
426 can become comparably time-consuming as the recording of 4D NMR spectra if resonance overlap  
427 is a limiting factor, as typically is the case for NOE spectra. This problem is further exacerbated  
428 by the spectral crowding of large proteins, particularly in the  $^1\text{H}$  dimension, and while 3D spectra  
429 may give higher signal to noise ratios than 4D spectra, downstream analysis frequently requires  
430 extensive disambiguation of overlapped peaks. Our study of  $\text{M}^{\text{pro}}_{\text{C145A}}$  shows that a large number  
431 of semi-quantitative NOE distances become accessible by recording of 4D NMR spectra on a  
432 perdeuterated larger protein with little or no ambiguity about the nuclei involved.

433 While the high signal to noise and spectral simplicity of working with perdeuterated proteins has  
434 long been recognized (Torchia et al., 1988; Lemaster and Richards, 1988; Grzesiek et al.,  
435 1993; Tugarinov et al., 2004) the number of structural restraints accessible used to be small. Our  
436 present study demonstrates that a much larger number of NOE interactions becomes available by  
437 the recording of 4D NOE spectra. Moreover, it highlights the exquisite detail and value of NOE-  
438 NOE interaction analysis explored by the Kaptein group and it demonstrates that this approach is  
439 highly suitable for the larger biomolecules and biomolecular complexes being explored today, in  
440 particular when using extensive perdeuteration. Therefore, we believe that the recording of high  
441 quality 4D NMR spectra of the type presented in this study is entirely practical and invaluable for  
442 the structural and functional analysis of large proteins and their complexes, with possible extension  
443 to the study of nucleic acids. We note, however, that in the absence of extensive deuteration the  
444 dilution of nuclear magnetization over sidechain resonances will strongly lower the sensitivity of  
445 the experiment, which is further exacerbated by decreased effectiveness of TROSY-based line  
446 narrowing in such samples. On the other hand, adaptations of the NOESY-NOESY-TROSY



447 experiment to methyl-protonated but otherwise perdeuterated proteins (Tugarinov et al., 2005b)  
448 are expected to be readily feasible.

449

## 450 **5. Data availability**

451 The raw Bruker NMR data sets including the acquisition parameters and NUS sampling lists,  
452 pulse programs, include file, and NMRPipe processing scripts are available for download from  
453 zenodo.org: <https://zenodo.org/record/4625615>  
454

455

## 456 **6. Special issue statement**

457  
458 This article is part of the special issue “Robert Kaptein Festschrift”. It is not associated with a  
459 conference.  
460

## 461 **7. Supplement**

462 Supporting information related to this article is available online at: <https://doi.org/xxxxxxxxxxx>.  
463

## 464 **8. Author contributions**

465 AJR expressed and purified protein samples, collected and analyzed the data, and edited the  
466 manuscript; JY optimized pulse sequence parameterization and processing and edited the  
467 manuscript; AB supervised the project and wrote the manuscript.  
468

## 469 **9. Competing interest**

470 The authors declare that they have no conflict of interest.

## 471 **10. Acknowledgements**

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477 **11. References**

- 478 Altincekic, N.: Large-scale recombinant production of the SARS-CoV-2 proteome for high-  
479 throughput and structural biology applications, *Frontiers in Molecular Biosciences*, doi:  
480 10.3389/fmolb.2021.653148 2021, 2021.
- 481 Barnes, C. A., Shen, Y., Ying, J. F., Takagi, Y., Torchia, D. A., Sellers, J. R., and Bax, A.:  
482 Remarkable Rigidity of the Single alpha-Helical Domain of Myosin-VI As Revealed by NMR  
483 Spectroscopy, *J. Am. Chem. Soc.*, 141, 9004-9017, 10.1021/jacs.9b03116, 2019.
- 484 Boelens, R., Koning, T. M. G., and Kaptein, R.: Determination of Biomolecular Structures From  
485 Proton-Proton Noes Using a Relaxation Matrix Approach, *J. Mol. Struct.*, 173, 299-311, 1988.
- 486 Boelens, R., Vuister, G. W., Koning, T. M. G., and Kaptein, R.: Observation of spin diffusion in  
487 biomolecules by 3-dimensional NOE-NOE spectroscopy, *J. Am. Chem. Soc.*, 111, 8525-8526,  
488 10.1021/ja00204a039, 1989.
- 489 Boras, B., Jones, R. M., Anson, B. J., Arenson, D., Aschenbrenner, L., Bakowski, M. A.,  
490 Beutler, N., Binder, J., Chen, E., Eng, H., Hammond, H., Hammond, J., Haupt, R. E., Hoffman,  
491 R., Kadar, E. P., Kania, R., Kimoto, E., Kirkpatrick, M. G., Lanyon, L., Lendy, E. K., Lillis, J.  
492 R., Logue, J., Luthra, S. A., Ma, C., Mason, S. W., McGrath, M. E., Noell, S., Obach, R. S.,  
493 O'Brien, M. N., O'Connor, R., Ogilvie, K., Owen, D., Pettersson, M., Reese, M. R., Rogers, T.  
494 F., Rossulek, M. I., Sathish, J. G., Shirai, N., Steppan, C., Ticehurst, M., Updyke, L. W., Weston,  
495 S., Zhu, Y., Wang, J., Chatterjee, A. K., Mesecar, A. D., Frieman, M. B., Anderson, A. S., and  
496 Allerton, C.: Discovery of a Novel Inhibitor of Coronavirus 3CL Protease for the Potential  
497 Treatment of COVID-19, *bioRxiv*, 2020.2009.2012.293498, 10.1101/2020.09.12.293498, 2021.
- 498 Breg, J. N., Boelens, R., Vuister, G. W., and Kaptein, R.: 3D NOE-NOE spectroscopy of  
499 proteins - Observation of sequential 3D NOE cross peaks in Arc repressor, *J. Magn. Reson.*, 87,  
500 646-651, 10.1016/0022-2364(90)90324-3, 1990.
- 501 Clore, G. M., Kay, L. E., Bax, A., and Gronenborn, A. M.: Four-dimensional <sup>13</sup>C/<sup>13</sup>C-edited  
502 nuclear Overhauser enhancement spectroscopy of a protein in solution: Application to  
503 interleukin 1 $\beta$ , *Biochemistry*, 30, 12-18, 1991.
- 504 Delaglio, F., Grzesiek, S., Vuister, G. W., Zhu, G., Pfeifer, J., and Bax, A.: NMRpipe - a  
505 multidimensional spectral processing system based on Unix pipes, *J. Biomol. NMR*, 6, 277-293,  
506 1995.

507 Diercks, T., Truffault, V., Coles, M., and Millett, O.: Diagonal-Free 3D/4D HN,HN-TROSY-  
508 NOESY-TROSY, *J. Am. Chem. Soc.*, 132, 2138-+, 10.1021/ja910523q, 2010.

509 Douangamath, A., Fearon, D., Gehrtz, P., Krojer, T., Lukacik, P., Owen, C. D., Resnick, E.,  
510 Strain-Damerell, C., Aimon, A., Abranyi-Balogh, P., Brandao-Neto, J., Carbery, A., Davison, G.,  
511 Dias, A., Downes, T. D., Dunnett, L., Fairhead, M., Firth, J. D., Jones, S. P., Keeley, A., Keseru,  
512 G. M., Klein, H. F., Martin, M. P., Noble, M. E. M., O'Brien, P., Powell, A., Reddi, R. N.,  
513 Skyner, R., Snee, M., Waring, M. J., Wild, C., London, N., von Delft, F., and Walsh, M. A.:  
514 Crystallographic and electrophilic fragment screening of the SARS-CoV-2 main protease, *Nature*  
515 *Communications*, 11, 10.1038/s41467-020-18709-w, 2020.

516 Geen, H., and Freeman, R.: Band-selective radiofrequency pulses, *J. Magn. Reson.*, 93, 93-141,  
517 1991.

518 Grzesiek, S., Anglister, J., Ren, H., and Bax, A.:  $^{13}\text{C}$  line narrowing by  $^2\text{H}$  decoupling in  
519  $^2\text{H}/^{13}\text{C}/^{15}\text{N}$ -enriched Proteins. Application to triple resonance 4D connectivity of sequential  
520 amides., *Journal of American Chemical Society*, 115, 4369-4370, 1993.

521 Grzesiek, S., and Bax, A.: The Importance of Not Saturating  $\text{H}_2\text{O}$  in Protein NMR. Application  
522 to Sensitivity Enhancement and NOE Measurement, *J. Am. Chem. Soc.*, 115, 12593-12594,  
523 1993.

524 Grzesiek, S., Wingfield, P., Stahl, S., Kaufman, J. D., and Bax, A.: Four-dimensional  $^{15}\text{N}$ -  
525 separated NOESY of slowly tumbling perdeuterated  $^{15}\text{N}$ -enriched proteins. Applications to  
526 HIV-1 Nef., *J. Am. Chem. Soc.*, 117, 9594-9595, 1995.

527 Harris, C. R., Millman, K. J., van der Walt, S. J., Gommers, R., Virtanen, P., Cournapeau, D.,  
528 Wieser, E., Taylor, J., Berg, S., Smith, N. J., Kern, R., Picus, M., Hoyer, S., van Kerkwijk, M.  
529 H., Brett, M., Haldane, A., del Rio, J. F., Wiebe, M., Peterson, P., Gerard-Marchant, P.,  
530 Sheppard, K., Reddy, T., Weckesser, W., Abbasi, H., Gohlke, C., and Oliphant, T. E.: Array  
531 programming with NumPy, *Nature*, 585, 357-362, 10.1038/s41586-020-2649-2, 2020.

532 Helmus, J. J., and Jaroniec, C. P.: Nmrplug: an open source Python package for the analysis of  
533 multidimensional NMR data, *J. Biomol. NMR*, 55, 355-367, 10.1007/s10858-013-9718-x, 2013.

534 Hunter, J. D.: Matplotlib: A 2D graphics environment, *Computing in Science & Engineering*, 9,  
535 90-95, 10.1109/mcse.2007.55, 2007.

536 Hwang, T. L., van Zijl, P. C. M., and Garwood, M.: Broadband adiabatic refocusing without  
537 phase distortion, *J. Magn. Reson.*, 124, 250-254, 1997.

538 Ikura, M., Kay, L. E., and Bax, A.: A novel approach for sequential assignment of  $^1\text{H}$ ,  $^{13}\text{C}$ , and  
539  $^{15}\text{N}$  spectra of larger proteins: heteronuclear triple-resonance three-dimensional NMR  
540 spectroscopy. application to calmodulin, *Biochemistry*, 29, 4659-4667, 1990.

541 Kay, L. E., Clore, G. M., Bax, A., and Gronenborn, A. M.: Four-dimensional heteronuclear  
542 triple-resonance NMR spectroscopy of interleukin-1B in solution, *Science*, 249, 411-414, 1990.

543 Kay, L. E., Keifer, P., and Saarinen, T.: Pure Absorption Gradient Enhanced Heteronuclear  
544 Single Quantum Correlation Spectroscopy with Improved Sensitivity, *J. Am. Chem. Soc.*, 114,  
545 10663-10665, 1992.

546 Koharudin, L. M. I., Bonvin, A., Kaptein, R., and Boelens, R.: Use of very long-distance NOEs  
547 in a fully deuterated protein: an approach for rapid protein fold determination, *J. Magn. Reson.*,  
548 163, 228-235, 10.1016/s1090-7807(03)00149-6, 2003.

549 Lee, W., Tonelli, M., and Markley, J. L.: NMRFAM-SPARKY: enhanced software for  
550 biomolecular NMR spectroscopy., *Bioinformatics (Oxford, England)*, 31, 1325-1327,  
551 10.1093/bioinformatics/btu830, 2015.

552 Lemaster, D. M., and Richards, F. M.: NMR sequential assignment of Escherichia-coli  
553 thioredoxin utilizing random fractional deuteration *Biochemistry*, 27, 142-150,  
554 10.1021/bi00401a022, 1988.

555 Marion, D., Driscoll, P. C., Kay, L. E., Wingfield, P. T., Bax, A., Gronenborn, A. M., and Clore,  
556 G. M.: Overcoming the overlap problem in the assignment of  $^1\text{H}$  NMR spectra of larger proteins  
557 by use of three-dimensional heteronuclear  $^1\text{H}$ - $^{15}\text{N}$  Hartmann-Hahn-multiple quantum coherence  
558 and nuclear Overhauser-multiple quantum coherence spectroscopy: application to interleukin  
559  $1\beta$ , *Biochemistry*, 28, 6150-6156, 1989a.

560 Marion, D., Kay, L. E., Sparks, S. W., Torchia, D. A., and Bax, A.: Three-dimensional  
561 heteronuclear NMR of  $^{15}\text{N}$ -labeled proteins, *J. Am. Chem. Soc.*, 111, 1515-1517, 1989b.

562 Oschkinat, H., Griesinger, C., Kraulis, P. J., Sorensen, O. W., Ernst, R. R., Gronenborn, A. M.,  
563 and Clore, G. M.: 3-Dimensional NMR spectroscopy of a protein in solution, *Nature*, 332, 374-  
564 376, 1988.

565 Pervushin, K., Riek, R., Wider, G., and Wuthrich, K.: Attenuated T2 relaxation by mutual  
566 cancellation of dipole- dipole coupling and chemical shift anisotropy indicates an avenue to  
567 NMR structures of very large biological macromolecules in solution, *Proc. Natl. Acad. Sci.*  
568 USA, 94, 12366-12371, 1997.

569 Pervushin, K. V., Wider, G., and Wuthrich, K.: Single transition-to-single transition polarization  
570 transfer (ST2-PT) in  $[N^{15}, H^1]$ -TROSY, *J. Biomol. NMR*, 12, 345-348, 1998.

571 Rovnyak, D., Frueh, D. P., Sastry, M., Sun, Z. Y. J., Stern, A. S., Hoch, J. C., and Wagner, G.:  
572 Accelerated acquisition of high resolution triple-resonance spectra using non-uniform sampling  
573 and maximum entropy reconstruction, *J. Magn. Reson.*, 170, 15-21, 10.1016/j.jmr.2004.05.016,  
574 2004.

575 Torchia, D. A., Sparks, S. W., and Bax, A.: Delineation of Alpha-Helical Domains in  
576 Deuteriated Staphylococcal Nuclease By 2d Noe Nmr-Spectroscopy, *J. Am. Chem. Soc.*, 110,  
577 2320-2321, 1988.

578 Tugarinov, V., Muhandiram, R., Ayed, A., and Kay, L. E.: Four-dimensional NMR spectroscopy  
579 of a 723-residue protein: Chemical shift assignments and secondary structure of malate synthase  
580 G, *J. Am. Chem. Soc.*, 124, 10025-10035, 2002.

581 Tugarinov, V., Hwang, P. M., and Kay, L. E.: Nuclear magnetic resonance spectroscopy of high-  
582 molecular-weight proteins, *Annu. Rev. Biochem.*, 73, 107-146, 2004.

583 Tugarinov, V., Choy, W. Y., Orekhov, V. Y., and Kay, L. E.: Solution NMR-derived global fold  
584 of a monomeric 82-kDa enzyme, *Proc. Natl. Acad. Sci. U. S. A.*, 102, 622-627, 2005a.

585 Tugarinov, V., Kay, L. E., Ibraghimov, I., and Orekhov, V. Y.: High-resolution four-dimensional  
586 H-1-C-13 NOE spectroscopy using methyl-TROSY, sparse data acquisition, and  
587 multidimensional decomposition, *J. Am. Chem. Soc.*, 127, 2767-2775, 10.1021/ja04032o, 2005b.

588 Vogeli, B., Segawa, T. F., Leitz, D., Sobol, A., Choutko, A., Trzesniak, D., van Gunsteren, W.,  
589 and Riek, R.: Exact Distances and Internal Dynamics of Perdeuterated Ubiquitin from NOE  
590 Buildups, *J. Am. Chem. Soc.*, 131, 17215-17225, 10.1021/ja905366h, 2009.

591 Vogeli, B., Kazemi, S., Guntert, P., and Riek, R.: Spatial elucidation of motion in proteins by  
592 ensemble-based structure calculation using exact NOEs, *Nat. Struct. Mol. Biol.*, 19, 1053-1058,  
593 10.1038/nsmb.2355, 2012.

594 Vuister, G. W., Boelens, R., and Kaptein, R.: Non-selective 3-dimensional NMR spectroscopy -  
595 The 3D NOE-HOHAHA experiment, *J. Magn. Reson.*, 80, 176-185, 1988.

596 Wagner, G.: Prospects for NMR of large proteins, *J. Biomol. NMR*, 3, 375-385, 1993.

597 Wüthrich, K.: *NMR of Proteins and Nucleic Acids*, John Wiley & Sons, New York, 1986.

598 Xia, Y. L., Sze, K. H., and Zhu, G.: Transverse relaxation optimized 3D and 4D N-15/N-15  
599 separated NOESY experiments of N-15 labeled proteins, *J. Biomol. NMR*, 18, 261-268,  
600 10.1023/a:1026590201757, 2000.

601 Ying, J., Delaglio, F., Torchia, D. A., and Bax, A.: Sparse multidimensional iterative lineshape-  
602 enhanced (SMILE) reconstruction of both non-uniformly sampled and conventional NMR data,  
603 *J. Biomol. NMR*, 68, 101-118, 2017.

604 Ying, J. F., Barnes, C. A., Louis, J. M., and Bax, A.: Importance of time-ordered non-uniform  
605 sampling of multidimensional NMR spectra of A beta(1-42) peptide under aggregating  
606 conditions, *J. Biomol. NMR*, 73, 429-441, 10.1007/s10858-019-00235-7, 2019.

607 Zuiderweg, E. R. P., and Fesik, S. W.: Heteronuclear Three-Dimensional NMR Spectroscopy of  
608 the Inflammatory Protein C5<sub>a</sub>, *Biochemistry*, 28, 2387-2391, 1989.

609 Zuiderweg, E. R. P., Petros, A. M., Fesik, S. W., and Olejniczak, E. T.: 4-Dimensional [C-13, H-  
610 1, C-13, H-1] Hmqc-Noe-Hmqc Nmr-Spectroscopy - Resolving Tertiary Noe Distance  
611 Constraints in the Spectra of Larger Proteins, *J. Am. Chem. Soc.*, 113, 370-372,  
612 10.1021/ja00001a060, 1991.

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