



1 **Four-dimensional NOE-NOE spectroscopy of SARS-CoV-2 Main Protease to facilitate**  
2 **resonance assignment and structural analysis**

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22 This study is dedicated to Robert Kaptein on the occasion of his 80<sup>th</sup> birthday

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24 **ABSTRACT.** Resonance assignment and structural studies of larger proteins by NMR can be  
25 challenging when exchange broadening, multiple stable conformations, and back-exchanging the  
26 fully deuterated chain pose problems. These difficulties arise for the SARS-CoV-2 Main Protease,  
27 a homodimer of 2×306 residues. We demonstrate that the combination of four-dimensional (4D)  
28 TROSY-NOESY-TROSY spectroscopy and 4D NOESY-NOESY-TROSY spectroscopy provides  
29 an effective tool for delineating the  $^1\text{H}$ - $^1\text{H}$  dipolar relaxation network. In combination with  
30 detailed structural information obtained from prior X-ray crystallography work, such data are  
31 particularly useful for extending and validating resonance assignments, as well as for probing  
32 structural features.

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### 33 **1 Introduction**

34 The extension of conventional two-dimensional  $^1\text{H}$ - $^1\text{H}$  NMR spectroscopy of natural proteins  
35 (Wüthrich, 1986) to three-dimensional (3D) homonuclear NMR experiments offered the  
36 ability to both simplify spectral analysis by removing resonance overlap (Vuister et al.,  
37 1988;Oschkinat et al., 1988) and by providing access to a direct, more detailed analysis of  $^1\text{H}$ -  
38  $^1\text{H}$  dipolar cross relaxation networks. In particular, the homonuclear 3D NOE-NOE  
39 experiment (Boelens et al., 1989;Breg et al., 1990) not only decreased resonance overlap, it  
40 directly elucidated spin-diffusion pathways. This information complemented and validated  
41 the elegant relaxation matrix analysis of spin diffusion (Boelens et al., 1988).

42 Such homonuclear  $^1\text{H}$  3D experiments and analysis strategies were soon followed by a  
43 myriad of heteronuclear 3D experiments that required isotopic enrichment, and therefore  
44 cloning and bacterial overexpression (Marion et al., 1989b;Zuiderweg and Fesik, 1989;Ikura  
45 et al., 1990;Marion et al., 1989a;Wagner, 1993). Most of these heteronuclear experiments  
46 simply served to disperse the regular  $^1\text{H}$ - $^1\text{H}$  2D spectrum into a third dimension, thereby  
47 removing spectral overlap but providing little or no new information on the all-important  
48  $^1\text{H}$ - $^1\text{H}$  spin diffusion pathways. The 3D NOESY-HMQC experiment (Marion et al.,  
49 1989b;Zuiderweg and Fesik, 1989) subsequently was extended to four dimensions (4D),  
50 thereby dispersing the conventional 2D  $^1\text{H}$ - $^1\text{H}$  NOESY experiment into two additional  
51 dimensions that correspond to the chemical shifts of the nuclei to which each of the protons  
52 is covalently bound (Kay et al., 1990;Clore et al., 1991;Zuiderweg et al., 1991).



53 These multi-dimensional experiments provided a tremendous degree of spectral  
54 simplification, in particular once appropriate analysis software became available. However,  
55 it also quickly became clear that extension to large, slowly tumbling proteins was hampered  
56 by low signal-to-noise, caused by the relative inefficiency of the magnetization transfer steps  
57 when the dimensionality of a spectrum is increased. This decrease in sensitivity was  
58 remedied by generating the protein in a highly perdeuterated state, while keeping the  
59 solvent-exchangeable backbone amide protons protonated (Torchia et al., 1988; Lemaster  
60 and Richards, 1988). Combining the perdeuteration approach with the triple resonance  
61 assignment strategy (Grzesiek et al., 1993) and the subsequently introduced powerful TROSY  
62 line-narrowing method (Pervushin et al., 1997) made it possible to assign and analyze the  
63 structure of quite large proteins, as exemplified by the 723-residue protein malate synthase  
64 G (Tugarinov et al., 2002; Tugarinov et al., 2005). The sensitivity gained by perdeuteration,  
65 enabling the recording of 4D  $^{15}\text{N}$ -separated NOE spectra, was key in solving the structure of  
66 a HIV-1 accessory protein that had been too challenging for analysis by more conventional  
67 methods (Grzesiek et al., 1995).

68 In the present report, we merge the above mentioned prior advances, 3D NOE-NOE and 3D  
69  $^{15}\text{N}$ -separated NOESY into a 4D experiment in combination with perdeuteration to study  
70  $\text{M}^{\text{pro}}$ , the main protease of SARS-CoV-2 which is the virus responsible for coronavirus-2019  
71 disease (COVID-19).  $\text{M}^{\text{pro}}$ , also known as  $3\text{CL}^{\text{pro}}$  or Nsp5, is a homodimeric cysteine protease  
72 of  $2 \times 306$  residues that does not have closely related mammalian homologues and is  
73 therefore an intense target for drug development. Its NMR analysis is challenging, not only  
74 for its large size (67.6 kD), but also because of the presence of a minor conformer associated  
75 with the cis-isomer of one of its 13 Pro residues (P184), the difficulty in back-exchanging all  
76 backbone amide protons when the protein is expressed in  $\text{D}_2\text{O}$ , and the presence of  
77 intermediate time scale motions that lead to exchange broadening in the vicinity of the  
78 protein's active site. Here we focus on a mutant where the catalytic Cys residue has been  
79 mutated to Ala (C145A), a construct that is stable for multiple weeks at the high  
80 concentrations required for NMR spectroscopy. The assignment process and a full structural  
81 analysis of the protein will be presented elsewhere. The focus of the present work is on  
82 technical innovations, including recording two types of 4D NOE-based NMR spectra, that



83 proved invaluable both for the validation of the resonance assignments, as well as the  
84 subsequent structural analysis.

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## 86 **2. Methods and Experiments**

### 87 **2.1 Protein production**

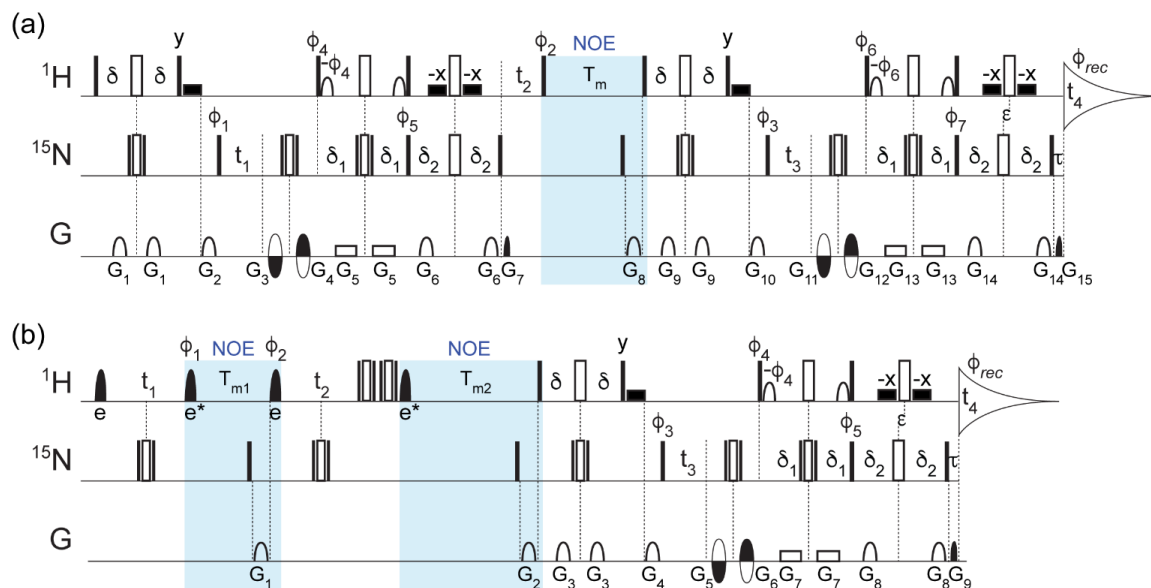
88 The gene encoding a C145A variant of M<sup>PRO</sup> (M<sup>PRO</sup><sub>C145A</sub>) with an N-terminal affinity (and  
89 solubility), tag was synthesized by GenScript (USA) and then cloned into a Pet24a+ plasmid  
90 between BamHI and XhoI restriction sites. The fusion protein encoded for 6His tag –GB1–SG  
91 rich linker–TEV cleavage site – M<sup>PRO</sup>, and was purified according to methods collectively  
92 developed by the COVID-19 NMR consortium (Altincekic, 2021). In brief, the cell lysate was  
93 passed down a 6His-affinity column (IMAC) and eluted in a small volume; the solubility tag was  
94 cleaved off to generate a native N-terminus; the reaction mix was then passed through an IMAC  
95 column to remove uncleaved protein, before size separation on a Sephadex G75 column.

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### 97 **2.2 Recording of NMR data**

98 Spectra were acquired on a sample containing 1.8 mM (0.9 mM dimer) <sup>2</sup>H,<sup>15</sup>N of C145A M<sup>PRO</sup> in  
99 10 mM sodium phosphate, pH 7.0, 0.5 mM TCEP, 3% v/v <sup>2</sup>H<sub>2</sub>O and 0.3 mM sodium  
100 trimethylsilylpropanesulfonate (DSS), in a 300 μL Shigemi microcell. All experiments were  
101 recorded at 25 °C on an 800 MHz Bruker Avance III spectrometer, equipped with a 5-mm TCI  
102 probe containing triple-axis gradient, and running TopSpin software version 3.1.

103 For the 4D TROSY-NOESY-TROSY experiment (Fig. 1a), the full data matrix consists of 1536\*  
104 (<sup>1</sup>H, t<sub>4</sub>, 119.8 ms) × 90\* (<sup>15</sup>N, t<sub>3</sub>, 35.1 ms) × 91\* (<sup>1</sup>H, t<sub>2</sub>, 20.0 ms) × 90\* (<sup>15</sup>N, t<sub>1</sub>, 35.1 ms) complex  
105 points. Nonuniform sampling was applied for the indirect dimensions, with unweighted, randomly  
106 distributed sampling points without time-ordering. Specifically, a total of 31896 FIDs along the  
107 directly detected t<sub>4</sub> dimension were recorded, corresponding to a sampling sparsity of 0.54%.  
108 Using 4 scans per FID for phase cycling, and an interscan delay of 2 seconds, the total  
109 measurement time was approximately 88 hours. Nonstandard processing was needed for the  
110 TROSY-NOESY-TROSY experiment because the spectrum was recorded with sensitivity-  
111 enhanced gradient selection in the <sup>15</sup>N t<sub>1</sub> evolution period that preceded the NOE mixing.  
112 Specifically, the 4D NUS data set was first sorted and expanded according to the sampling



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114 **Figure 1.** Pulse schemes for four-dimensional TROSY-NOESY-TROSY (a) and NOESY-  
 115 NOESY-TROSY (b) experiments. The filled and open rectangular bars on the  $^1\text{H}$  and  $^{15}\text{N}$  channels  
 116 represent  $90^\circ$  and  $180^\circ$  pulses, respectively. The filled shaped  $^1\text{H}$  pulses correspond to EBURP2  
 117 (labeled e) and time-reversed EBURP2 (labeled e\*) pulses (Geen and Freeman, 1991) while the  
 118 open  $^1\text{H}$  shaped pulses represent  $90^\circ$  water-flipback pulses (center lobe of a sinc profile, 1.1-ms  
 119 duration at 800 MHz) (Grzesiek and Bax, 1993). The wide filled rectangular boxes denote  $90^\circ$   
 120 water-flipback pulses (also 1.1-ms duration at 800 MHz). Unless indicated otherwise, all pulses  
 121 were applied along x. The following delays were used for the initial INEPT and TROSY  
 122 transfers:  $\delta = 2.1$  ms,  $\delta_1 = 2.1$  ms,  $\delta_2 = 2.5$  ms. The  $^1\text{H}$  chemical shift evolution during the  
 123 delay  $\tau = 0.181$  ms was compensated by offsetting the last pair of  $^1\text{H}$  and  $^{15}\text{N}$   $180^\circ$  pulses  
 124 by  $\varepsilon = \tau/2$  to avoid the linear phase error in the  $t_4$  dimension. For (a): NOE mixing time  $T_m = 200$   
 125 ms; phase cycling:  $\phi_1 = y$ ,  $\phi_2 = x$ ,  $x$ ,  $-x$ ,  $-x$ ,  $-x$ ,  $\phi_3 = y$ ,  $-y$ ,  $\phi_4 = y$ ,  $\phi_5 = y$ ,  $\phi_6 = y$ ,  $\phi_7 = y$ ,  $\phi_{\text{rec}} = y$ ,  $-y$ ,  $-y$ ,  
 126  $y$ ; gradients were sine bell or rectangular shaped, as depicted in the figure, with durations  
 127  $G_{1,2,3,4,5,6,7,8,9,10,11,12,13,14,15} = 0.977, 1.2, 0.4, 0.4, 0.986, 0.977, 0.081, 1.7, 0.977, 1.2, 0.4, 0.4, 0.986,$   
 128  $0.977,$  and  $0.081$  ms, z-strengths of 21.7, 28.7, -25.9, 32.9, 2.1, 25.9, 29.4, 30.8, 21.7, 28.7, -31.5,  
 129 38.5, 2.1, 25.9, and 35.0 G/cm, and additional x- and y-strength of -22.5, 27.5, and 25.0 G/cm for  
 130  $G_{11}$ ,  $G_{12}$ , and  $G_{15}$ , respectively. The duration of decoding pulses  $G_7$  ( $G_{15}$ ) was empirically  
 131 optimized for maximum signal, and can differ from the theoretical value derived from the  
 132 gyromagnetic ratios of  $^{15}\text{N}$  and  $^1\text{H}$  and the encoding pulses  $G_3+G_4$  ( $G_{11}+G_{12}$ ) by several  
 133 microseconds due to rise and fall times of short gradient pulses. Quadrature detection in  $t_3$  ( $t_1$ )  
 134 was achieved using the echo-antiecho scheme (Kay et al., 1992) by inverting the encoding gradient  $G_{11}$   
 135 and  $G_{12}$  ( $G_3$  and  $G_4$ ) together with  $\phi_6$  and  $\phi_7$  ( $\phi_4$  and  $\phi_5$ ) to obtain the second FID for every  $t_3$  ( $t_1$ )  
 136 increment. The  $t_2$  dimension was acquired using States-TPPI by incrementing  $\phi_2$  by  $90^\circ$ . For (b),  
 137 the EBURP2 and time-reversed EBURP2 pulses have a duration of 1.0 ms at 800 MHz, centered  
 138 at 8.3 ppm. NOE mixing times,  $T_{m1} = 50$  ms;  $T_{m2} = 300$  ms. Phase cycling:  $\phi_1 = x$ ,  $x$ ,  $-x$ ,  $-x$ ,  $\phi_2 =$   
 139  $x-\pi/4$ ,  $\phi_3 = y$ ,  $-y$ ,  $\phi_4 = y$ ,  $\phi_5 = y$ ,  $\phi_{\text{rec}} = y$ ,  $-y$ ,  $-y$ ,  $y$ . Gradients were sine bell or rectangular shaped



140 with durations  $G_{1,2,3,4,5,6,7,8,9} = 1.7, 1.2, 0.977, 1.2, 0.4, 0.4, 0.986, 0.977,$  and 0.081 ms, z-strengths  
141 of 20.3, 30.8, 21.7, 28.7, -31.5, 38.5, 2.1, 25.9, and 35.0 G/cm, and additional x- and y-strengths  
142 of -22.5, 27.5 and 25.0 G/cm for  $G_5, G_6,$  and  $G_9,$  respectively. The duration of  $G_9$  was empirically  
143 optimized for maximum signal. Quadrature detection in  $t_3$  was achieved using the echo-antiecho  
144 scheme by inverting the encoding gradient  $G_5$  and  $G_6$  together with the  $\phi_4$  and  $\phi_5$  to obtain the  
145 second FID for every  $t_3$  increment, while States-TPPI was used to obtain quadrature in the  
146  $t_1$  dimension, by incrementing the  $\phi_1$  pulse phase by  $90^\circ,$  and for  $t_2$  by incrementing  $\phi_2$  by  $90^\circ.$   
147 Pulse sequence code is available in the Supporting Information.

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149 schedule using the nusExpand.tcl script within the NMRPipe software package. The expanded data  
150 was then converted to the NMRPipe format, with the quadrature mode for  $t_3$  set to Echo-AntiEcho,  
151 while the quadrature mode for  $t_1$  was temporarily set to Complex. After the conversion, the 4D  
152 matrix needs to be transposed to enable use of the NMRPipe macro bruk\_ranceA.M to correctly  
153 reshuffle the data, turning the phase-modulated  $t_1$  dimension into conventional amplitude  
154 modulated data prior to processing as regular, complex data. This transposition is accomplished  
155 by reading in the NMRPipe-formatted matrix with the z-axis along the  $t_2$  dimension, application  
156 of the macro, and restoring the data to its original axis order prior to regular processing, with the  
157 full script available as Supporting Information. For the processing, the direct dimension was  
158 apodized with a squared, shifted sine bell window, spanning from  $72^\circ$  to  $176.4^\circ,$  in addition to 15  
159 Hz exponential line broadening, followed by zero filling and Fourier transformation.  
160 Subsequently, the indirect data points that were not experimentally sampled were reconstructed  
161 using the SMILE program, and the reconstructed data was further processed in NMRPipe. To  
162 enhance the spectral resolution, by default the acquisition times in all indirect dimensions were  
163 extended by 50% during the SMILE reconstruction, leading to an effective sampling sparsity of  
164 0.068%. The data matrix for the final reconstructed 4D spectrum consists of  $614 (^1\text{H}, F_4, 6.3$   
165  $\text{Hz/point}) \times 512 (^{15}\text{N}, F_3, 5.0 \text{ Hz/point}) \times 512 (^1\text{H}, F_2, 8.9 \text{ Hz/point}) \times 512 (^{15}\text{N}, F_1, 5.0 \text{ Hz/point})$   
166 real points.

167 The time domain data matrix of the 4D NOESY-NOESY-TROSY experiment (Fig. 1b) consists  
168 of  $1536 (^1\text{H}, t_4, 95.8 \text{ ms}) \times 90 (^{15}\text{N}, t_3, 35.1 \text{ ms}) \times 60 (^1\text{H}, t_2, 12.0 \text{ ms}) \times 60 (^1\text{H}, t_1, 12.0 \text{ ms})$   
169 complex points. An unweighted, random NUS sampling scheme with a sparsity of 1.69%  
170 (corresponding to 43856  $t_4$  FIDs) was used. Using an interscan delay of 1.7 s and 4 scans per FID,  
171 the total experimental time was approximately 110 hours. The data was processed and  
172 reconstructed in the same manner as described above, yielding the effective sparsity of 0.21% and



173 a final spectral matrix size of  $492 (^1\text{H}, F_4, 7.8 \text{ Hz/point}) \times 512 (^{15}\text{N}, F_3, 4.7 \text{ Hz/point}) \times 512 (^1\text{H},$   
174  $F_2, 13.9 \text{ Hz/point}) \times 512 (^1\text{H}, F_1, 13.9 \text{ Hz/point})$  real points. Note that since in the NOESY-  
175 NOESY-TROSY experiment the data was recorded using the echo-antiecho mode (Kay et al.,  
176 1992) only in the  $t_3$  dimension, immediately preceding acquisition, the `bruk_ranceA.M` macro was  
177 not needed after the conversion of the expanded NUS data. The residual inphase axial peaks along  
178 the  $F_2$  dimension were treated as real peaks and optimally reconstructed by SMILE to suppress the  
179 sampling artifacts of the axial signals from spreading to the regions with NOE peaks. The  
180 processing macros used for both 4D spectra are included as Supporting Information.

### 181 2.3 Spectrum analysis

182 Spectra were processed using `nmrPipe` software (Delaglio et al., 1995); peak picking and spectrum  
183 analysis was performed using `SPARKY` software (Goddard and Kneller, 2008; Lee et al., 2015) as  
184 well as `NMRDraw` (Delaglio et al., 1995). Programs for visualization and analysis were written  
185 using freely available python libraries (Hunter, 2007; Harris et al., 2020), as well as NMR-specific  
186 python libraries (Helmus and Jaroniec, 2013).

187

## 188 **3 Results and Discussion**

189 Two types of complementary 4D NOE experiments were recorded: (1) 4D TROSY-NOESY-  
190 TROSY and (2) 4D NOESY-NOESY-TROSY (Fig. 1). While the former is very similar to the  
191 HMQC-NOESY-TROSY experiment used recently for a single  $\alpha$ -helical domain with a long  
192 rotational correlation time (Barnes et al., 2019), the 4D NOESY-NOESY-TROSY experiment  
193 extends earlier work by Kaptein and co-workers (Boelens et al., 1989; Breg et al., 1990).

### 194 3.1 Recording and analysis of the 4D TROSY-NOESY-TROSY spectrum

195 The rotational correlation time of  $\text{M}^{\text{Pro}}$  at 25 °C is *ca* 27 ns, and consequently transverse  
196 relaxation is rapid for both  $^{15}\text{N}$  and  $^1\text{H}^{\text{N}}$ . For this reason, it proved beneficial to substitute a  
197 TROSY element for the HMQC segment that was previously used for such measurements (Kay  
198 et al., 1990; Barnes et al., 2019). Even though the TROSY element only utilizes half of the  
199 amide  $^1\text{H}^{\text{N}}$  magnetization present at the start of the pulse sequence, combining its  $^{15}\text{N}$   
200 evolution with sensitivity-enhanced gradient selection during the subsequent  $t_2$  evolution  
201 period (Fig. 1a) limits the loss to  $\sqrt{2}$ , or even somewhat less when taking the gain from the  
202  $^{15}\text{N}$  Boltzmann magnetization into account (Pervushin et al., 1998). Combined with the





203 enhanced relaxation properties during  $t_1$  and  $t_2$  evolution of the TROSY-selected coherence,  
204 we found experimentally that spectral quality attainable for  $M^{\text{Pro}}$  with the 4D TROSY-NOESY-  
205 TROSY was better than with the HMQC-NOESY-TROSY version of the experiment. Figure 2  
206 shows expanded regions of six ( $F_1, F_2$ ) cross-sections through the 4D spectrum, orthogonal to  
207 the ( $F_3, F_4$ ) frequencies of the six amide correlations that are highlighted in the regular 2D  $^1\text{H}$ -  
208  $^{15}\text{N}$  TROSY-HSQC spectrum of Figure 2A. The cross sections exemplify the power of such  
209 analysis for three types of secondary structure:  $\alpha$ -helix (Fig. 2b,c),  $\beta$ -sheet (Fig. 2d,e), and a  
210 loop region (Fig. 2f,g).

211 Due to the long NOE mixing time used in this experiment (200 ms), substantial spin diffusion  
212 occurs which results in numerous NOE correlations for each amide. For example,  $\alpha$ -helical  
213 residues L232 and M235 not only show NOE interactions with one another, but also share  
214 NOE cross peaks to V233 and A234, with M235 even showing a weak cross peak to N231.  
215 Such correlations are particularly useful for validating the assignments obtained from the  
216 limited number of triple resonance backbone assignment experiments that are applicable to  
217 larger proteins.

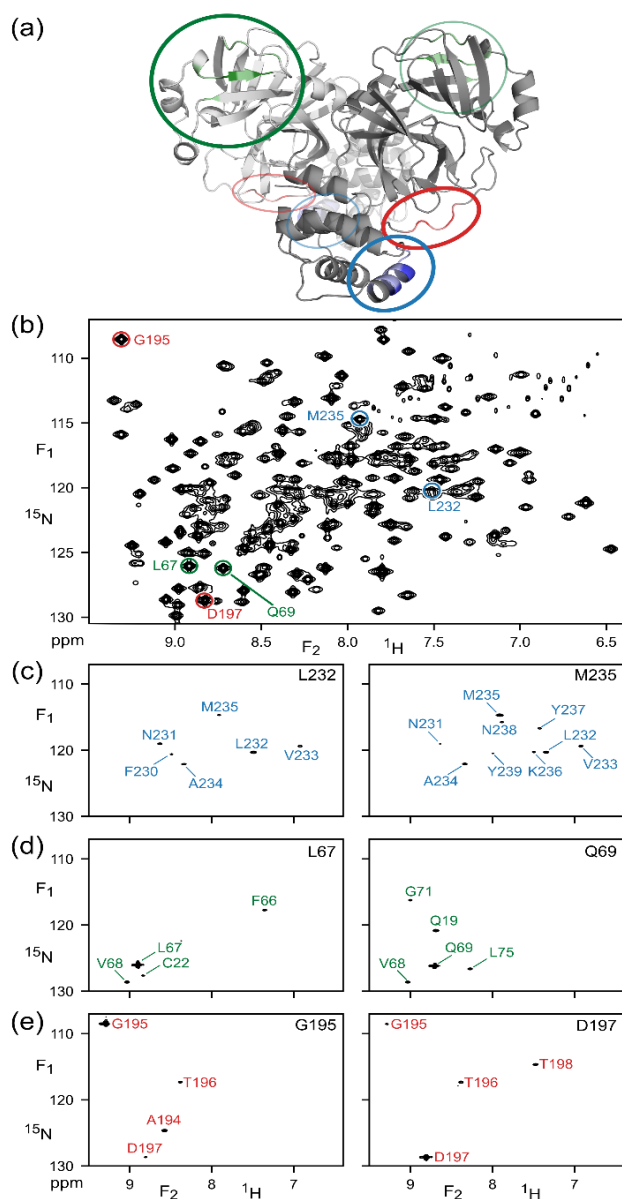
218 The amides of L67 and Q69 in strand  $\beta_4$  only share a single NOE, to sequential residue V68,  
219 but they show valuable long-range NOEs to amide protons in strands  $\beta_1$  (C22) and  $\beta_5$  (L75).  
220 G195 and D197, located in the long loop that connects strand  $\beta_{13}$  to helix  $\alpha_6$ , have an NOE  
221 to one another as well as sequential NOEs, but show no long-range interactions, consistent  
222 with the X-ray structure (Douangamath et al., 2020). However, NOEs from L67 or Q69 to T21  
223 or Q19 are not observed, despite close proximity, due to the minimal back exchange of amide  
224 protons in the  $\beta_1$  strand.

225 It is interesting to compare the diagonal peak intensities in these various cross sections of  
226 the TROSY-NOESY-TROSY spectrum. Diagonal intensity is a function of the amount of amide  
227  $^1\text{H}$  z magnetization present at the start of the pulse sequence, i.e., it depends on the non-  
228 selective longitudinal relaxation time of the amide proton, but also on the attenuation of this  
229 magnetization during the NOE mixing time, in other words, on the selective longitudinal  
230 relaxation time which is dominated by  $J(0)$  spectral density terms. The latter dominate the  
231 differences in diagonal intensity seen in the various cross sections. For example, the helical  
232 amides of L232 and M235 rapidly lose their magnetization to their proximate sequential





233 amide neighbors, separated by *ca* 2.7 Å, that each are in close contact with other neighboring  
234 protons. By contrast, none of the L67, Q69, G195 and D197 amides are closer than 3.7 Å from  
235 any neighboring protonated amide in the 1.4-Å X-ray structure of M<sup>Pro</sup> (Douangamath et al.,  
236 2020), causing their diagonal intensities to remain high.  
237



**Figure 2.** Illustration of amide-amide NOEs in perdeuterated, amide-protonated SARS-CoV-2 Main Protease, observed by 4D TROSY-NOESY-TROSY. (a) Ribbon diagram depicting the backbone homodimeric X-ray structure (pdb entry 6Y84), with colors marking the regions that are highlighted in (F<sub>1</sub>,F<sub>2</sub>) cross sections taken at the (F<sub>3</sub>,F<sub>4</sub>) coordinates of (c) L232 and M235 (blue); (d) L67 and Q69 (green) and (e) G195 and D197 (red). These resonances are marked in the 800 MHz TROSY-HSQC



### 262 3.1 Recording and analysis of the 4D NOESY-NOESY-TROSY spectrum

263 As highlighted by the work of Kaptein and co-workers, 3D NOE-NOE experiments provided  
264 an effective method for studying the  $^1\text{H}$ - $^1\text{H}$  cross relaxation network in proteins in more  
265 detail. Here, we extend this powerful experiment to four dimensions, making it more  
266 straightforward to analyze such a spectrum, while limiting the relaxation pathways by  
267 perdeuteration of the protein.

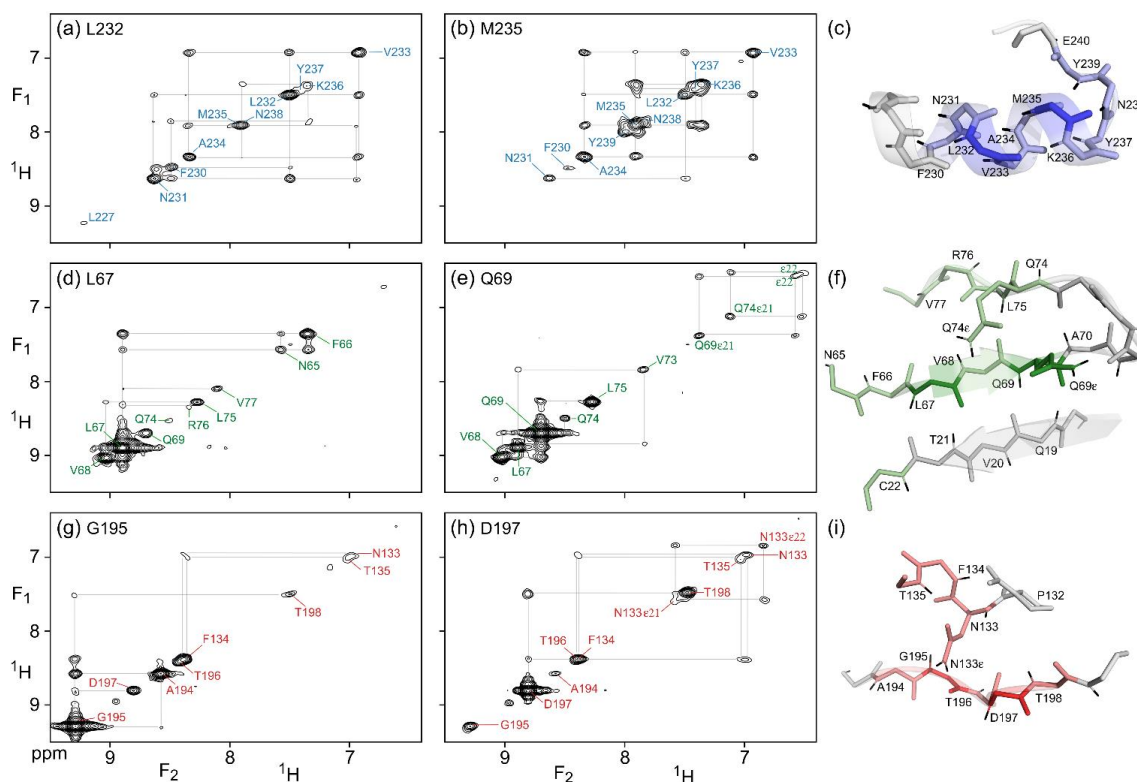
268 The pulse scheme of this 4D NOESY-NOESY-TROSY is shown in Figure 1b. It represents a  
269 straightforward extension of the original NOE-NOE 3D experiment (Boelens et al., 1989), but with  
270 the detection period substituted by the gradient-enhanced 2D  $^1\text{H}$ - $^{15}\text{N}$  TROSY scheme (Pervushin  
271 et al., 1998). The latter enhances the attainable spectral resolution in the  $t_3$  and  $t_4$  dimensions,  
272 while dispersing the detected  $^1\text{H}^{\text{N}}$  resonances in the  $^{15}\text{N}$  dimension. A number of minor technical  
273 considerations are also relevant in this respect. (1) First, in order to maximize the number of ( $t_1$ ,  
274  $t_2$ ,  $t_3$ ) data points sampled, the phase cycling of the 4D experiment was reduced to 4 steps, and the  
275 observed spectral window was restricted to the region downfield of the  $\text{H}_2\text{O}$  resonance. To prevent  
276 bleeding in of several weaker imperfectly deuterated aliphatic or exchangeable resonances present  
277 in the upfield spectral region, selective EBURP and reverse-EBURP pulses (Geen and Freeman,  
278 1991) were used to also restrict the regions where  $^1\text{H}$  resonances were excited to those resonating  
279 downfield from the water resonance. (2) Recording of a 4D NMR spectrum at adequate resolution  
280 requires the use of non-uniform sampling (NUS) (Rovnyak et al., 2004). High quality NUS  
281 reconstruction of a 4D NMR spectrum can be accomplished rapidly by the SMILE program (Ying  
282 et al., 2017) but this as well as most other NUS reconstruction software performs better if the  
283 various time domains are acquired in a manner that results in either a  $0^\circ$  or a  $180^\circ$  linear phase  
284 correction across the spectrum. For this purpose, and to ensure that the non-suppressed axial peaks  
285 can be optimally reconstructed, which requires  $0^\circ$  linear phase correction, it was preferable to insert  
286 a non-selective composite  $^1\text{H}$  inversion pulse, followed by a second such pulse that reverses any  
287 phase imperfections introduced by the first composite pulse (Hwang et al., 1997). Specifically, the  
288  $\phi_1$  phase cycling serves to eliminate axial peaks in the  $t_1$  dimension caused by pulse imperfection  
289 as well as  $T_1$  relaxation and amide exchange with solvent during  $T_{m1}$ , while also suppressing axial  
290 peaks in the  $t_2$  dimension resulting from  $T_1$  relaxation and water exchange during  $T_{m2}$ . To minimize  
291 the number of phase cycling steps,  $\phi_2$  was not phase cycled. However, this resulted in small



292 residual axial peaks along the  $t_2$  dimension caused by pulse imperfections. To ensure that these  
293 residual axial peaks were absorptive in the final spectrum, facilitating optimal SMILE  
294 reconstruction, an echo is generated by the application of two composite  $^1\text{H}$   $180^\circ$  pulses in order  
295 to suppress initial chemical shift evolution at  $t_2=0$ , thereby eliminating the need for a linear phase  
296 correction. Considering that the real and imaginary components of the residual axial signals have  
297 the same amplitude, leading to a  $45^\circ$  phase error for them in the  $F_2$  dimension, the  $\phi_2$  pulse was  
298 phase-shifted by  $-45^\circ$  to ensure that the phase of the NOE peaks matches that of the axial peaks,  
299 enabling a frequency-independent  $45^\circ$  correction to phase both types of peaks to the absorptive  
300 mode.

301 Compared to the 4D TROSY-NOESY-TROSY pulse scheme, the 4D NOESY-NOESY-TROSY  
302 experiment avoids the lossy magnetization transfer step from  $^1\text{H}$  to  $^{15}\text{N}$  and back. Instead, its  
303 magnetization is simply transferred, in part, to its nearest neighbors by cross relaxation  
304 during the first NOE mixing period of duration  $T_{m1} = 50$  ms. There is virtually no loss in total  
305 spin polarization summed over the initial “starting spin”, whose  $t_1$  evolution is monitored,  
306 and those of its immediate neighbors that are within cross-relaxation contact. As a result,  
307 the intrinsic sensitivity of such NOESY-NOESY-TROSY measurements is quite high, allowing  
308 the choice of a long duration of 300 ms for the second NOE mixing time,  $T_{m2}$ . During this  
309 second, much longer mixing time, the  $z$  magnetization distributes over considerable  
310 distances due to indirect transfers (Figure 3). Even in this fully perdeuterated protein, NOEs  
311 to nearly a dozen neighboring protons are observed on the diagonals of the  $(F_1, F_2)$  cross  
312 sections, taken at the same ( $^{15}\text{N}$ ,  $^1\text{H}$ ) frequencies used for illustrating the power of the 4D  
313 TROSY-NOESY-TROSY spectrum of Figure 2. However, as pointed out by Boelens et al. and  
314 Breg et al. (Boelens et al., 1989; Breg et al., 1990), the NOE-NOE combination offers a wealth  
315 of new information on the cross-relaxation pathways that led to the long-distance NOEs,  
316 tremendously facilitating both the assignment and analysis of distance information. Below,  
317 we briefly highlight a few examples.

318 As expected,  $\alpha$ -helical residue L232 shows intense cross peaks to both of its sequential  
319 neighbors, N231 and V233, as well as a weaker cross peak to F230. Despite the relatively  
320 short mixing time of only 50 ms that separates  $t_1$  and  $t_2$  evolution, the latter must result



321

322 **Figure 3.** (F<sub>1</sub>,F<sub>2</sub>) cross sections through the 4D NOESY-NOESY-TROSY spectrum of M<sup>Pro</sup>, taken  
323 orthogonal to the (F<sub>3</sub>,F<sub>4</sub>) TROSY-HSQC plane at the <sup>15</sup>N,<sup>1</sup>H frequencies of (a) L232, (b) M235,  
324 (d) L67, (e) Q69), (g) G195, and (h) D197. These cross sections show diagonal resonances for  
325 amide protons that are within long-range contact of the selected amide, either through direct or  
326 indirect NOE transfer during the two mixing periods that have a total duration of 50+300 ms. Off-  
327 diagonal resonances in these cross sections correspond to NOE magnetization transfer during the  
328 50-ms mixing period that separates the t<sub>1</sub> and t<sub>2</sub> evolution periods. Colors match those of the  
329 corresponding residues in Figure 2. Expanded views of the structural elements (pdb entry 6Y84)  
330 that gave rise to the observed NOEs are shown in panels (c), (f), and (i).  
331

332 mostly from indirect transfer through N231, because N231 and F230 share an intense cross  
333 peak. So, in effect each cross section through the 4D spectrum shown in Figure 3 corresponds  
334 to a 2D NOESY spectrum of a small localized region within the protein structure, making its  
335 analysis far simpler. For residues with few neighbors, direct NOE contacts between  
336 neighbors separated by as much as 4.5 Å give rise to quite intense cross peaks after 50 ms  
337 NOE mixing, as exemplified by the contacts between G195 and its A194 and T196 neighbors  
338 (Fig. 3g). A weaker cross peak between G195 and D197, at an interproton distance of 6.4 Å,



339 appears not to be mediated by spin diffusion because the G195 and D197panels (Fig. 3g)  
340 show no common strong NOE to any visible resonance. However, the possibility that the  
341 hydroxyl proton of T196 serves as a relay partner cannot be excluded.

342 The NOESY-NOESY-TROSY spectrum also shows a number of NOEs to sidechain amide  
343 protons that are not visible in the TROSY-NOESY-TROSY spectrum because the TROSY  
344 element does not select magnetization transfer for NH<sub>2</sub> groups. For example, D197 shows  
345 long-range NOEs to the N133 carboxamide protons, whereas Q69 shows NOEs to both its  
346 own carboxamide protons and to those of Q74. The non-equivalent NH<sub>2</sub> pairs are readily  
347 recognized by cross-peak to diagonal peak intensity ratios that are close to one, owing to  
348 their short interproton distance.

349

#### 350 **4. Concluding remarks**

351 The spectra shown in this study were recorded during the summer of 2020, when access to  
352 campus facilities was strongly restricted due to COVID-19 pandemic mitigation efforts.  
353 These restrictions allowed for much lengthier acquisition of spectra than commonly used,  
354 for a total of eight days for the two 4D spectra. As a benefit of NUS reconstruction, it is  
355 possible to generate spectra of the same resolution recorded in any fraction of that time.  
356 Alternatively, we can discard the data recorded at the longest values of  $t_1$ ,  $t_2$ , and  $t_3$ . Indeed,  
357 processing the same time domain data sets but shortening the time domains using a  
358 previously described protocol that considers the total normalized length of the 3D ( $t_1, t_2, t_3$ )  
359 time domain vector (Ying et al., 2019), using only one third of the acquired time domain data  
360 yields spectra that are very similar to the ones shown in Figures 2 and 3, albeit at slightly  
361 lower resolution and signal-to-noise, due to the use of three-fold less time domain data.  
362 Nevertheless, the quality of the resulting spectra remains excellent (Supporting Information  
363 Fig. S1 and S2).

364 As pointed out by Kaptein and co-workers, recording of NOE-NOE spectra provides  
365 important experimental data on the pathway of magnetization transfer during NOE mixing.  
366 Such information potentially can be used to convert this data into more quantitative distance  
367 information than is commonly done, providing access to generating higher resolution  
368 structures than is usually achieved with the qualitative interpretation of NOE intensities



369 (Vogeli et al., 2009;Vogeli et al., 2012). Quantitative NOE interpretation traditionally relied  
370 on the recording of a series of NOE buildup data, which can become comparably time-  
371 consuming as the recording of 4D NMR spectra if resonance overlap is a limiting factor, as  
372 typically is the case for NOE spectra. This problem is further exacerbated by the spectral  
373 crowding of large proteins, particularly in the  $^1\text{H}$  dimension, and while 3D spectra may give  
374 higher signal to noise ratios than 4D spectra, downstream analysis frequently requires  
375 extensive disambiguation of overlapped peaks. Our study of  $\text{M}^{\text{Pro}}$  shows that a large number  
376 of semi-quantitative NOE distances become accessible by recording of 4D NMR spectra on a  
377 perdeuterated larger protein with little or no ambiguity about the nuclei involved.

378 While the high signal to noise and spectral simplicity of working with perdeuterated proteins  
379 has long been recognized (Torchia et al., 1988;Lemaster and Richards, 1988;Grzesiek et al.,  
380 1993;Tugarinov et al., 2004) the number of structural restraints accessible used to be small.  
381 Our present study demonstrates that a much larger number of NOE interactions becomes  
382 accessible by the recording of 4D NOE spectra. Moreover, it highlights the exquisite detail  
383 and value of NOE-NOE interaction analysis explored by the Kaptein group and it  
384 demonstrates that this approach is highly suitable for the larger biomolecules and  
385 biomolecular complexes being explored today, even with extensive perdeuteration.  
386 Therefore, we believe that the recording of high quality 4D NMR spectra of the type presented  
387 in this study is entirely practical and invaluable for the structural and functional analysis of  
388 large proteins and their complexes, with possible extension to the study of nucleic acids.

389

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395 **Author contributions.** AJR expressed and purified protein samples, collected and analyzed the  
396 data, and edited the manuscript; JY optimized pulse sequence parameterization and processing and  
397 edited the manuscript; AB supervised the project and wrote the manuscript.

398 **Competing interests.** The authors declare that they have no conflict of interest.



399

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## 405 REFERENCES

- 406 Altincekic, N.: Large-scale recombinant production of the SARS-CoV-2 proteome for high-  
407 throughput and structural biology applications, *Frontiers in Molecular Biosciences*, doi:  
408 10.3389/fmolb.2021.653148 2021, 2021.
- 409 Barnes, C. A., Shen, Y., Ying, J. F., Takagi, Y., Torchia, D. A., Sellers, J. R., and Bax, A.:  
410 Remarkable Rigidity of the Single alpha-Helical Domain of Myosin-VI As Revealed by NMR  
411 Spectroscopy, *J. Am. Chem. Soc.*, 141, 9004-9017, 10.1021/jacs.9b03116, 2019.
- 412 Boelens, R., Koning, T. M. G., and Kaptein, R.: Determination of Biomolecular Structures From  
413 Proton-Proton Noes Using a Relaxation Matrix Approach, *J. Mol. Struct.*, 173, 299-311, 1988.
- 414 Boelens, R., Vuister, G. W., Koning, T. M. G., and Kaptein, R.: Observation of spin diffusion in  
415 biomolecules by 3-dimensional NOE-NOE spectroscopy, *J. Am. Chem. Soc.*, 111, 8525-8526,  
416 10.1021/ja00204a039, 1989.
- 417 Breg, J. N., Boelens, R., Vuister, G. W., and Kaptein, R.: 3D NOE-NOE spectroscopy of proteins  
418 - Observation of sequential 3D NOE cross peaks in Arc repressor, *J. Magn. Reson.*, 87, 646-651,  
419 10.1016/0022-2364(90)90324-3, 1990.
- 420 Clore, G. M., Kay, L. E., Bax, A., and Gronenborn, A. M.: Four-dimensional  $^{13}\text{C}/^{13}\text{C}$ -edited  
421 nuclear Overhauser enhancement spectroscopy of a protein in solution: Application to interleukin  
422  $1\beta$ ., *Biochemistry*, 30, 12-18, 1991.
- 423 Delaglio, F., Grzesiek, S., Vuister, G. W., Zhu, G., Pfeifer, J., and Bax, A.: NMRpipe - a  
424 multidimensional spectral processing system based on Unix pipes, *J. Biomol. NMR*, 6, 277-293,  
425 1995.
- 426 Douangamath, A., Fearon, D., Gehrtz, P., Krojer, T., Lukacik, P., Owen, C. D., Resnick, E., Strain-  
427 Damerell, C., Aimon, A., Abranyi-Balogh, P., Brandao-Neto, J., Carbery, A., Davison, G., Dias,  
428 A., Downes, T. D., Dunnett, L., Fairhead, M., Firth, J. D., Jones, S. P., Keeley, A., Keseru, G. M.,  
429 Klein, H. F., Martin, M. P., Noble, M. E. M., O'Brien, P., Powell, A., Reddi, R. N., Skyner, R.,  
430 Snee, M., Waring, M. J., Wild, C., London, N., von Delft, F., and Walsh, M. A.: Crystallographic  
431 and electrophilic fragment screening of the SARS-CoV-2 main protease, *Nature Communications*,  
432 11, 10.1038/s41467-020-18709-w, 2020.
- 433 Geen, H., and Freeman, R.: Band-selective radiofrequency pulses, *J. Magn. Reson.*, 93, 93-141,  
434 1991.
- 435 Grzesiek, S., Anglister, J., Ren, H., and Bax, A.:  $^{13}\text{C}$  line narrowing by  $^2\text{H}$  decoupling in  
436  $^2\text{H}/^{13}\text{C}/^{15}\text{N}$ -enriched Proteins. Application to triple resonance 4D connectivity of sequential  
437 amides., *Journal of American Chemical Society*, 115, 4369-4370, 1993.
- 438 Grzesiek, S., and Bax, A.: The Importance of Not Saturating  $\text{H}_2\text{O}$  in Protein NMR. Application  
439 to Sensitivity Enhancement and NOE Measurement, *J. Am. Chem. Soc.*, 115, 12593-12594, 1993.





- 440 Grzesiek, S., Wingfield, P., Stahl, S., Kaufman, J. D., and Bax, A.: Four-dimensional  $^{15}\text{N}$ -  
441 separated NOESY of slowly tumbling perdeuterated  $^{15}\text{N}$ -enriched proteins. Applications to HIV-  
442 1 Nef., *J. Am. Chem. Soc.*, 117, 9594-9595, 1995.
- 443 Harris, C. R., Millman, K. J., van der Walt, S. J., Gommers, R., Virtanen, P., Cournapeau, D.,  
444 Wieser, E., Taylor, J., Berg, S., Smith, N. J., Kern, R., Picus, M., Hoyer, S., van Kerkwijk, M. H.,  
445 Brett, M., Haldane, A., del Rio, J. F., Wiebe, M., Peterson, P., Gerard-Marchant, P., Sheppard, K.,  
446 Reddy, T., Weckesser, W., Abbasi, H., Gohlke, C., and Oliphant, T. E.: Array programming with  
447 NumPy, *Nature*, 585, 357-362, 10.1038/s41586-020-2649-2, 2020.
- 448 Helmus, J. J., and Jaroniec, C. P.: Nmrglue: an open source Python package for the analysis of  
449 multidimensional NMR data, *J. Biomol. NMR*, 55, 355-367, 10.1007/s10858-013-9718-x, 2013.
- 450 Hunter, J. D.: Matplotlib: A 2D graphics environment, *Computing in Science & Engineering*, 9,  
451 90-95, 10.1109/mcse.2007.55, 2007.
- 452 Hwang, T. L., van Zijl, P. C. M., and Garwood, M.: Broadband adiabatic refocusing without phase  
453 distortion, *J. Magn. Reson.*, 124, 250-254, 1997.
- 454 Ikura, M., Kay, L. E., and Bax, A.: A novel approach for sequential assignment of  $^1\text{H}$ ,  $^{13}\text{C}$ , and  
455  $^{15}\text{N}$  spectra of larger proteins: heteronuclear triple-resonance three-dimensional NMR  
456 spectroscopy. application to calmodulin, *Biochemistry*, 29, 4659-4667, 1990.
- 457 Kay, L. E., Clore, G. M., Bax, A., and Gronenborn, A. M.: Four-dimensional heteronuclear triple-  
458 resonance NMR spectroscopy of interleukin-1B in solution, *Science*, 249, 411-414, 1990.
- 459 Kay, L. E., Keifer, P., and Saarinen, T.: Pure Absorption Gradient Enhanced Heteronuclear Single  
460 Quantum Correlation Spectroscopy with Improved Sensitivity, *J. Am. Chem. Soc.*, 114, 10663-  
461 10665, 1992.
- 462 Lee, W., Tonelli, M., and Markley, J. L.: NMRFAM-SPARKY: enhanced software for  
463 biomolecular NMR spectroscopy., *Bioinformatics (Oxford, England)*, 31, 1325-1327,  
464 10.1093/bioinformatics/btu830, 2015.
- 465 Lemaster, D. M., and Richards, F. M.: NMR sequential assignment of Escherichia-coli thioredoxin  
466 utilizing random fractional deuteration *Biochemistry*, 27, 142-150, 10.1021/bi00401a022, 1988.
- 467 Marion, D., Driscoll, P. C., Kay, L. E., Wingfield, P. T., Bax, A., Gronenborn, A. M., and Clore,  
468 G. M.: Overcoming the overlap problem in the assignment of  $^1\text{H}$  NMR spectra of larger proteins  
469 by use of three-dimensional heteronuclear  $^1\text{H}$ - $^{15}\text{N}$  Hartmann-Hahn-multiple quantum coherence  
470 and nuclear Overhauser-multiple quantum coherence spectroscopy: application to interleukin 1 $\beta$ ,  
471 *Biochemistry*, 28, 6150-6156, 1989a.
- 472 Marion, D., Kay, L. E., Sparks, S. W., Torchia, D. A., and Bax, A.: Three-dimensional  
473 heteronuclear NMR of  $^{15}\text{N}$ -labeled proteins, *J. Am. Chem. Soc.*, 111, 1515-1517, 1989b.
- 474 Oschkinat, H., Griesinger, C., Kraulis, P. J., Sorensen, O. W., Ernst, R. R., Gronenborn, A. M.,  
475 and Clore, G. M.: 3-Dimensional NMR spectroscopy of a protein in solution, *Nature*, 332, 374-  
476 376, 1988.
- 477 Pervushin, K., Riek, R., Wider, G., and Wuthrich, K.: Attenuated T2 relaxation by mutual  
478 cancellation of dipole-dipole coupling and chemical shift anisotropy indicates an avenue to NMR  
479 structures of very large biological macromolecules in solution, *Proc. Natl. Acad. Sci. USA*, 94,  
480 12366-12371, 1997.
- 481 Pervushin, K. V., Wider, G., and Wuthrich, K.: Single transition-to-single transition polarization  
482 transfer (ST2-PT) in  $[\text{N}15, \text{H}1]$ -TROSY, *J. Biomol. NMR*, 12, 345-348, 1998.
- 483 Rovnyak, D., Fruch, D. P., Sastry, M., Sun, Z. Y. J., Stern, A. S., Hoch, J. C., and Wagner, G.:  
484 Accelerated acquisition of high resolution triple-resonance spectra using non-uniform sampling



- 485 and maximum entropy reconstruction, *J. Magn. Reson.*, 170, 15-21, 10.1016/j.jmr.2004.05.016,  
486 2004.
- 487 Torchia, D. A., Sparks, S. W., and Bax, A.: Delineation of Alpha-Helical Domains in Deuteriated  
488 Staphylococcal Nuclease By 2d Noe Nmr-Spectroscopy, *J. Am. Chem. Soc.*, 110, 2320-2321,  
489 1988.
- 490 Tugarinov, V., Muhandiram, R., Ayed, A., and Kay, L. E.: Four-dimensional NMR spectroscopy  
491 of a 723-residue protein: Chemical shift assignments and secondary structure of malate synthase  
492 G, *J. Am. Chem. Soc.*, 124, 10025-10035, 2002.
- 493 Tugarinov, V., Hwang, P. M., and Kay, L. E.: Nuclear magnetic resonance spectroscopy of high-  
494 molecular-weight proteins, *Annu. Rev. Biochem.*, 73, 107-146, 2004.
- 495 Tugarinov, V., Choy, W. Y., Orekhov, V. Y., and Kay, L. E.: Solution NMR-derived global fold  
496 of a monomeric 82-kDa enzyme, *Proc. Natl. Acad. Sci. U. S. A.*, 102, 622-627, 2005.
- 497 Vogeli, B., Segawa, T. F., Leitz, D., Sobol, A., Choutko, A., Trzesniak, D., van Gunsteren, W.,  
498 and Riek, R.: Exact Distances and Internal Dynamics of Perdeuterated Ubiquitin from NOE  
499 Buildups, *J. Am. Chem. Soc.*, 131, 17215-17225, 10.1021/ja905366h, 2009.
- 500 Vogeli, B., Kazemi, S., Guntert, P., and Riek, R.: Spatial elucidation of motion in proteins by  
501 ensemble-based structure calculation using exact NOEs, *Nat. Struct. Mol. Biol.*, 19, 1053-1058,  
502 10.1038/nsmb.2355, 2012.
- 503 Vuister, G. W., Boelens, R., and Kaptein, R.: Non-selective 3-dimensional NMR spectroscopy -  
504 The 3D NOE-HOHAHA experiment, *J. Magn. Reson.*, 80, 176-185, 1988.
- 505 Wagner, G.: Prospects for NMR of large proteins, *J. Biomol. NMR*, 3, 375-385, 1993.
- 506 Wüthrich, K.: *NMR of Proteins and Nucleic Acids*, John Wiley & Sons, New York, 1986.
- 507 Ying, J., Delaglio, F., Torchia, D. A., and Bax, A.: Sparse multidimensional iterative lineshape-  
508 enhanced (SMILE) reconstruction of both non-uniformly sampled and conventional NMR data, *J.*  
509 *Biomol. NMR*, 68, 101-118, 2017.
- 510 Ying, J. F., Barnes, C. A., Louis, J. M., and Bax, A.: Importance of time-ordered non-uniform  
511 sampling of multidimensional NMR spectra of A beta(1-42) peptide under aggregating conditions,  
512 *J. Biomol. NMR*, 73, 429-441, 10.1007/s10858-019-00235-7, 2019.
- 513 Zuiderweg, E. R. P., and Fesik, S. W.: Heteronuclear Three-Dimensional NMR Spectroscopy of  
514 the Inflammatory Protein C5<sub>a</sub>, *Biochemistry*, 28, 2387-2391, 1989.
- 515 Zuiderweg, E. R. P., Petros, A. M., Fesik, S. W., and Olejniczak, E. T.: 4-Dimensional [C-13, H-  
516 1, C-13, H-1] Hmqc-Noe-Hmqc Nmr-Spectroscopy - Resolving Tertiary Noe Distance Constraints  
517 in the Spectra of Larger Proteins, *J. Am. Chem. Soc.*, 113, 370-372, 10.1021/ja00001a060, 1991.  
518