



Selective excitation enables encoding and measurement of multiple diffusion parameters in a single experiment

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Abstract. Band selectivity to address specific resonances in a spectrum enables one to encode individual settings for diffusion experiments. In a single experiment, this could include different gradient strengths (enabling coverage of a larger range of diffusion constants), different diffusion delays, or different gradient directions (enabling anisotropic diffusion measurement). In this report a selective variant of the bipolar pulsed gradient, eddy-current delay (BPP-LED) experiment enabling selective encoding of three resonances was implemented. As proof-of-principle, the diffusion encoding gradient amplitude was assigned a range dependent on the selected signal, thereby allowing the extraction of the diffusion coefficient for water and a tripeptide (Met-Ala-Ser) with optimal settings in a single experiment.

1 Introduction

10 There is little dispute over the importance of diffusion as a physical effect, and its influence on many natural processes.

Diffusion poses a limiting factor in many industrial processes, such as the mixing of chemical reagents to achieve a specific product with sufficient yield. Understanding the interplay between intrinsic diffusion rates and operational time dependent parameters need to be properly understood and carefully considered in designing such manufacturing processes. Nuclear magnetic resonance (NMR) has proven to be uniquely capable to extract diffusion constants for a specific chemical substance and, in favorable cases, even mixtures, and also to study and understand the processes of diffusion at all length scales and within all compartments available to the molecule under consideration. Thus NMR has facilitated experimental proofs of Fick's laws, and has facilitated precise measurements of anisotropic effects arising from spatially extended molecules in solution, and subtracting the effects due to geometry, or ionic charges, and the like.

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In magnetic resonance imaging, diffusion is currently the limiting spatial resolution factor for inductive NMR detection, because excited spins in a molecule tend to diffuse away from their excitation site whilst waiting for pulse readout. Whereas this uncertainty cannot be removed completely, shorter pulse sequences have the effect of improving resolution by reducing the distance a spin ensemble can wander.

Spatial resolution is especially important in such areas as brain science and brain diagnostics, where anisotropic diffusion tensor imaging is the primary noninvasive means to discover the sub-cellular structure of a specific brain (Göbel-Guéniot et al. (2020)). Essentially, diffusing spin ensembles do not readily traverse cell walls and axons, so that the local structure of brain tissue renders an anisotropic response, with directional weighting being in favour of gliding along the cell walls. In this way, diffusion has helped to reveal brain connectivity patterns. But also in studies of nanoporous materials, anisotropic diffusion parameters have been used to reveal local nanostructure.

Diffusion anisotropic measurements aim to reveal the 3-dimensional pattern of molecular movement. Mathematically, the movement at a spatial point has to be resolved in three orthogonal directions, which typically would require at least three motionally sensitive measurements, each in combination with a spatial gradient aligned with the specific direction of measurement. The most time-consuming part of the pulse sequence is the echo time, and the recovery time. Spatial encoding will additionally require the three measurements for each spatial voxel, further slowing down the acquisition.

A degree of freedom available to spectroscopic diffusion measurements is the spectral dispersion, taking advantage of the individual resonances as a means to encode additional information within a single experiment. This is particularly interesting for molecular mixtures whose components vary in the physical dimensions and thus their diffusion coefficient, or for a tracer molecule in an anisotropic environment where diffusion is dependent on direction. Instead of performing multiple diffusion measurements, each optimized for a particular regime, a frequency bandwidth could be selectively encoded with appropriate diffusion parameters independent of another, different bandwidth, itself encoded with differing diffusion parameters. This could be extended down to encoding individual resonances in a spectrum with diffusion parameters appropriate for extracting diffusive properties with high precision.

There are two additional benefits to integrating selective elements to the experiment: first is the elimination of dominating, uninteresting signals (typically solvent) to improve sensitivity to minor components. This has been demonstrated for protein diffusion in water using a selective version of the stimulated echo experiment (Yao et al. (2014)) and a selective version of the spin echo experiment for measuring minor components in a mixture (Howe (2017)). The second benefit, noted by both Yao and co-workers (Yao et al. (2014)) and Howe (Howe (2017)), is to reduce spectral congestion and thereby improve DOSY data analysis, an active field of research in extracting diffusion coefficients from overlapping signals (Aguilar et al. (2010); Colbourne et al. (2011); Foroozandeh et al. (2018); Lin et al. (2020)).

In this report, we have extended the stimulated echo experiment using bipolar gradients and longitudinal eddy current compensation (BPP-LED) (Wu et al. (1995)) to enable selective diffusion encoding. As proof-of-concept we demonstrate the ability to selectively address up to three individual resonances (each with a bandwidth of $60\,\mathrm{Hz}$), each encoded with independent diffusion parameters.





In this paper we are **specifically paying tribute** to Geoffrey Bodenhausen, a pioneer of NMR spectroscopy, on the occasion of his seventieth birthday. Our chief source of inspiration comes from one of his earliest papers, published in 1976 (Bodenhausen et al. (1976)) whilst he was in Oxford, and which explores selective excitation, as well as numerous of his papers that have explored the measurement of diffusion by various ingenious means.

2 Materials and Methods

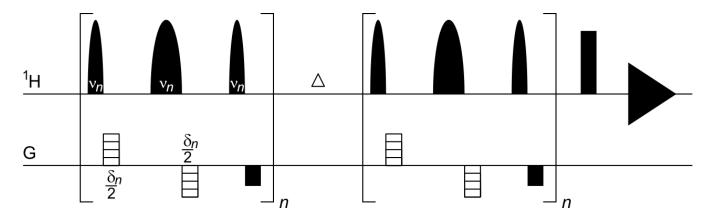


Figure 1. The selective BPP-LED (bipolar pulse paired, longitudinal eddy-current delay) diffusion experiment: Sel-BPP-LED. Spectral regions with center frequency ν_n can be encoded - n=3 was tested in this work. For each n, ν_n and δ_n can be uniquely defined. Despite a hard 90° read pulse, using the same phase cycle as the BPP-LED sequence, the resulting spectrum consists of only the selected spectral regions (Figure 2).

Materials. Deuterium oxide (D_2O) and the tri-peptide Met-Ala-Ser (MAS) were purchased from Sigma Aldrich and used as received. All H_2O was of MQ quality. An NMR sample in a $5\,\mathrm{mm}$ NMR tube was prepared by dissolving $10\,\mathrm{mg}$ MAS in $500\,\mu\mathrm{L}$ of $90:10\,D_2O:H_2O$.

NMR Spectroscopy. NMR experiments were performed using an Avance III 500 MHz wide-bore NMR spectrometer (Bruker Biospin, Ettlingen) using a Micro5 micro-imaging probe equipped with a $5 \,\mathrm{mm}$ NMR detector. Sample temperature was controlled using water cooling flowing through the imaging gradient sleeve, maintained at $20\,^{\circ}\mathrm{C}$.

Non-selective diffusion experiments were performed using the bipolar gradient, longitudinal eddy current compensated experiment (BPP-LED) (Wu et al. (1995)) (Bruker pulse program ledbpge2s1d). The diffusion-encoding gradient pulse was 2 ms, gradient recovery time was 200 µs, gradient strength was varied using the parameter optimization function in TopSpin 3.6.3 (Bruker BioSpin) from 1 to 95% of maximum gradient strength through 16 experiments, and the diffusion time was 250 ms.

Selective diffusion experiments were performed using a modified version of the non-selective experiment (Sel-BPP-LED) - 90° hard pulses were replaced by sinc shaped pulses, and 180° refocusing pulses were replaced by Gaussian refocusing pulses (Sinc1.1000 and Gaus1_180r.1000 from the Bruker shaped pulse library), Figure 1. The selective pulse length and power





Signal	Selective	SNR	Diffusion Coefficient
	(y/n)	$(\times 10^3)$	$(\times 10^{-10} \ m^2 \ s^{-1})$
Water	n	231.8 ± 0.7	20.20 ± 0.03
Water	у	229 ± 1	19.44 ± 0.01
Ala	n	7.34 ± 0.04	4.11 ± 0.01
Ala	у	11.23 ± 0.06	4.150 ± 0.001

Table 1. Non-selective (BPP-LED) and selective (Sel-BPP-LED) diffusion experiments are compared. The water (4.8 ppm) and alanine methyl signal of MAS (1.4 ppm) were used for these analyses. SNR was calculated using the first increment in the diffusion series. Diffusion coefficients were extracted from the diffusion plots using Equation 1. The diffusion time was the same for all experiments ($\Delta = 250 \, \mathrm{ms}$). Reported values are the mean \pm standard deviation of triplicate measurements.

were calculated using the Shape Tool (TopSpin 3.6.3) using a selective bandwidth of $60\,\mathrm{Hz}$, resulting in excitation pulses of $26.8\,\mathrm{ms}$ and refocusing pulses of $14.7\,\mathrm{ms}$. The diffusion time was $\Delta=250\,\mathrm{ms}$, with the timing in the pulse program modified taking into account the additional selective blocks in the pulse sequence. Three signals were chosen for the selective diffusion experiment: the water signal (4.8 ppm), and from the MAS peptide the methyl signal of methionine (2.1 ppm) and the methyl signal of alanine (1.45 ppm).

All NMR experiments were performed using RF pulses calibrated on the day of measurement. Each measurement consisted of 8 scans, each scan containing 32 K data points over a spectral width of 20 ppm. The FIDs were zero-filled by a factor of 2 and multiplied by an exponential function equivalent to $0.3\,\mathrm{Hz}$ line width prior to Fourier transformation. The series of 16 spectra from each diffusion measurement was extracted using an in-house Matlab script (Matlab 2020b, Mathworks, Natick, USA). The Matlab 'fit' function was used to extract the diffusion coefficients.

Diffusion coefficients were extracted by fitting the intensity versus applied gradient strength using the equation (Wu et al. (1995); Sinnaeve (2012)):

$$I = exp(-\gamma^2 G^2 \delta^2 D(\Delta - \delta/3 - \tau/2)) \tag{1}$$

where I is the normalized NMR signal intensity, γ is the 1 H gyromagnetic ratio, δ is the diffusion gradient pulse length, Δ is the diffusion time, τ is the time between the bipolar gradient pulses, and G is the applied gradient strength. The diffusion of water was used to calibrate the gradient strength, assuming a diffusion coefficient $D = 2.02 \times 10^{-9} \, \mathrm{m}^{2}/\mathrm{s}$ (Tofts et al. (2000); Holz et al. (2000)).

2.1 Results and Discussion

A series of experimental NMR spectra measured using both BPP-LED and Sel-BPP-LED are presented in Figure 2, with a summary of details provided in Table 1. The SNR of the normalized spectra was essentially unchanged in the case of the water signal, while a significant improvement (+53%) was measured for the MAS-Ala methyl signal. The Sel-BPP-LED experiment yielded intensity decay curves faithfully reproducing the non-selective experiment (Figure 3a). A slight variation



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in the extracted diffusion coefficients was observed (3.7% and -1.1% relative deviation for D_{water} and $D_{MAS,Ala}$). The likely source for the deviations are selective RF pulse imperfections which could be compensated by using selective pulse shapes with better performance, for example Gaussian pulse cascades Q3 and Q5 (Emsley and Bodenhausen (1992)) or optimal control derived selective pulses (Matson et al. (2009)).

The increased degree of experimental freedom enabled by Sel-BPP-LED is demonstrated in Figure 2b,c and Figure 3b. Figure 2b reveals that the water signal fully decays well before the MAS when using the same gradient amplitude across all signals. Adjusting the gradient amplitude range for the water signal to apply 1 - 60% of maximum strength was found to be sufficient to reach full decay at the end of the experiment. In the *same* experiment, the MAS signals were simultaneously exposed to gradient amplitudes ranging from 1 - 95% of maximum strength, appropriate to sample the intensity decay curve for the larger molecule. As a result, the Sel-BPP-LED experiment enables parallel diffusion measurements of molecules of vastly different diffusive properties by selectively encoding the appropriate diffusion experimental parameter (i.e. gradient amplitude in this case) into a well resolved signal.

Selective variants of numerous NMR experiments have been realized since the idea of converting multi-dimensional to 1D experiments using selective pulses was reported (Kessler et al. (1986)). Such experiments are often exploited to simplify otherwise complex spectra (Kiraly et al. (2021); Alexandersson et al. (2020); Poggetto et al. (2017); MacKinnon et al. (2016); Pelupessy et al. (1999)), to suppress strong signals that dominate the dynamic range (Cutting et al. (2000)), or to selectively drive desired coherence pathways (Haller et al. (2019); Ferrage et al. (2004); Chiarparin et al. (1998)). Diffusion experiments have also benefited from the addition of selectivity, to reduce the influence of strong solvent signals in biomolecular samples (Shukla and Dorai (2011); Yao et al. (2014)), to focus the diffusion experiment onto select molecules in a complex mixture (Lyu et al. (2018)), or to use the diffusion dimension as an access point to further selective-based NMR experiments (e.g. selective TOCSY (Lyu et al. (2018)) and supplemented with relaxation encoding (Poggetto et al. (2017))).

The selective experiment described in this report offers the same advantages in terms of signal suppression and reducing complexity. A key difference compared to previous selective diffusion reports is the encoding of information into individual resonances. This is in contrast to the method described by Howe (Howe (2017)), who demonstrated diffusion measurements by selective excitation of four resonances. Since every resonance was exposed to the same experiment parameters, all four resonances could be simultaneously excited resulting in a net gain in time per scan compared to the experiment described here.

Yao and colleagues demonstrated a selective diffusion experiment using selective pulses of larger bandwidth (~2 kHz) (Yao et al. (2014)) and therefore also gained in experimental time per scan. The benefit of the Sel-BPP-LED experiment (in fact we are not limited to BPP-LED, any diffusion experiment should be compatible with the concept) is the ability to parallelize measurements, accessing diffusion information from multiple sample species in a single experiment.

The limit to the number of selective units, n, in the selective diffusion experiment is governed by i) the desired bandwidth to be selectively encoded, ii) the desired diffusion time Δ , and, related, iii) the T_1 relaxation of the selected signals. For the worst case scenario, selectivity with small bandwidth of multiple resonances with short T_1 will not be possible since the resulting diffusion time would be too long and signal intensity would be lost to relaxation. In the experiment demonstrated here, a selective bandwidth of $60 \, \text{Hz}$ was used exclusively, requiring selective pulse lengths of $26.8 \, \text{ms}$ and $14.7 \, \text{ms}$ for excitation



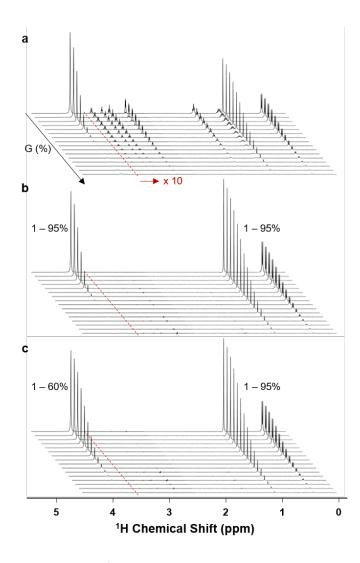


Figure 2. Exemplary 1H NMR spectra of $20 \,\mathrm{mg}\,\mathrm{mL}^{-1}$ Met-Ala-Ser (MAS) tripeptide, non-selective (a) and selective (b,c) diffusion experiments. The resonances used for selective encoding were: water (4.8 ppm), Met methyl group of MAS (2.1 ppm), and Ala methyl group of MAS (1.5 ppm). Demonstrated in c, using selective encoding the gradient amplitude experienced by the water signal could be controlled independent of that experienced by the MAS signals (1-60% vs. 1-95%). In all plots, the intensity of the region from 1 - 4.5 ppm was increased by a factor of 10 for clarity (highlighted in a).

and refocusing. This limited the diffusion times $\Delta > 3 \times 68.3 \,\mathrm{ms}$ for the 3 signals selectively encoded, or more generally $\Delta > n \times (2 \times t_{90,sel} + t_{180,sel} + \delta)$. Shorter diffusion times can be accessed by selectively encoding spectral regions instead of individual resonances, thereby reducing the required length of the selective pulse. This has been demonstrated for protein and peptide diffusion measurements, selectively exciting bandwidths on the order of $2 \,\mathrm{kHz}$ with the benefit of relatively short selective pulse lengths on the order of $2.5 \,\mathrm{ms}$ (Yao et al. (2014)). Encoding more than one resonance with the same diffusion





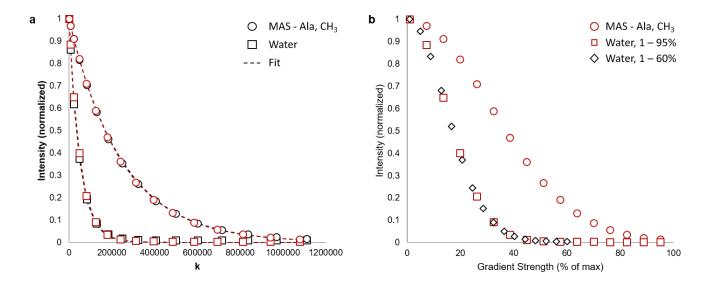


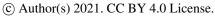
Figure 3. a) Comparison of signal intensity versus the diffusion experiment parameter $k = \gamma^2 G^2 \delta^2 (\Delta - (\delta/3) - (\tau/2))$ for the alanine methyl signal of Met-Ala-Ser (MAS, circles) and the water signal (squares). Black symbols: the experiment was non-selective; red symbols: selective excitation was used. The dashed lines are the fits to the data using Equation 1. The adjusted R^2 values were all > 0.999. The diffusion time was $\Delta = 250$ ms. b) Comparison of signal intensity versus applied strength gradient (% of maximum) for the water (squares, diamonds) and MAS-Ala methyl (circles) signals using Sel-BPP-LED. Using the selective experiment, the applied gradient strength experienced by the water signal could be varied independently of the applied gradient strength experienced by MAS. Diamonds: applied gradient strength varied from 1 - 60%. Using the selective excitation experiment, MAS signals were always exposed to an applied gradient varying from 1 - 95%. The experiments were performed in triplicate, the mean values are plotted. The diffusion time was $\Delta = 250$ ms.

parameters would also be possible using pulses with multi-selectivity, effectively reducing n and also enabling access to shorter diffusion times.

3 Conclusions

Taking advantage of individual resonances as a means to encode additional, unique information into a single experiment is a means to achieve measurement parallelization. For each unique encoding n, experimental time is accelerated by a factor n. In this work a Sel-BPP-LED diffusion experiment demonstrated this concept, with each selectively manipulated resonance encoded with a unique diffusion gradient amplitude. While demonstrated for the BPP-LED experiment, the concept is general and can be applied to any diffusion pulse sequence. Selective encoding enables the simultaneous measurement of diffusion coefficients of sample mixture components experiencing different transport properties dictated by molecular size or selective restriction via matrix interactions. This principle could be extended to anisotropic diffusion by encoding gradient directions

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into different resonances. To improve the experiment, selective RF pulses with better performance should be explored to avoid systematic deviations in the extracted diffusion coefficients.

Code availability. The Sel-BPP-LED pulse program, tested using TopSpin 3.6.3, is available at https://doi.org/10.5281/zenodo.5105713.

Data availability. The NMR data is available at https://doi.org/10.5281/zenodo.5105713.

Author contributions. Conceptualization: PS, MJ, JGK. Formal Analysis: NM. Investigation: NM, MA, TG. Supervision: BL, MJ, JGK. Visualization: NM. Writing - original draft: JGK and NM. Writing - review and editing: all authors.

150 Competing interests. The authors declare no competing interests.

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