Signal-to-noise ratio in diffusion-ordered spectroscopy: how good is good enough?

Jamie Guest[1], Peter Kiraly[1,2], Mathias Nilsson[1], Gareth A. Morris[1]

[1]Department of Chemistry, University of Manchester, Oxford Road, Manchester, M13 9PL, UK

5 [2]JEOL UK Ltd., Bankside, Long Hanborough, OX29 8SP, UK

Correspondence to: Gareth A. Morris (g.a.morris@manchester.ac.uk)

Abstract. Diffusion-ordered NMR spectroscopy (DOSY) constructs multidimensional spectra displaying signal strength as a function of Larmor frequency and of diffusion coefficient from experimental measurements using pulsed field gradient spin or stimulated echoes. Peak positions in the diffusion domain are determined by diffusion coefficients estimated by fitting

10 experimental data to some variant of the Stejskal-Tanner equation, with the peak widths determined by the standard error estimated in the fitting process. The accuracy and reliability of the diffusion domain in DOSY spectra are therefore determined by the uncertainties in the experimental data, and thus in part by the signal-to-noise ratio of the experimental spectra measured. Here the Cramér-Rao lower bound, Monte Carlo methods and experimental data are used to investigate the relationship between signal-to-noise ratio, experimental parameters, and diffusion domain accuracy in 2D DOSY experiments.

15 Experimental results confirm that sources of error other than noise put an upper limit on the improvement in diffusion domain accuracy obtainable by time averaging.

MAGNETIC RESONANCE
Open Access
Discussions

1 Introduction

20   The utility of pulsed field gradient spin or stimulated echo (PFGSE) experiments for distinguishing between the NMR signals of different species was first pointed out by Stilbs (Stilbs, 1981), but practical applications of this principle only became common with the introduction of diffusion-ordered spectroscopy (DOSY) by Morris and Johnson (Morris, 1992). In DOSY (Johnson, 1999; Morris, 2007), a pseudo-2D (or higher dimensional) spectrum is synthesised in which the signals of an NMR spectrum are dispersed into an extra dimension according to the estimated diffusion coefficient D. This is obtained by fitting

25   experimental measurements of signal attenuation as a function of pulsed field gradient amplitude to a theoretical model, usually some variation on the Stejskal-Tanner equation. (Stejskal, 1965; Sinnaeve, 2012) The value added by the DOSY approach over simple PFGSE measurements is that since all signals from spins within a given species should show the same diffusion, in favourable cases cross-sections through the DOSY spectrum at different D values give separate spectra – which can be interpreted just as normal 1D spectra – for each of the components of a mixture. This paper examines the impact of one crucial

30   determinant of the success or failure of a DOSY experiment, the signal-to-noise ratio (SNR) of the experimental data.

One common analogy is that DOSY is akin to performing chromatography within an NMR tube, separating spectra rather than physically separating analytes. The name DOSY is, however, misleading in some respects. In conventional 2D NMR methods such as COSY, NOESY and TOCSY the 2D spectrum can be obtained by direct Fourier transformation of signals that are

35   phase or amplitude modulated as a function of an evolution period t_1. The frequency F_1 at which a given signal appears is determined directly by the frequency of evolution in t_1: while the phase or amplitude of a signal may behave unexpectedly, the frequency is determined directly by the quantum mechanics, so signals should always appear at the "correct" frequency. In pseudo-2D methods such as DOSY (and relaxation-based analogues, often referred to as relaxation-ordered spectroscopy, ROSY (Lupulescu, 2003; Gilard, 2008; Nishiyama, 2010; Dal Poggetto, 2017)) this is not the case: the diffusion dimension is

40   a statistical construct, and the positions of signals in the diffusion dimension are scattered about the true D values. When a DOSY spectrum is constructed, peaks in the diffusion domain are conventionally given Gaussian shapes with widths that reflect the uncertainty in D estimated from the fitting statistics. Thus in COSY spectra, peaks with the same chemical shift are exactly aligned; in DOSY spectra, peaks with the same diffusion coefficient have Gaussian shapes that should overlap but are not coincident. This is just one reason why the interpretation of DOSY spectra demands more of the spectroscopist's skill and

45   judgment than most other types of NMR spectrum; others include the effects of signal overlap and of systematic errors introduced by imperfect experiments.

In simple mixtures in which the NMR signals are well resolved and the individual species have very different diffusion coefficients, even a crude DOSY experiment will work well. Where species of similar size, and hence similar D, are to be

50   resolved, however, high quality experimental data are essential. One of the key determinants of the utility of a DOSY spectrum is its diffusion resolution, the minimum difference in D that can safely be distinguished. In the absence of systematic error, this is determined by the signal-to-noise ratio of the experimental data. Here we use theory, empiricism and simulated and experimental data to answer some key questions: how good do our experimental data need to be to resolve a given difference in D? how is the uncertainty in D related to the signal-to-noise ratio (SNR) of raw experimental data, and can this relationship

55   be expressed in a simple form? and at what point do improvements in SNR stop translating into improved resolution in the diffusion domain?

2 Methods

In its commonest ("high resolution") form, DOSY uses least squares fitting of the amplitudes of peaks in pulsed field gradient echo spectra to determine diffusion coefficients D. A series of N otherwise identical experiments is carried out in which the

60   amplitudes G of diffusion-encoding field gradient pulses are varied to map out the decay of signal amplitude as a function of

G. In the great majority of experiments, a simple fit to a single exponential is used; multiexponential fitting is possible, but is extremely demanding of SNR (Nilsson, 2006) and is not considered here. The diffusional attenuation S_i/S_0 in successive measurements takes the form

65    $S_i/S_0 = \exp(-b_iD)$ (1)

where the form of b_i is determined by the pulse sequence used (Sinnaeve, 2012). In the simple case of a pulsed field gradient spin or stimulated echo in which spatial encoding and decoding are performed by two gradient pulses of duration δ a time $\Delta - \delta$ apart,

70

$b_i = \gamma^2 G_i^2 \delta^2 (\Delta - \delta/3)$ (2)

if the gradient pulses are rectangular in shape, or

75    $b_i = \gamma^2 G_i^2 \delta^2 (\Delta - \delta/4)$ (3)

if half-sine shaped gradient pulses are used. These expressions assume that the field gradient is constant across the sample, which is not always a good approximation; the effects of field gradient non-uniformity can be taken in to account by replacing the term G^2 by an appropriate power series in G^2 (Connell, 2009).

80

Experimental data are imperfect, most notably because of the presence of a background of random electronic noise. In a well-conducted experiment the effect of this on the measurement of the amplitude S of a signal, whether in terms of peak height or of signal integral, is well described by the addition of a Gaussian distribution of standard deviation σ_S. In the case of peak height, the signal-to-noise ratio (SNR) is by convention defined as $S/(2\,\sigma_S)$ in NMR spectroscopy. In a DOSY dataset using N

85   different gradient strengths G_i, each of the N measurements S_i of the amplitude of a given peak will have the same standard deviation σ_S. The effect of this uncertainty on the value of D determined by nonlinear least squares fitting can easily be found by brute force Monte Carlo simulation, or directly from the Cramér-Rao lower bound (CRLB). The latter has been extensively used in NMR, notably for selecting "optimum" sampling patterns G_i for the simultaneous determination of the diffusion coefficients of species of different D or for the estimation of diffusion distributions $S(D)$ (see e.g. Brihuega-Moreno, 2003;

90   Franconi, 2018; Reci, 2020; note that the derivations given in the first two references contain some minor typographical errors). Here we use the CRLB for the much more pedestrian purpose of quantifying diffusion resolution in DOSY.

A convenient measure of resolution R_D in the diffusion dimension of the DOSY spectrum is the inverse of the coefficient of variation of D, that is the ratio of the estimated D to its estimated standard deviation σ_D. Using the conventional definition of

95   SNR given above, expression (10) of (Franconi, 2018) becomes

$$R_D = \left(\frac{D}{\sigma_D}\right) = 2\,SNR\sqrt{\frac{A\,C - B^2}{A}}$$ (4)

where

100

$$A = \int_{i=1}^{N} e^{-2\epsilon_i}\,, \quad B = \int_{i=1}^{N} t_i e^{-2\epsilon_i}\,, \quad C = \int_{i=1}^{N} \epsilon_i^2\, e^{-2\epsilon_i}\,, \text{ and } \epsilon_i = b_iD$$ (5)

For a given diffusion coefficient D and choice of N gradient values G_i, therefore, the dependence of the resolution R_D on the signal-to-noise ratio of a given signal can be calculated. Here R_D was evaluated as a function of the number N of gradient

105   values sampled, the maximum exponent ϵ_{max}, and the form of the sampling scheme.

Expressions (4) and (5) allow direct calculation of R_D. Equivalent results can be obtained easily by Monte Carlo methods, constructing an attenuation table $e^{-\epsilon_i}$ and then repeatedly adding Gaussian noise n of standard deviation $\sigma_S = 1/(2\,SNR)$ to each point of the table and fitting it to a function of the form $\alpha\,e^{-\beta\epsilon_i}$. The standard deviation σ_β of the parameter β is then the inverse

110   of R_D. Again R_D was evaluated as a function of the number N of gradient values sampled, the maximum exponent ϵ_{max}, and the form of the sampling scheme.

Experimental ^{1}H DOSY data were acquired for a 100 mM solution of quinine in DMSO-d$_6$, with 50 mM sodium trimethylsilylpropionate (TSP) as reference, using the Oneshot pulse sequence (Pelta, 2002) on a 500 MHz Varian VNMRS

115   spectrometer equipped with a 5 mm triaxial gradient probe at 25 °C nominal temperature. 12 quadratically-spaced (equally spaced in gradient squared) nominal gradient amplitudes from 12.5 to 52.8 G cm^{-1} were used, with a net gradient-encoding rectangular pulse width of 1 ms and a diffusion delay Δ of 0.16 s. 8 transients of 16384 complex points were acquired for each gradient value in a total experiment time of 5 min. The data were subjected to standard DOSY processing in VnmrJ, consisting of zero-filling, reference deconvolution (Morris, 1997) with a target Lorentzian linewidth of 1.3 Hz, baseline correction, peak

120   picking, fitting to a Stejskal-Tanner equation modified to compensate for the measured gradient non-uniformity of the probe used (Connell, 2009), and construction of the DOSY spectrum using the fitted signal amplitude, diffusion coefficient D, and standard error σ_D. The signal decay for the quinine methoxy peak at 3.9 ppm, which had a SNR of 14400:1 at the lowest gradient used, was extracted, and the Stejskal-Tanner fit repeated with different additions of synthetic Gaussian noise to investigate the influence of SNR on R_D.

125   **3 Results and Discussion**

Equation (4) shows that, as is intuitively reasonable, the diffusion resolution is directly proportional to SNR (provided that systematic sources of error are negligible). The proportionality constant is, however, a complicated function of the choice of sampling function and its relation to the diffusion coefficient: the more data points are measured the better R_D will be, but just how good depends on what parts of the attenuation curve those points sample. If only the early part of the curve is sampled

130   ($\epsilon_{max} < 1$, where ϵ_{max} is the maximum value of ϵ) then the effect of diffusion on the measured points will be small, or if too wide a range of gradients G is sampled ($\epsilon_{max} \gg 1$) then many of the measured points will contain very little signal, and in both cases R_D will suffer. In a typical high resolution DOSY experiment, the sample will contain species of different sizes with a range of diffusion coefficients D. Where the range is not too wide it is common practice to use a simple sampling scheme in which the field gradient pulse amplitude is incremented either linearly, from some minimum value G_{min} to a maximum G_{max}

135   in equal steps of G:

$$G_i = G_{min} + (i-1)(G_{max} - G_{min})/(N-1) \qquad (6)$$

or quadratically, from G_{min} to G_{max} in equal steps of G^2:

140

$$G_i = \sqrt{G_{min}^2 + (i-1)(G_{max}^2 - G_{min}^2)/(N-1)} \qquad (7).$$

Because the diffusion-encoding gradient pulses G also play a part in determining coherence transfer pathways in many NMR methods for measuring diffusion, complementing and reinforcing the effects of phase cycling, it is important in practice that

MAGNETIC RESONANCE
Discussions
Open Access

145 small values of G_{min} be avoided. This is particularly important if experiments such as Oneshot (Pelta, 2002) that employ unbalanced bipolar gradient pulse pairs are used with low numbers of transients (and hence incomplete phase cycling). Common practice is therefore to use a constant ratio $G_{min}/G_{max} = \kappa$, where $\kappa = 0.05 - 0.25$, so that G varies from κG_{max} to G_{max}. Linear and quadratic sampling give similar diffusion resolution, as is shown below. Quadratic sampling can make it easier to detect systematic deviations from exponential decay as a function of gradient squared, and hence to identify peaks in which

150 the signals of species of different D overlap.

For a given set of experimental delays and pulse durations, linear and quadratic spacing in G will give different sets of Stejskal-Tanner exponents ϵ_i. Different diffusion coefficients D will give different maxima ϵ_{max}, and because the attenuation caused by the minimum gradient G_{min} depends on D, the minimum Stejskal-Tanner exponent ϵ_{min} will vary slightly with ϵ_{max}. Thus for

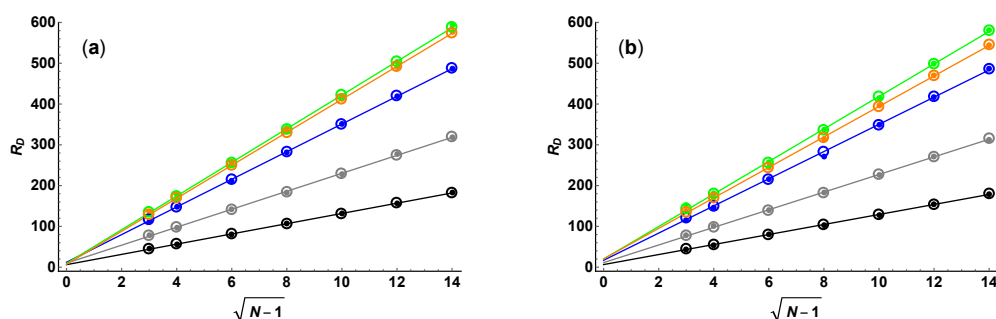155 linear sampling the Stejskal-Tanner exponents are

$$\epsilon_i = \left[\kappa + \frac{(i-1)(1-\kappa)}{(N-1)} \right]^2 \epsilon_{max} \qquad (8)$$

and for quadratic sampling

160

$$\epsilon_i = \left[\kappa^2 + \frac{(i-1)(1-\kappa^2)}{(N-1)} \right] \epsilon_{max} \qquad (9).$$

Figure 1 compares the results of Monte Carlo simulations (small filled circles) of exponential fits for the two sampling schemes, with $SNR = 100$ and $\kappa = 0.05$ in both cases, as a function of N and ϵ_{max} with the Cramér-Rao upper bounds (open circles) for

165 R_D. As expected, there is excellent agreement between the Monte Carlo and analytical results. The lines for linear regression confirm that there is a direct proportionality with $\sqrt{(N-1)}$ for low ϵ_{max}, but that for higher ϵ_{max}, where the signal is strongly attenuated for greater ϵ_i values, the line of best fit is displaced. The slope of the line of best fit for R_D as a function of $\sqrt{(N-1)}$ rises as ϵ_{max} increases until it reaches a maximum at around $\epsilon_{max} = 2.1$, after which it decreases again. This is again as expected: for low ϵ_{max} the data are dominated by points that have high precision but low attenuation, while for high ϵ_{max} the converse is

170 true.

Figure 1: Diffusion resolution R_D as a function of $\sqrt{(N-1)}$, where N is the number of gradient values used, for (a) linear and (b)
175 quadratic sampling in the gradient domain, determined by Monte Carlo simulation (small filled circles) and Cramér-Rao Least Bounds analysis (open circles), for $SNR = 100$ and maximum Stejskal-Tanner exponents ϵ_{max} of 0.25 (black), 0.5 (grey), 1 (blue), 2 (green), and 3 (orange). Solid lines show the results of linear regression of the Cramér-Rao data.

MAGNETIC RESONANCE
Discussions
Open Access

The predicted diffusion resolution R_D is a function of the sampling scheme, signal-to-noise ratio SNR, maximum Stejskal-
180   Tanner exponent ϵ_{max}, and number of gradient values used N. Given the nature of Eqs. (4) and (5) it is clear that no simple
analytical form exists for $R_D(SNR, \epsilon_{max}, N)$. Equally, it is known that R_D is directly proportional to SNR, and it is reasonable to
expect R_D to be proportional to the square root of $N-1$, since (a) increasing N will decrease the effects of random errors in
proportion to the square root of the effective number of independent measures of D, and (b) that number will be dependent on
$N-1$, since it is the *change* in signal amplitude that provides information on D, reducing the number of degrees of freedom
185   by one. In general the effective number will be less than $N-1$ for all but low values of ϵ_{max}, because signal attenuation will
reduce the information content for higher values ϵ_i. It is thus reasonable to seek an approximate analytical representation of
the form

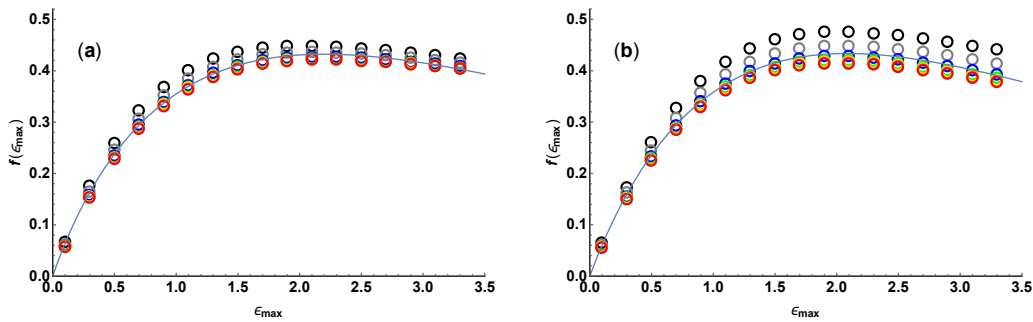$$R_D(SNR, \epsilon_{max}, N) \approx SNR \sqrt{(N-1)}\, f(\epsilon_{max}) \qquad (10).$$

190

Figure 2 shows the variation of f as a function of ϵ_{max}, calculated numerically using Eqs. (4), (5) , (8) and (9) for values of N
between 10 and 200 for linear and quadratic sampling, together with fits to a three-parameter function of the form

$$f(\epsilon_{max}) = a\,\epsilon_{max}\,e^{-b\,(\epsilon_{max})^c} \qquad (11).$$

195

The quality of fit is more than adequate for practical use, establishing a simple relationship between diffusion resolution,
signal-to-noise ratio and experimental parameters; fit parameters are given in Table 1.

200   **Figure 2: Relative diffusion resolution $f(\epsilon_{max})$ determined Cramér-Rao Least Bounds analysis (open circles) as a function of
maximum Stejskal-Tanner exponent ϵ_{max}, for (a) linear and (b) quadratic sampling in the gradient domain with 10 (black), 17 (grey),
37 (blue), 65 (green), 101 (yellow), and 197 (red) gradient values. Solid lines show the results of nonlinear regression of the data
points shown to the three-parameter function Eq. (11).**

205

	Linear sampling	Quadratic sampling
a	0.72	0.66
b	0.71	0.61
c	0.77	0.86

**Table 1. Fitted parameters for Eq. (11) obtained from the data of Fig. 2. No error estimates are given as the data fitted are not
normally distributed.**

210 In principle, diffusion accuracy should increase indefinitely as the signal-to-noise ratio of the experimental data increases. In practice this is not the case, because spectral noise is far from the only source of uncertainty in the signal attenuations measured in DOSY experiments. Radiofrequency pulse irreproducibility, field-frequency ratio instability, gradient noise, temperature variation and a range of other sources all limit the reliability of signal intensity measurements in NMR, limiting resolution in DOSY and causing t_1-noise in multidimensional spectra (Mehlkopf, 1984; Morris, 1992). In general, the accuracy and

215 reproducibility of NMR data tend to deteriorate as the number of pulses used in a sequence increases (because of pulse phase and amplitude jitter caused by limited radiofrequency spectral purity), as the durations of the delays used increase (because of the cumulative effect of field-frequency fluctuations), and as the overall duration of an experiment increases (because of slow changes in environmental factors such as room temperature, air pressure etc.). Most such perturbations are at least semi-systematic in nature, but many (particularly pulse phase instability) have effects that can appear random, and can therefore

220 decrease, at least to some extent, with time averaging. Other sources of distortion in the measured signal decay are both systematic and reproducible and therefore do not decrease with time averaging. These include changes in signal attenuation caused by convection (never wholly absent in practical NMR experiments on liquids (Swan, 2015; Barbosa, 2016)), and by the presence of signals from unwanted coherence transfer pathways. Distortions caused by spatial non-uniformity of the field gradient can be corrected for if appropriate calibration is performed (Connell, 2009).

225

There is thus a practical limit to the benefits to be gained by increasing SNR, whether by time averaging, increasing the signal strength (e.g. by increasing sample concentration), or reducing the noise (e.g. by using a cold probe and preamp). This is illustrated here with experimental data obtained as described earlier for the methoxy signal from a sample of quinine. The starting SNR of the quinine methoxy peak in the lowest gradient spectrum was 14400:1; successively greater amounts of

230 synthetic Gaussian noise were added and fitting repeated, averaging the results of 100 additions, to show the influence of SNR on the diffusion resolution R_D. If the contributions from sources other than noise to the errors in the experimental peak height as a function of gradient strength are normally distributed and have a root mean square deviation which is a fraction $1/(2\ SNR_{lim})$ of the initial peak amplitude, then the effect on fitting, and hence on diffusion resolution, of adding uncorrelated noise is to degrade the effective signal-to-noise ratio SNR in Eq. (10) to
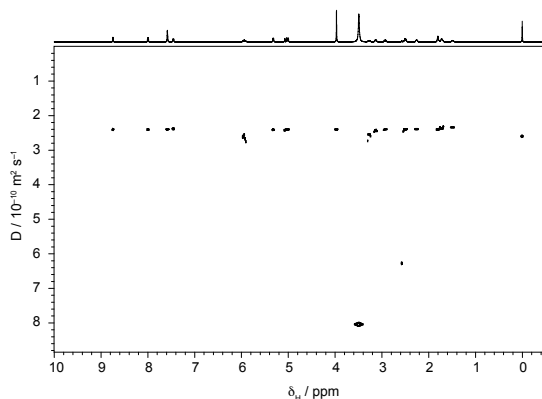
235
$$SNR_{eff} = SNR \sqrt{\frac{SNR_{lim}^2}{SNR_{lim}^2 + SNR^2}}$$
(12).

This gives a final predicted diffusion resolution for given experimental conditions of

$$R_D(SNR, \epsilon_{max}, N) \approx \frac{SNR}{\sqrt{1 + \left(\frac{SNR}{SNR_{lim}}\right)^2}} \sqrt{(N-1)} f(\epsilon_{max})$$
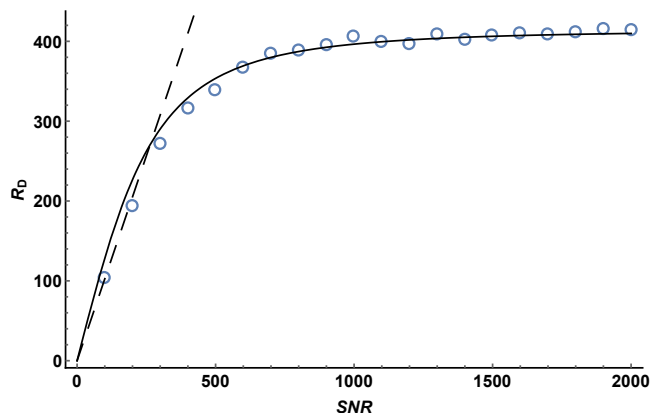(13),

240

where $f(\epsilon_{max})$ can be approximated by Eq. (11). Thus if the noise contribution to the experimental uncertainty is dominant, the effective signal-to-noise ratio is the actual SNR, but at high SNR the effective signal-to-noise ratio for the purposes of Stejskal-Tanner fitting is the limit SNR_{lim} imposed by other error sources.

245 **Figure 3: 500 MHz Oneshot ^{1}H DOSY spectrum of 100 mM quinine in DMSO-d$_6$ with 50 mM sodium trimethylsilylpropionate as reference, acquired as described in the text.**

To investigate the effect of signal-to-noise ratio on diffusion resolution, synthetic noise was added to the experimental data used to construct the ^{1}H DOSY spectrum of quinine shown in Fig. 3. Figure 4 shows the effect of SNR on the measured R_D

250 for experimental data for the quinine methoxy peak, found by titrating in extra noise as described above. The experimental signal-to-noise ratio of the first gradient increment was 14400:1, but the diffusion resolution R_D found when the raw experimental data were fitted was only 420, a small fraction of the predicted value of almost 15000. As Figure 3 shows, at low SNR the observed diffusion resolution follows the line expected for the unmodified Cramér-Rao limit of Eq. (11), but as SNR increases the improvement in R_D levels off, slowly approaching the limit seen for the data with no noise added. Fitting of Eq.

255 (13) to the noise-supplemented experimental data gave a value of just over 300 for SNR_{lim}. To put this value in context, it corresponds to a respectably small root mean square uncertainty in the signal amplitudes measured of $1/600 \sim 0.17\%$ of the original peak intensity, typical of good quality results obtained with multiple pulse sequences on a modern spectrometer. With extended time averaging and appropriate precautions and instrumental interventions it is possible to obtain data with significantly smaller uncertainties than this (see e.g. Power, 2016), but the cost in time and effort can be considerable.

260

Figure 4: Diffusion resolution R_D as a function of signal-to-noise ratio for the methoxy signal of quinine in a Oneshot experiment on a 100 mM solution of quinine in DMSO-d$_6$. Open circles show the average of 100 values of R_D by fitting of the experimental data with the addition of synthetic Gaussian noise for each value of SNR, the dashed line shows the predicted Cramér-Rao limit, Eq. (11),

265 **for the experimental parameters used ($N = 12$, $\epsilon_{max} = 0.76$), and the solid line the result of nonlinear least-squares fitting of the Cramér-Rao limit modified to take into account the presence of other errors in the signal intensity, Eq. (12), with $SNR_{lim} = 305$.**

MAGNETIC
RESONANCE
Open Access
Discussions

4 Conclusions

It is well known that the signal-to-noise ratio of diffusion-weighted experimental NMR data plays a critical role in determining
270 the diffusion resolution of a DOSY spectrum constructed from it. There is thus a temptation to conduct very long experiments
with extensive time averaging in order to obtain the best possible results. Conversely, in dilute systems the temptation is to
conduct equally long experiments in the hope of obtaining results with sufficient diffusion resolution to shed light on speciation
etc. In both cases it is possible, and indeed common, to waste a great deal of instrument time for no good result, either because
sources of error other than noise dominate the fitting statistics, or because the final signal-to-noise ratio is insufficient. Here it
275 is shown that a trivial calculation will show both whether or not such experiments are worth attempting in the first place, and
what limiting diffusion resolution is achievable.

Code and data availability

Raw experimental data for Fig. 3 and the Mathematica code used to generate Figs. 1, 2 and 4 can be downloaded from DOI
280 10.17632/d7bdxz9hsk.1.

Author contributions

GAM and MN designed the experiments and simulations. JG and PK carried out the experimental work. JG and GAM
performed the simulations and analysis. GAM prepared the manuscript with contributions from all co-authors.
285

Competing interests

Mathias Nilsson is an editor of MR.

Acknowledgments

References

Barbosa, T.M., Rittner, R., Tormena, C.F., Morris, G.A. and Nilsson, M.: Convection in liquid-state NMR: expect the
unexpected, RSC Advs. 6, 95173-95176, doi: 10.1039/C6RA23427E, 2016.

295 Connell, M. A., Bowyer, P. J., Bone, P. A., Davis, A. L., Swanson, A. G., Nilsson, M. and Morris, G. A.: Improving the
accuracy of pulsed field gradient NMR diffusion experiments: Correction for gradient non-uniformity, J. Magn. Reson. 198,
121-131, doi: 10.1016/j.jmr.2009.01.025, 2009.

Dal Poggetto, G., Castañar, L., Adams, R. W., Morris, G. A. and Nilsson, M: Relaxation-encoded NMR experiments for
mixture analysis: REST and beer, Chem. Commun. 53, 7461–7464, doi: 10.1039/c7cc03150e, (2017).

300 Damberg, P., Jarvet, J. and Gräslund, A.: Accurate measurement of translational diffusion coefficients: a practical method to
account for nonlinear gradients, J. Magn. Reson. 148, 343–348, doi: 10.1006/jmre.2000.2260, 2001.

Gilard, V., Trefi, S., Balayssac, S., Delsuc, M. A., Gostan, T., Malet-Martino, M., Martino, R., Pringent, Y. and Taulelle, F.:
DOSY NMR for Drug analysis, in NMR Spectroscopy in Pharmaceutical Analysis, ed. Holzgrabe, U., Wawer, I. and Diehl,
B., Elsevier, Amsterdam, ch. 6, pp. 269-289, doi: 10.1016/B978-0-444-53173-5.X0001-7, 2008.

305 Johnson, C.S .: Diffusion ordered nuclear magnetic resonance spectroscopy: principles and applications, Prog. Nucl. Magn.
Reson. Spectrosc., 34, 203–256, doi: 10.1016/S0079-6565(99)00003-5, 1999.

Lupulescu, A., Kotecha, M. and Frydman, L.: Relaxation-Assisted Separation of Chemical Sites in NMR Spectroscopy of Static Solids, J. Am. Chem. Soc. 125, 3376-3383, doi: 10.1021/ja021173m, 2003.

Mehlkopf, A.F., Korbee, D., Tiggelman, T.A. and Freeman, R., J. Magn. Reson. 58, 315-323, doi: 10.1016/0022-2364(84)90221-X, 1984.

Morris, G.A.: Systematic Sources of Signal Irreproducibility and t_1 Noise in High-Field NMR Spectrometers, J. Magn. Reson., 100, 316-328, doi: 10.1016/0022-2364(92)90264-8, 1992.

Morris, G. A.: Diffusion-ordered spectroscopy (DOSY), eMagRes, doi: 10.1002/9780470034590.emrstm0119.pub2, 2007.

Morris, G.A., Barjat, H. and Horne, T.J.: Reference deconvolution methods, Prog. Nucl. Magn. Reson. Spectrosc. 31, 197-257, doi: 10.1016/S0079-6565(97)00011-3, 1997.

Morris, K. F. and Johnson, C. S.: Diffusion-ordered two-dimensional nuclear magnetic resonance spectroscopy, J. Am. Chem. Soc., 114, 3139-3141, doi: 10.1021/ja00034a071, 1992.

Nilsson, M., Connell, M. A., Davis, A. L., and Morris, G. A.: Biexponential fitting of diffusion-ordered NMR data: practicalities and limitations, Anal. Chem. 78, 3040–3045, doi: 10.1021/ac060034a, 2006.

Nishiyama, Y., Frey, M. H. Mukasa, S. and Utsumi, H.: ^{13}C solid-state NMR chromatography by magic angle spinning ^{1}H T_1 relaxation ordered spectroscopy, J. Magn. Reson. 202, 135-139, doi: doi:10.1016/j.jmr.2009.10.009, 2010.

Pelta, M. D., Morris, G. A., Stchedroff, M.J., and Hammond, S. J.: A one-shot sequence for high-resolution diffusion-ordered spectroscopy, Magn. Reson. Chem. 40, S147-s152, doi: 10.1002/mrc.1107, 2002.

Sinnaeve, D.: The Stejskal-Tanner equation generalized for any gradient shape – an overview of most pulse sequences measuring free diffusion, Concepts Magn. Reson. A, 40A, 39–65, doi: 10.1002/cmr.a.21223, 2012.

Stejskal, E. O. and Tanner, J. E: Spin diffusion measurements: spin echoes in the presence of a time-dependent field gradient, J. Chem. Phys. 42, 288–292, doi: 10.1063/1.1695690, 1965.

Stilbs, P.: Molecular self-diffusion coefficients in fourier transform nuclear magnetic resonance spectrometric analysis of complex mixtures, Anal. Chem., 53, 2135–2137, doi: 10.1021/ac00236a044, 1981.

Swan, I., Reid, M., Howe, P.W.A., Connell, M.A., Nilsson, M., Moore, M.A. and Morris, G.A.: Sample convection in liquid-state NMR: why it is always with us, and what we can do about it, J. Magn. Respn., 252, 120-129, doi: 10.1016/j.jmr.2014.12.006, (2015).