



22 interactions can be switched on, or recoupled, in order to correlate nearby spins or to accurately determine
23 internuclear distances. Recoupling sequences can be broadly categorized as homonuclear (Bennett et al.,
24 1992; Ok et al., 1992; Zhang et al., 2020; Gelenter et al., 2020; Takegoshi et al., 2001; Szeverenyi et al.,
25 1982; Hou et al., 2011b, 2013; Carravetta et al., 2000; Bennett et al., 1998; Nielsen et al., 2012) or
26 heteronuclear (Gelenter et al., 2020; Gullion and Schaefer, 1989; Jaroniec et al., 2002; Hing et al., 1992;
27 Hartmann and Hahn, 1962; Rovnyak, 2008; Metz et al., 1994; Hediger et al., 1994; Hou et al., 2011a;
28 Brinkmann and Levitt, 2001; Gelenter and Hong, 2018; Zhang et al., 2016; Nielsen et al., 2012). The
29 homonuclear Radio Frequency Driven Recoupling (RFDR) sequence (Bennett et al., 1992) has been
30 successfully applied for the qualitative and quantitative determinations of the dipolar spin correlations in
31 materials (Saalwächter, 2013; Messinger et al., 2015; Fritz et al., 2019; Roos et al., 2018; Nishiyama et al.,
32 2014a; Wong et al., 2020; Hellwagner et al., 2018; Pandey and Nishiyama, 2018) and biomolecular samples
33 (Zheng et al., 2007; Tang et al., 2011; Shen et al., 2012; Pandey et al., 2014; Grohe et al., 2019; Andreas et
34 al., 2015; Petkova et al., 2002; Aucoin et al., 2009; Zinke et al., 2018; Zhang et al., 2017; Zhou et al., 2012;
35 Jain et al., 2017; Colvin et al., 2015; Shi et al., 2015; Daskalov et al., 2020). Sun et al. (1995) showed that
36 the RFDR pulse sequence element could also be used as a part of the SPICP experiment (Wu and Zilm,
37 1993) for removing the undesired effect of the chemical shift terms to zero order.

38 Depending on the assumptions (Ok et al., 1992; Ishii, 2001), two different Average Hamiltonian
39 Theory (Haeberlen and Waugh, 1968; Maricq, 1982) (AHT) descriptions have been detailed for RFDR. In
40 both, homonuclear dipolar recoupling occurs via a rotor-synchronized train of π -pulses, with one pulse each
41 rotor period (Bennett et al., 1992) on a single channel. In the first case, delta π -pulses are assumed (Bennett
42 et al., 1992). The efficiency of recoupling is linked with the rotational resonance conditions (Bennett et al.,
43 1992, 1998), and depends on the ratio between chemical shift offset difference and MAS rate. In the second
44 theoretical description, the effects of finite π -pulses are considered (Bennett et al., 1992; Ishii, 2001;
45 Nishiyama et al., 2014b; Zhang et al., 2015; Brinkmann et al., 2002; Ji et al., 2020). The efficiency of
46 recoupling in this case depends on a duty factor (Ishii, 2001), defined as the fraction of the rotor period



47 occupied by the π -pulse. The RFDR pulses are applied according to a variety of xy phase cycling schemes,
48 which have been analyzed with the intent to suppress imperfections associated with offset differences, rf-
49 field inhomogeneity and second order Average Hamiltonian terms between different anisotropic
50 interactions (Zhang et al., 2015).

51 The full high field truncated dipolar Hamiltonian of the homonuclear I_2 spin system is represented
52 as follows:

$$53 \quad H_{D,Full}^H = \omega_{D,12}(t)[3I_{z1}I_{z2} - \bar{I}_1 \cdot \bar{I}_2]. \quad \text{Eq. (1)}$$

54 where $\omega_{D,12}(t)$ is a periodic time dependent function (Olejniczak et al., 1984) that depends on the
55 positions of spins I_1 and I_2 within the rotor. This Hamiltonian is subsequently referred to as the full
56 Hamiltonian, and contains only the A and B terms of the dipolar alphabet (Slichter, 1990).

57 The interesting conclusion can be obtained, if we simplify the Eq. (1). The dipolar Hamiltonian
58 during RFDR can be simplified (in the absence of other interactions) by considering that $\bar{I}_1 \cdot \bar{I}_2$ commutes
59 with the secular part ($I_{z1}I_{z2}$) and with the rf-field Hamiltonian. At the end of each rotor period, the
60 oscillatory $\omega_{D,12}(t)$ term ensures zero total evolution. The simplified Eq. (1) is:

$$61 \quad H_{D,M}^H = 1.5\omega_{D,12}(t)2I_{z1}I_{z2}. \quad \text{Eq. (2)}$$

62 Comparing Eq. (2) with full Dipolar Hamiltonian of the heteronuclear IS spin system(Mehring, 1983):

$$63 \quad H_{D,Full}^{IS} = \omega_{D,12}(t)2I_zS_z, \quad \text{Eq. (3)}$$

64 we notice that the difference between Eq. (3) and Eq. (1) is a factor of 1.5. Note that we have made the
65 substitution of I_{z1} to I_z and I_{z2} to S_z while the dipolar function, $\omega_{D,12}(t)$, has been kept the same. Such
66 comparison suggests a HETeronuclear-RFDR (HET-RFDR), which should have a scaling of 1.5 as
67 compared with the homonuclear case.

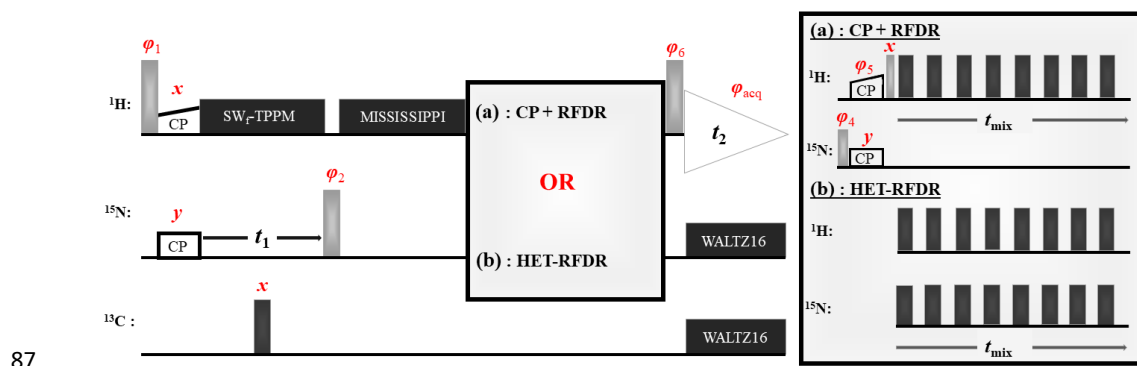


68 In this article we investigate spin dynamics under HET-RFDR, in which RFDR π -pulses are
69 applied simultaneously on two channels (Figure 1). We demonstrate simultaneous heteronuclear and
70 homonuclear transfers using HET-RFDR applied to α -PET (Movellan et al., 2019) labeled SH3 at 10 kHz
71 and 55.555 kHz MAS.

72 We perform and compare a numerical operator analysis of both RFDR and HET-RFDR
73 experiments under different simulated conditions. This numerical analysis allows to define the conditions
74 under which homonuclear and heteronuclear RFDR polarization transfers have similar behaviors, to
75 understand the paths through which the signals are transferred between operators, and to understand the
76 crucial role of 90 degree phase alternation (XY-4, XY-8, etc) (Ishii, 2001; Nishiyama et al., 2014b; Zhang
77 et al., 2015; Hellwagner et al., 2018) for both RFDR and HET-RFDR recoupling.

78 **HET-RFDR Experiments**

79 Figure 1 shows two 2D (H)N(H)H pulse sequences used to evaluate the HET-RFDR transfer. For
80 both sequences, the transfer from proton to nitrogen is implemented with ramped cross polarization (CP)
81 and then the nitrogen dimension is encoded (t_1 for 2D spectra.). In Figure 1A, the transfer to structurally
82 interesting protons is implemented with N to H CP followed by H-H RFDR. In Figure 1B, the same
83 transfer is implemented with a single HET-RDFR period. The HET-RFDR transfer avoids the back CP
84 step. Instead, nitrogen polarization is placed along the \hat{z} axis and transferred to directly bonded proton
85 spins and at the same time to remote proton spins with the simultaneous application of the π -pulses on the
86 proton and nitrogen channels.



87

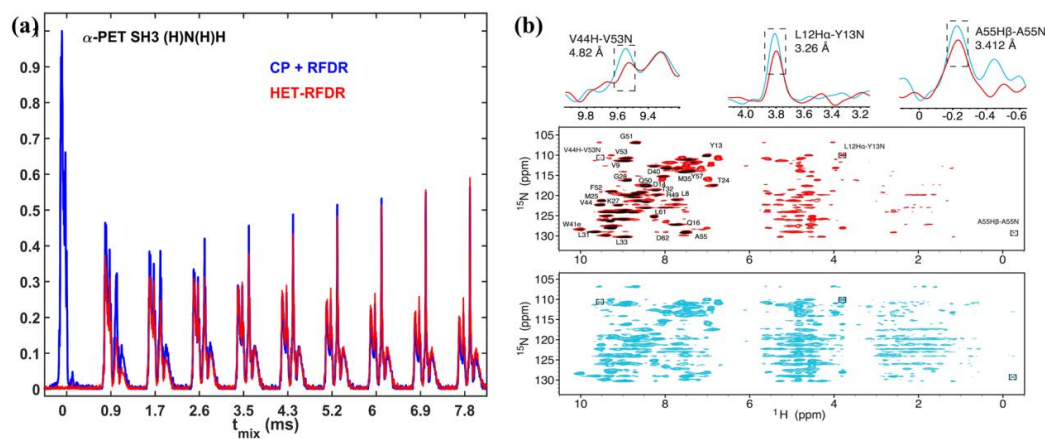
88 **Figure 1** Two versions of the (H)N(H)H pulse sequence are shown. The first, (a), is the standard implementation with CP +
 89 RFDR. The second, (b), instead uses the new HET-RFDR recoupling element. Light grey pulses represent $\pi/2$ -pulses, whereas
 90 dark grey pulses represent π -pulses. The ramped CP transfer from proton to nitrogen as well as from nitrogen to proton in (a) are
 91 indicated with constant power on the nitrogen channel and a ramp in power on the proton channel. During the indirect dimension
 92 (t_1), SW_f-TPPM decoupling is applied at 55 kHz, respectively. A single π -pulse in the middle of t_1 decouples carbon. Water
 93 suppression is implemented with the MISSISSIPPI (Zhou and Rienstra, 2008) sequence. During acquisition, WALTZ16 (Thakur et
 94 al., 2006) decoupling is applied on nitrogen and carbon channels. The phases are: $\varphi_1 = x, -x$; $\varphi_{acq} = y, -y, -y, y, -y, y, y, -y$.
 95 In (a) the phases are: $\varphi_2 = x$; $\varphi_4 = x, x, -x, -x$; $\varphi_5 = y, y, y, y, -y, -y, -y, -y$; $\varphi_6 = x$. In (b) the phases are: $\varphi_2 =$
 96 $x, x, -x, -x$; $\varphi_6 = x, x, x, x, -x, -x, -x, -x$. RFDR π -pulses on both channels use the XY8 scheme (Gullion et al., 1990).

97 Figure 2 compares the 1D and 2D spectra obtained with the two sequences of Figure 1. In Figure
 98 2a, the 1D signal is shown as a function of RFDR mixing time. For the standard sequence (blue) the N to
 99 H CP was 0.55 ms. The HET-RFDR signal is shown in (red). For the directly bonded amide protons, the
 100 HET-RFDR polarization transfer achieves only ~40% of the CP signal. This occurs at 0.846 ms mixing
 101 (second red spectrum). However, with increased mixing of about 3 ms, HET-RFDR reaches the same
 102 efficiency as the standard sequence. This is notable since transfer over long distances has been
 103 implemented with ~3 ms mixing for deuterated samples (Grohe et al., 2019; Linser et al., 2014).

104 Structurally interesting cross-peaks are indeed observed in the 2D HET-RFDR spectrum shown in
 105 Figure 2b at both 1 ms (red) and 3 ms (cyan) mixing. For comparison, the (H)NH spectrum (without
 106 RFDR mixing) is shown in black, to indicate the directly bonded amide correlations. For example, we
 107 have observed the amide-amide contact between V44 and V53, which is 4.82 Å in the crystal (pdb code



108 2NUZ (Castellani et al., 2002)). The amide to side chain contact of a A55 N to H β (3.41 Å) is also
109 indicated in the Figure, along with a sequential contact from Y13 ¹⁵N to L12 ¹H α , which is 3.26 Å. These
110 peaks are boxed in Figure 2b, and the 1D slices shown above the 2D spectra. Comparing cross peak
111 intensities with the two mixing times, we observe an increase in signal for the longer 3 ms mixing,
112 indicating that the HET-RFDR sequence is indeed competitive for recording structurally interesting
113 contacts.



114

115 **Figure 2** 1D (a) and 2D (b) (H)N(H)H spectra of α -PET labeled SH3. For all spectra the first CP from proton to nitrogen was
116 performed with 1.05 ms. (a) 1D spectra with different sequences used for the second transfer: CP + RFDR (blue) and HET-RFDR
117 (red). For CP + RFDR, 0.55 ms of CP was used. For both RFDR and HET-RFDR, t_{mix} of 0, 0.846, 1.728, 2.592, 3.456, 4.32,
118 5.184, 6.048, 6.912, 7.7776 ms are shown. (b) 2D HET-RFDR at two mixing times: 1.152 (red) and 3.456 (blue) ms. For
119 comparison, the CP based (H)N(H) spectrum is overlaid in black showing in-residue correlations. Spectra were recorded at a
120 600 MHz Bruker instrument equipped with a 1.3 mm probe and an MAS frequency of 55 kHz. The widths of π -pulses on proton
121 and nitrogen channels were 5.8 μ s and 6.6 μ s, respectively. The experimental parameters are detailed in Table 1 and 2 the
122 ‘Experimental Methods’.

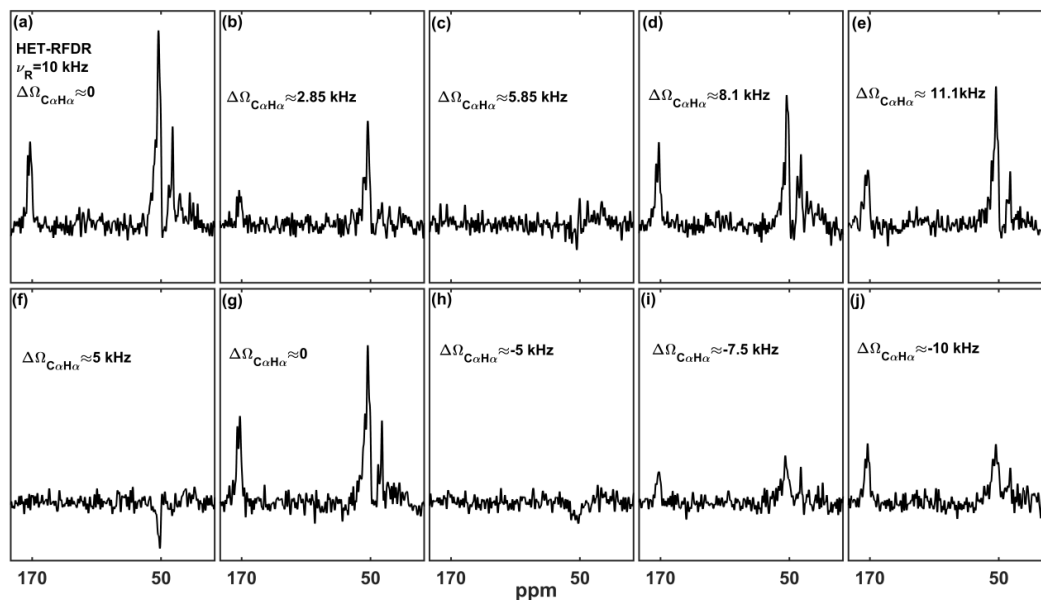
123 At 55 kHz MAS on a 600 MHz instrument, the chemical shift offsets can always be much smaller
124 than the spinning frequency. At a lower MAS frequency, the offsets become important for HET-RFDR.
125 The recoupling then depends on a heteronuclear ‘offset difference’ that we define as $\Delta\Omega_{ij} = \Omega_i - \Omega_j$,
126 where Ω_i and Ω_j are the offsets on each channel (the difference between the Larmor frequency of the spin



127 and the carrier frequency (Bak et al., 2000)). The explanation of the following behavior is described in the
128 “Numerical Operator Analysis” section. When $\Omega_i = \Omega_j = 0$ as well as $\Delta\Omega_{ij} = \Omega_i - \Omega_j \approx n\nu_R$ ($n=0, \pm 1,$
129 $\pm 2, \dots$), the HET-RFDR polarization transfer reaches local maximal intensities. However, when $\Delta\Omega_{ij} =$
130 $\Omega_i - \Omega_j \approx 0.5n\nu_R$ ($n=\pm 1, \pm 3, \dots$), the HET-RFDR polarization transfer reaches local minima. The
131 experimental confirmation of this is shown in Figure 3, where the effect of different proton and carbon
132 offsets is explored for proton-carbon HET-RFDR spectra. The spinning frequency was reduced to 10 kHz
133 MAS for these measurements and the signal detected on the carbon channel. The 1D HC HET-RFDR
134 pulse sequence is shown in the SI (Figure S1).

135 Figures 3a-e depicts the HET-RFDR spectra when the carbon carrier frequency is changed (numbers
136 show the offset from the alpha carbon at ~53 ppm), whereas the alpha proton offset is kept at 0 kHz (at
137 4.6 ppm). While heteronuclear transfer is detected at zero offset (Figure 3a) or with 11.1 kHz carbon
138 offset (Figure 3e), the signal remains in the noise when the carbon offset is 5.85 kHz (Figure 3c).

139 A similar effect can be detected when the proton carrier frequency is changed (increased from 4.6 ppm),
140 but this time the carbon offset is set to 5 kHz from C α (83.66 ppm) to show that it is the offsets on both
141 channels ($\Delta\Omega_{C\alpha H\alpha}$) that is important (Figures 3f-j). The series of spectra show a local minimal transfers at
142 offset differences of 5 kHz (Figure 3f) and -5 kHz (Figure 3h) and local maximal polarization transfers at
143 differences of 0 (Figure 3g) and -10 kHz (Figure 3j).



144

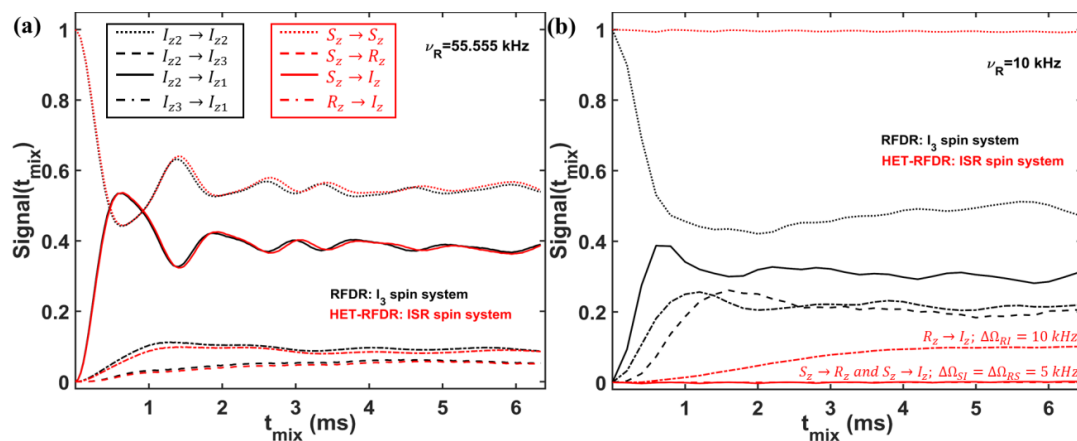
145 **Figure 3** The influence of the carbon and proton offsets on proton-carbon HET-RFDR polarization transfers at 4.8 ms mixing.
146 α -PET labeled SH3 was used with 10 kHz MAS at a 600 MHz spectrometer using a 1.3 mm probe. The widths of π -pulses on
147 proton and carbon channels were 5.8 us and 6.6 us, respectively. For (a)-(e) the proton carrier frequency was set to 4.6 ppm and
148 carbon carrier frequency was set to 51 ppm (a), 70 ppm (b), 90 ppm (c), 105 ppm (d) 125 ppm (e). For (f)-(j) the carbon carrier
149 frequency was set to 83.66 ppm and the proton carrier frequency was set to 4.6 ppm (f), 12.933 ppm (g), 21.26 ppm (h), 25.43
150 ppm (i) and 29.6 ppm (j). The indicated offset differences, $\Delta\Omega_{C\alpha H\alpha} = \Omega_{C\alpha} - \Omega_{H\alpha}$ in kHz were calculated based on typical
151 isotropic chemical shifts of C_α (51 ppm) and H_α (4.6 ppm) at a 600 MHz spectrometer. The experimental parameters are detailed
152 in Table 1 and 2 the ‘Experimental Methods’. The 1D HET-RFDR sequence is shown in the SI (Figure S1).

153 Numerical Operator Analysis

154 To comprehend the mechanism underlying the transfers during the HET-RFDR and also the well-
155 known RFDR pulse sequence, we use a numerical simulation approach. We identify the conditions under
156 which the heteronuclear and homonuclear spin systems under HET-RFDR and RFDR sequences have
157 similar behaviors. Considering the evolutions of the different spin systems through HET-RFDR and
158 RFDR during the first two rotor periods, we identify the operators that are involved in the polarization
159 transfer.



160 To identify the conditions under which the HET-RFDR and RFDR sequences have similar and
161 different behaviors we simulated a three spin system at high (55.555 kHz) and low (10 kHz) MAS
162 frequencies. In Figure 4 we compare the RFDR transferred signals for I_3 (a homonuclear 3-spin system,
163 black lines) and HET-RFDR transferred signals for ISR (three different types of spins with the names I , S
164 and R ; red lines) spin systems. At 55.555 Hz MAS when the offset difference is small compared to MAS
165 rate, the behavior of the homonuclear I_3 spin system is similar to the behavior of the heteronuclear ISR
166 spin system (Figure 4a). However, when the MAS rate is low (10 kHz) and the offset difference cannot be
167 neglected, the behaviors of these spin systems are completely different (Figure 4b). For the homonuclear
168 spin system (I_3), the polarization transfers are efficient for all dipolar pairs (black lines), whereas for the
169 heteronuclear spin system (ISR) the HET-RFDR polarization transfer is detected between R and I spins
170 (Figure 4b, red dashed-dotted line) only. For this RI pair the offset difference was chosen as 10 kHz,
171 whereas for the other spin pairs (SI , RS) the offset differences were set to 5 kHz. These simulations show
172 a special condition of $\sim 0.5\nu_R$ of offset difference for the heteronuclear spins under which the transfer is
173 negligible. The simulations are in full agreement with the experiments, which were shown in Figure 3.
174 Another interesting observation can be made from the influence of the offset difference on the RFDR
175 transfer for the homonuclear I_3 spin system (Figure 4b, black lines). For a 5 kHz of offset difference, the
176 RFDR polarization transfer between I_{22} and I_{23} spins is significantly faster with 10 kHz MAS (Figure 4b,
177 black dashed line) than at 55.555 kHz MAS (Figure 4a, black dashed line). Since the duty factor is
178 decreased with decreasing MAS frequency (Ishii, 2001): 0.33 for 55.555 kHz MAS and 0.06 for 10 kHz
179 MAS, the opposite behavior is expected if one considers only the effect of finite pulses in the RFDR
180 experiment (Ishii, 2001). It indicates that when the offset difference cannot be neglected with respect to
181 the MAS rate, it has a significant influence on the RFDR transfer efficiency between homonuclear spins
182 despite the significant remoteness from the rotational resonance condition (Bennett et al., 1992, 1998).



183

184 **Figure 4** Comparison of the simulated RFDR and HET-RFDR signals. *I*₃ (three homonuclear spins, black lines) and *ISR* (three
 185 different spin types, red lines) for 55.555 kHz (a) and 10 kHz (b) MAS. 83 kHz of rf-field is used (6 us of the widths of π-pulses).
 186 The vertical axis shows the intensities of the starting and transferred signals between different operators of *I*₃ and *ISR* spin
 187 systems, respectively (the initial operator → the measured operator): *I*_{z2} → *I*_{z2} and *S*_z → *S*_z – (the dotted lines); *I*_{z2} → *I*_{z3} and
 188 *S*_z → *R*_z – (the dashed lines); *I*_{z2} → *I*_{z1} and *S*_z → *I*_z – (the solid lines); *I*_{z3} → *I*_{z1} and *R*_z → *I*_z – (the dashed-dotted lines). For
 189 both spin systems the offset (Ω) and CSA values are: [-3; 2; 7] (kHz) and [5.2; 2.5; 3]. The dipolar coupling constants for
 190 homonuclear spin system (*I*₃) spin system are: *v*_{12,D} = 7.333 kHz, *v*_{13,D} = 2 kHz, *v*_{23,D} = 0.333 kHz. For *ISR* spin system all
 191 dipolar constants are 1.5 times larger: *v*_{1S,D} = 11 kHz, *v*_{1R,D} = 3 kHz, *v*_{SR,D} = 0.5 kHz. The simulated measurements occurs
 192 every 2 rotor periods. XY8 phase cycling is used. *I*_{z1} → *I*_{z1}, *I*_{z3} → *I*_{z3}, *I*_z → *I*_z and *R*_z → *R*_z are not shown.

193 In order to understand the different dependence on offset difference for the heteronuclear and
 194 homonuclear spin systems as well as via which operators the polarization transfer occurs, we considered
 195 the evolutions of two systems - *I*₂ homonuclear and *IS* heteronuclear spin systems - under RFDR and
 196 HET-RFDR sequences with 10 kHz MAS. We simulated the polarization transfers between different
 197 operators during the first two rotor periods, which completes the basic RFDR element: *t*(π_x) → *del*₁ →
 198 *t*(π_y) → *del*₂. We consider the amplitudes of the operators for a single molecular orientation since it
 199 allows to see the significant evolution of the operators during the two rotor periods. Figure 5a,c,e shows
 200 the amplitudes of four Cartesian operators (Ernst et al., 1987) for *IS* (HET-RFDR) and Figures 5b,d,f



201 shows the operators for I_2 (RFDR) spin systems. The measured Cartesian operators are $I_z, S_z, 2I_xS_y, 2I_yS_x$
202 and $I_{z1}, I_{z2}, 2I_{x1}I_{y2}, 2I_{y1}I_{x2}$ for IS and I_2 spin systems, respectively.

203 The evolutions of four operators *during* two rotor periods for the IS spin system the I_2 spin system are
204 different, regardless of the offset difference. However, with a zero offset difference, the simulated
205 heteronuclear operators (Figure 5a) and the homonuclear operators (Figure 5b) show the same values of
206 the amplitudes at one and two rotor periods. From the 64 possibilities (details in the SI, section ‘The
207 Operator Paths’) for magnetization transfer between heteronuclear operators I_z and S_z during the two rotor
208 periods, we find only one path with nonzero amplitude: $I_z \xrightarrow{\pi_x} 2I_xS_y \xrightarrow{del_1} 2I_xS_y \xrightarrow{\pi_y} S_z \xrightarrow{del_2} S_z$. In contrast to
209 the single path found for HET-RFDR, for the homonuclear case all 64 paths connecting operators I_{z1} and
210 I_{z2} have non-zero amplitudes. However, after each rotor period, the sum of all homonuclear paths provides
211 the same values of the amplitudes as for the heteronuclear IS spin system.

212 In contrast, with a non-zero offset difference, the amplitudes of homonuclear and heteronuclear operators
213 do not coincide at any time (Figures 5c and d). Moreover, while the amplitude of $I_{z1} \rightarrow I_{z2}$ polarization
214 transfer is significantly increased (Figure 5d, green line), the corresponding heteronuclear amplitude for
215 $I_z \rightarrow S_z$ transfer is significantly decreased (Figure 5c, green line).

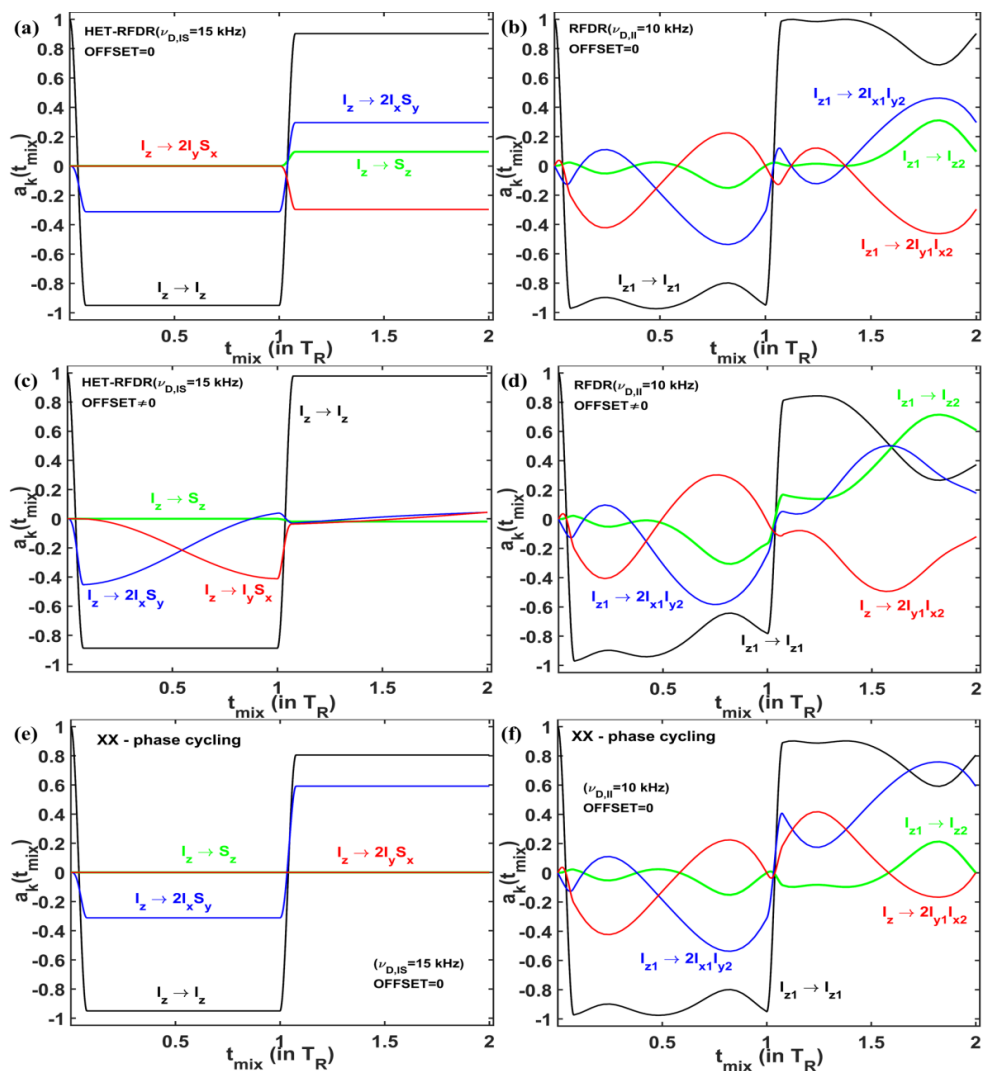
216 In Figure 3 we experimentally demonstrated (it also was shown with simulations in Figure 4b), that when
217 the offset differences, $\Delta\Omega_{C\alpha H\alpha}$, were not neglected with respect to MAS rate, the minimal and maximal
218 HET-RFDR polarization transfers were achieved under $\pm \sim 0.5\nu_R$ and $0, \pm \sim \nu_R$, respectively. Such
219 dependence on the offset difference for the heteronuclear spin system can be understood from Figure 5c,
220 where the simulations are performed with $0.5\nu_R$ offset difference. During the first π_x pulse the starting
221 signal is transferred from I_z to $2I_xS_y$. Because of the offset difference of $0.5\nu_R$, the amplitude of this
222 operator is mainly transferred to $2I_yS_x$ during the first delay (Figure 5c, red line). Since the second π -pulse
223 has phase y, there is no transfer from $2I_yS_x$ to I_{z2} and very little $I_z \rightarrow S_z$ polarization transfer overall by
224 the end of the second rotor period (Figure 5c, green line). Under $\pm \sim \nu_R$ offset difference the operator $2I_xS_y$



225 is transferred to itself during that first rotor period. Therefore the local maximal HET-RFDR polarization
226 transfer is detected. The sign, “~”, is used since we consider the spin evolution with finite pulses.

227 Such dependence of the IS spin system on the offset difference indicates the importance of the
228 phase cycling for RFDR and HET-RFDR sequences. Figures 5d and f show the evolution of the operators
229 when there is no offset and both π -pulses have the same phase cycling – XX. For IS spin system (Figure
230 5e) only two operators have nonzero amplitudes during the investigated time: I_z (black line) and $2I_xS_y$
231 (blue line), whereas S_z and $2I_yS_x$ are not created. For the I_2 spin system (Figure 5d) all four operators
232 involve during these two rotor periods. However, by the end of two rotor periods only two operators have
233 nonzero amplitudes, as for the IS spin system. In neither case is there magnetization transfer from I_z to S_z
234 nor from I_{z1} to I_{z2} after one or two rotor periods. The formal proof of zero transfer signal for homonuclear
235 two spin system in the absence of offset difference can be found in the SI, “RFDR Phase Cycling”
236 section.

237 Additional spectra and simulation results are found in the supporting information. We recorded
238 proton-carbon HET-RFDR spectra using fully protonated [^{13}C , ^{15}N] labeled SH3. We numerically
239 simulated multi-spin systems, either containing two protons and two carbons, or one nitrogen and two
240 protons, in order to track more complex transfer of magnetization. The main conclusions from the
241 simulations and the experiments in the SI are the agreement between experimental and simulated HET-
242 RFDR, and the expected small dependence of the HET-RFDR recoupling on the flip angle deviations
243 with XY8 phase cycling (Gullion et al., 1990).



244

245 **Figure 5** The operator evolution through HET-RFDR and RFDR over two rotor periods. The simulated amplitudes of the
 246 operators of a single crystal (Euler angles: 184° ; 141° ; 349°) for HET-RFDR ((a), (c)) and RFDR ((b), (d)). For the heteronuclear
 247 I_1S spin system, ($\nu_{D,IS} = 15$ kHz, the initial operator is I_z) and for the homonuclear I_2 spin system, ($\nu_{D,I1} = 10$ kHz, the initial
 248 operator is I_{z1}). The MAS frequency was 10 kHz and the rf-field was 65 kHz. Black lines – I_z and I_{z1} ; Green lines – S_z and I_{z2} ;
 249 Blue lines – $2I_x S_y$ and $2I_{x1} I_{y2}$; Red lines – $2I_y S_x$ and $2I_{y1} I_{x2}$. For (a) – (d) the phases of the first and second π -pulses are X and Y,
 250 respectively. (e) and (f) show the case of I_1S and I_2 spin systems, respectively, when the phases of the first and second π -pulses are
 251 both X. (a), (b), (e), (f) – Offset values in kHz: 0, 0. (c) and (d) – Offset values in kHz: 2, -3.



252 **Conclusion**

253 In this article we firstly demonstrated HETeronuclear RFDR recoupling, when π -pulses with XY8
254 phase cycling were applied simultaneously on two channels. Observation of simultaneous heteronuclear
255 and homonuclear polarization transfers as well as long range contacts were observed in 2D (H)NH spectra
256 using HET-RFDR for the microcrystalline protein SH3 using α -PET labeling. The comparison of 1D
257 HET-RFDR with CP followed by homonuclear RFDR showed similar efficiency of both methods at long
258 mixing times of about 3ms and longer. We experimentally demonstrated and numerically explained the
259 dependence of the HET-RFDR efficiency on the offset difference between dipolar coupled spins. A
260 numerical operator analysis of both HET-RFDR and RFDR sequences showed that when the offset
261 difference was small with respect to the MAS frequency, and with measurement at a whole number of
262 rotor periods, the behavior of HET-RFDR was similar to the well-known homonuclear RFDR. However,
263 different behaviors were observed when the offset difference could not be neglected.

264 Considering the evolution of a single crystal during HET-RFDR and RFDR, we showed the
265 operators that were responsible for the transfer. We demonstrated that XY phase cycling of π -pulses has a
266 crucial role for both HET-RFDR and RFDR transfer. With phase cycling of XX (or $X\bar{X}$) the transfers
267 between heteronuclear and homonuclear spins did not occur in the absence of offsets. With the presence
268 of the offset differences when they cannot be neglected in comparison to the MAS rate, RFDR
269 polarization transfer with phase cycling of XX or $X\bar{X}$ does occur, although with lower efficiency as was
270 described before (Bennett et al., 1992).

271 **Experimental methods**

272 *Sample preparation:* Microcrystalline chicken alpha spectrin SH3 protein was used for acquisition of all
273 experimental data. The samples were labeled with 100% protonation at exchangeable sites and either with
274 alpha proton exchange by transamination (α -PET) or with uniform ^{13}C and ^{15}N labeling with the protocol
275 described in (Movellan et al., 2019).



276 *Simulations*: HET-RFDR and RFDR simulations were performed with in-house MATLAB scripts using
277 numerical solution of the equation of motion (Nimerovsky and Goldbourt, 2012).

278 *Solid state NMR spectroscopy*: The HC and (H)N(H)H spectra of α -PET SH3 were acquired at 14.1 T (600
279 MHz) using a Bruker AVIIIHD spectrometer using a MASDVT600W2 BL1.3 HXY probe. The
280 experiments were performed at 10 kHz and 55.555 kHz MAS with the temperature of the cooling gas set
281 to 280 K and 235 K, respectively.

282 For 1D and 2D α -PET SH3 (H)N(H)H spectra, the ramped CP transfer from proton to nitrogen was
283 performed under the same conditions for all experiments: 42.95 kHz on the nitrogen channel and the optimal
284 ramped amplitude on the proton channel of 86.95-108.69 kHz. The mixing time was 1.05 ms. 9.3 kHz
285 WALTZ-16 (Shaka et al., 1983) with 25 μ s pulses and 10.4 kHz WALTZ-16 (Shaka et al., 1983) with 100
286 μ s pulses were applied on nitrogen and carbon channels during the acquisition. MISSISSIPPI water
287 suppression (Zhou and Rienstra, 2008) was applied for 100 ms with 13.513 kHz of the rf-field. The carrier
288 positions were set to 4.6 ppm, 118.5 ppm and 53.7 ppm for ^1H , ^{15}N and ^{13}C , respectively, except where
289 otherwise indicated.

290 Table 1 summarizes the applied experimental parameters for 1D spectra.

291 **Table 1** Summary of the experimental parameters used in the 1D CP + RFDR (the start and the end values are shown) and HET-
292 RFDR using α -PET labeled SH3.

	CP + RFDR		HET-RFDR
	CP	RFDR	
^1H (kHz)	86.95-108.69	86.21	86.21
^{15}N (kHz)	42.95	-	75.75
transfer time (ms)	0.55	[0-7.776]	[0-7.776]
NS	32		32
D1 (s)	2		2
AQ (s)	0.020448		0.020448
SW (kHz)	25		25

293 NS – number of scans; D1 – a recycle delay; AQ – the acquisition time; SW – the spectral width.



294 For 2D (H)N(H)H HET-RFDR spectra, during the indirect dimension 11.6 kHz SW_{τ} -TPPM (Thakur et al.,
295 2006) decoupling with 36.36 μ s pulses was applied on the proton channel. Two mixing times were used:
296 1.152 ms and 3.456 ms. The widths of π -pulses on proton and nitrogen channels were 5.8 μ s and 6.6 μ s,
297 respectively. 16 scans were acquired per increment in t_1 . The total time for the single 2D experiment was
298 10 hours. Table 2 summarizes the rest of the parameters.

299 **Table 2** Summary of the experimental parameters used in 2D HET HET-RFDR α -PET SH3 experiments.

	AQ1; AQ2 (s)	SW1; SW2 (kHz)	DW1; DW2 (μ s)
HET-RFDR	0.0527075; 0.020448	9.713; 25	102.94 20

300 1 and 2 are indirect and direct dimensions; AQ – the acquisition time; SW – the spectral width; DW – the dwell time.

301 For all 1D HC HET-RFDR experiments (Figure 3), 4.8 ms of the mixing time was applied. The widths of
302 π -pulses on proton and carbon channels were 5.8 μ s (86.21 kHz) and 6.6 μ s (75.75 kHz), respectively. 87
303 kHz SPINAL64 (Fung et al., 2000) with 6 μ s pulses was used during the acquisition. 128 scans were
304 accumulated. The spectral width was 50 kHz and the acquisition time 0.01536 s.

305 **Author Contributions**

306 EN performed the simulations and discovered heteronuclear HET-RFDR. EN and LBA designed
307 experiments. EN and KX recorded data. EN and LBA wrote the article. KTM prepared the SH3 protein
308 samples. All authors edited and approved the article.

309 **Competing Interests**

310 The authors declare that they have no conflict of interest.

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